

# Shabal

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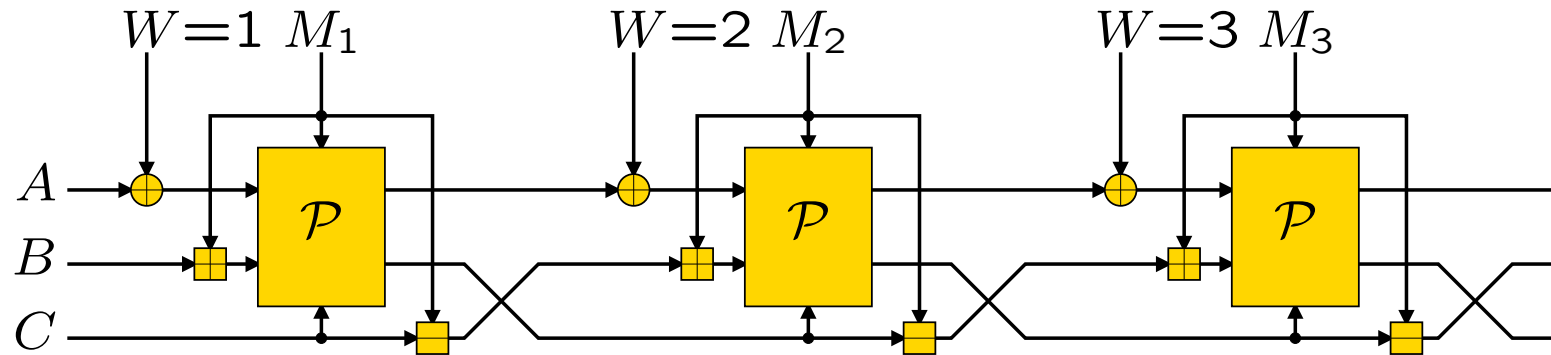
The second SHA-3 Candidate Conference, August 24, 2010

How does Chabal look like?



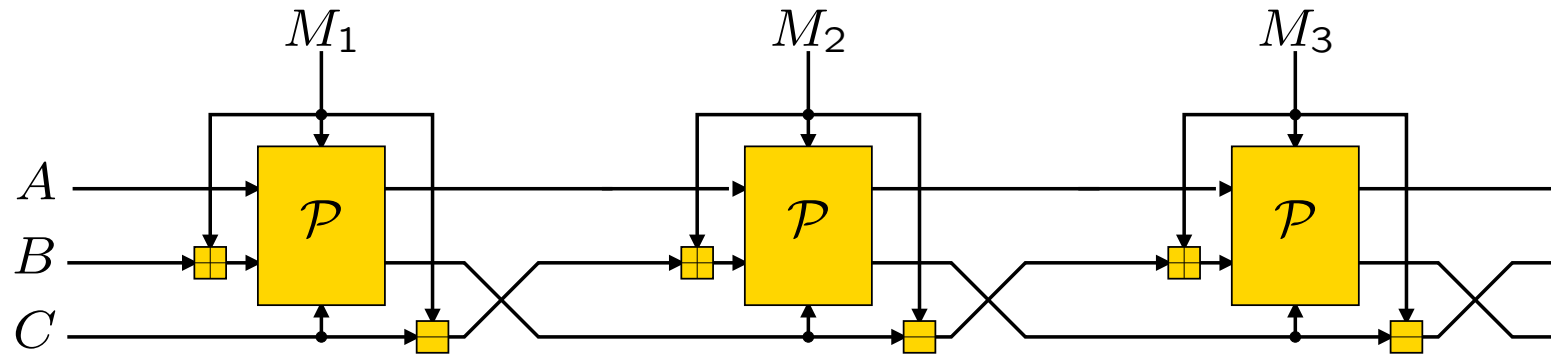
[http://commons.wikimedia.org/wiki/File:Sebastien-Chabal\\_large.jpg](http://commons.wikimedia.org/wiki/File:Sebastien-Chabal_large.jpg)

## How does Shabal look like?

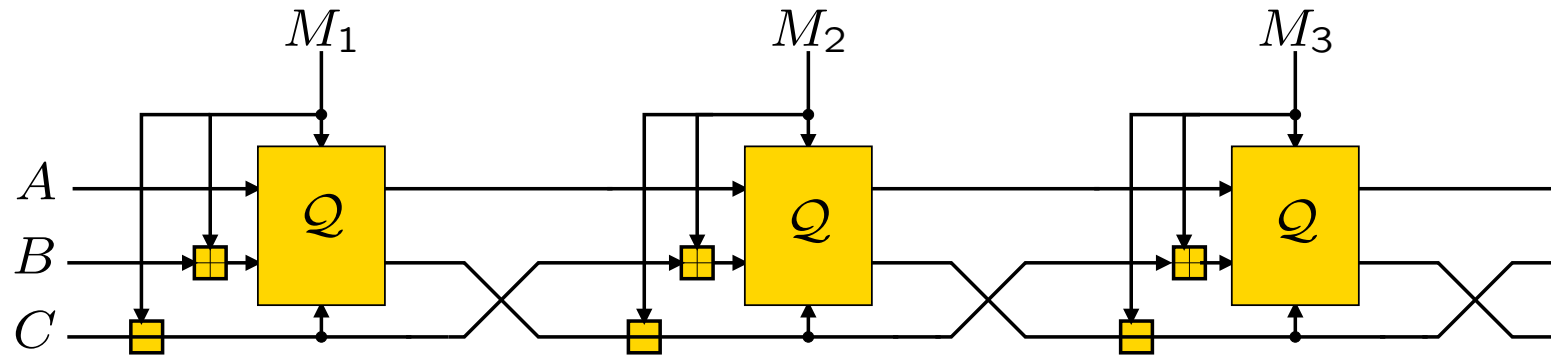


- no tweak;
- same function for all output sizes;
- 1408-bit internal state and 512-bit message blocks;
- 3 additional blank rounds parametrized by the last message block without incrementing the counter;

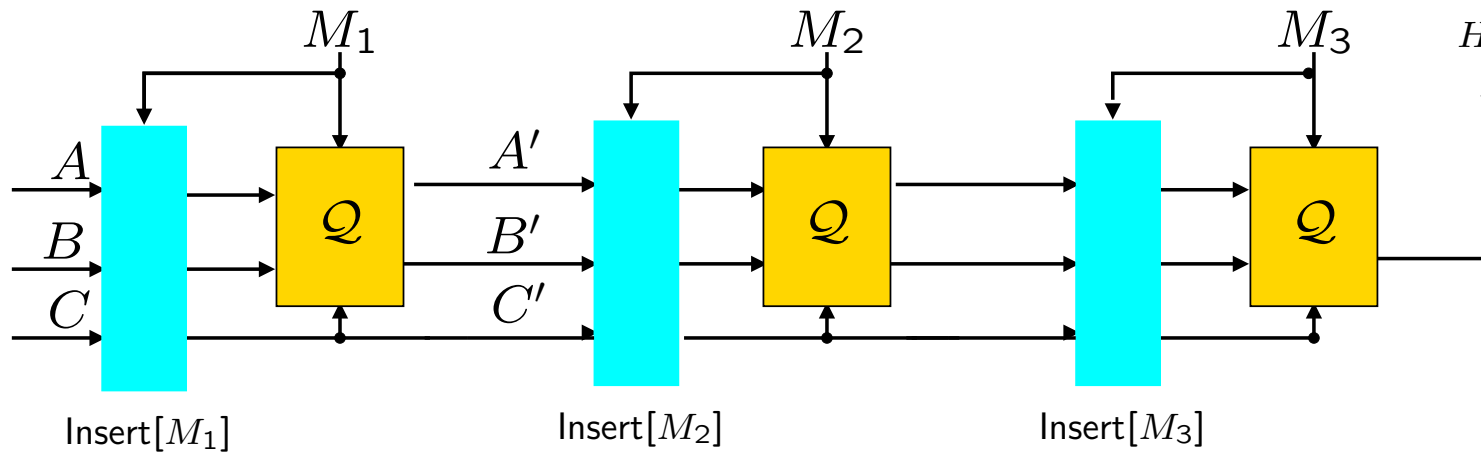
## Equivalent mode of operation



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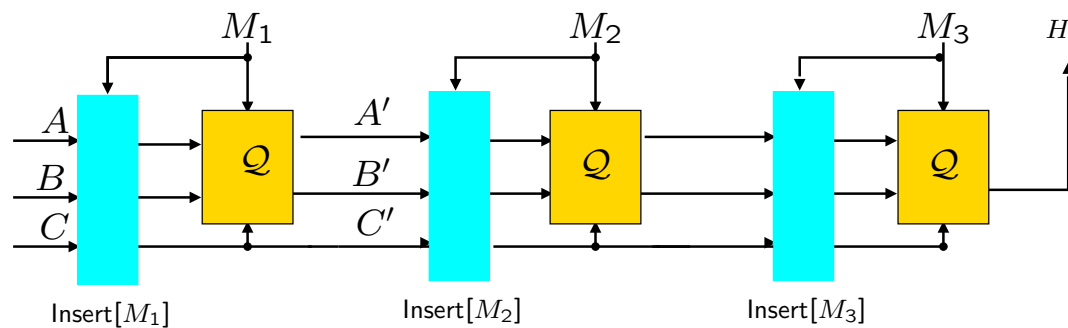
## General mode of operation



### Example.

For  $\ell_c = 0$  and  $\text{Insert} = \text{Id}$ , it corresponds to chop-MD.

# Indifferentiability



## Indifferentiability bound.

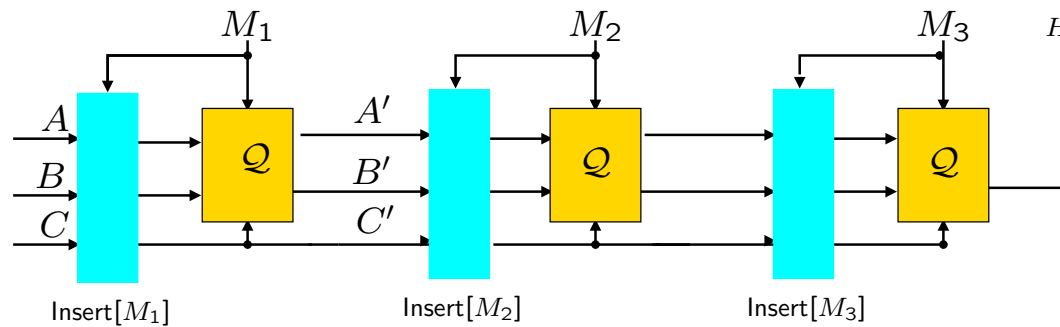
If  $\mathcal{Q}$  is an ideal keyed permutation on  $m$ -bit inputs,

$$\min \left( 2^{\frac{m}{2}}, 2^{m - \ell_h - \log \ell_h} \right).$$

With prefix-free encoding,

$$2^{\frac{m}{2}}$$

# Indifferentiability



## Indifferentiability bound.

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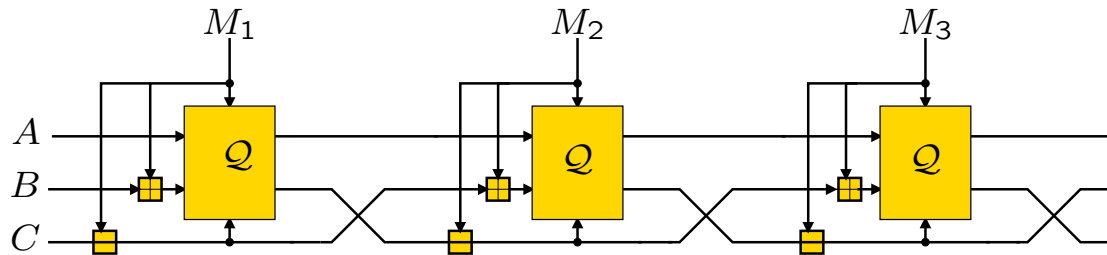
Realistic model for the finalization: with blank rounds, if the insertion function is well-chosen (e.g. in Shabal),

$$\min 2^{\frac{m}{2}}, 2^{m+\ell_c-\ell_h-\log \ell_h}.$$

Indifferentiability up to  $2^{448}$  queries compared to  $2^{128}$  or  $2^{256}$  for single-pipe designs [Blake, Hamsi, SHAvite-3, Skein].



## Second-preimage resistance



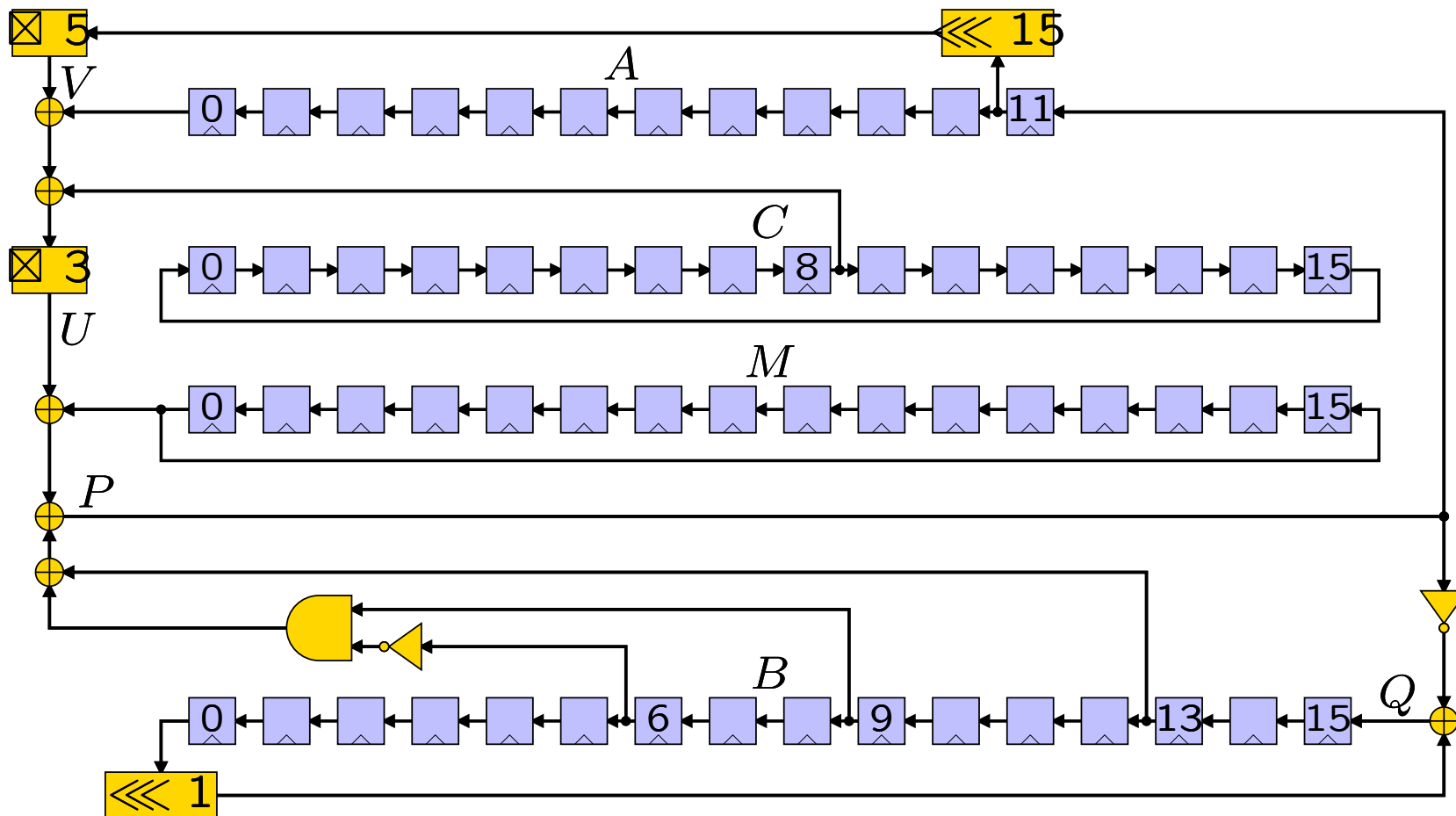
### Bound on second-preimage resistance (besides the generic preimage attack).

If  $Q$  is an ideal keyed permutation on  $m$ -bit inputs, for  $\kappa$ -block messages, the number of queries for a 2nd-preimage attack is at least

$$\frac{1}{8} \min \left( 2^{m - \log \ell_c}, 2^{m + \ell_c - \log \kappa}, 2^{\frac{m + \ell_c}{2}} \right).$$

Proven 2nd-preimage resistance (besides the generic attack) up to  $2^{702}$  queries compared to existing 2nd-preimage attacks with complexity  $2^{513}$  for Keccak-512,  $2^{453}$  for Cubehash 16/32...

## Shabal keyed permutation

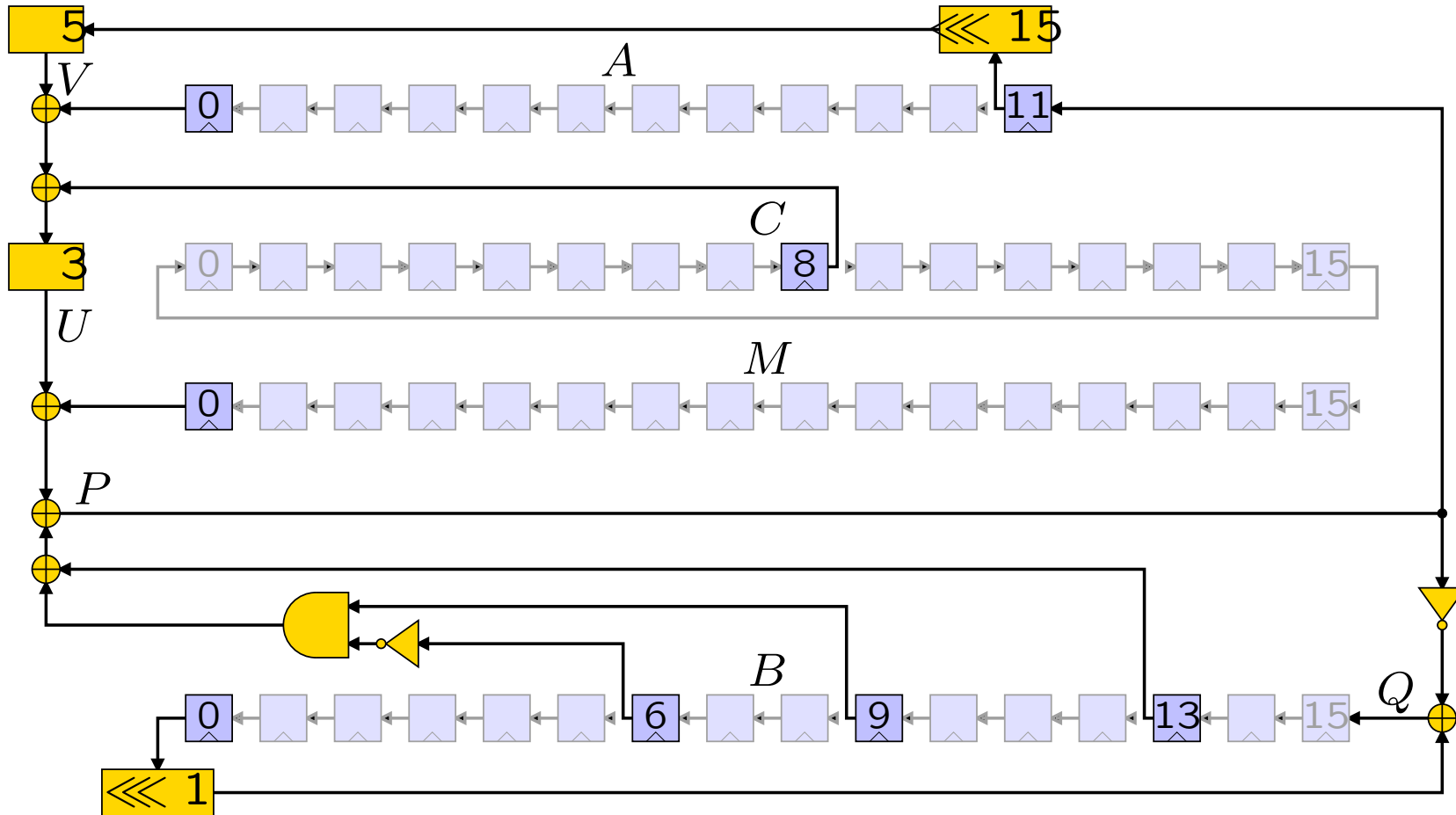


For  $i = 0, \dots, 15$ :  $B[i] \leftarrow B[i] \lll 17$

Apply 48 *steps*

For  $i = 0, \dots, 35$ :  $A[i \bmod 12] \leftarrow A[i \bmod 12] \boxplus C[(i + 3) \bmod 16]$

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Can you find him?



## Distinguishers on the inner permutation



### Non-dependencies of the inverse permutation [Shabal 08]

[Aumasson 09],[Shabal 09].

The number of preimages for a given  $(y, M)$  may be only  $2^{m-96}$ .

### Differential distinguishers [Aumasson et al. 09], [Novotney 10],[Isobe-Shirai 10].

Let  $\Delta$  be a difference on the msb of each word of  $M$ .

Then,  $(X, M)$  and  $(X \oplus f(\Delta), M \oplus \Delta)$  are related.

### Rotational distinguisher [van Assche 10].

$$\mathcal{P}(X \lll 1, M \lll 1) = \mathcal{P}(X, M) \lll 1$$

with probability  $2^{-159}$ .

### Fixed points [Knudsen et al. 09].

## New indistinguishability proof for a “biased” permutation

New framework [eprint 09].

It assumes that  $\mathcal{Q}$  is drawn uniformly at random from  $\text{FUNC}' \subset \text{FUNC}$ .

Types of distinguishers which can be included:

- bias in the distribution of the output [eprint 09];
- related (input, output) pairs, e.g. differential and rotational distinguishers [this paper];
- weak inputs, e.g. fixed points [eprint 09].

**New indistinguishability bound taking into account all known distinguishers.**

Shabal is indistinguishable from a random oracle up to  $2^{332}$  queries.

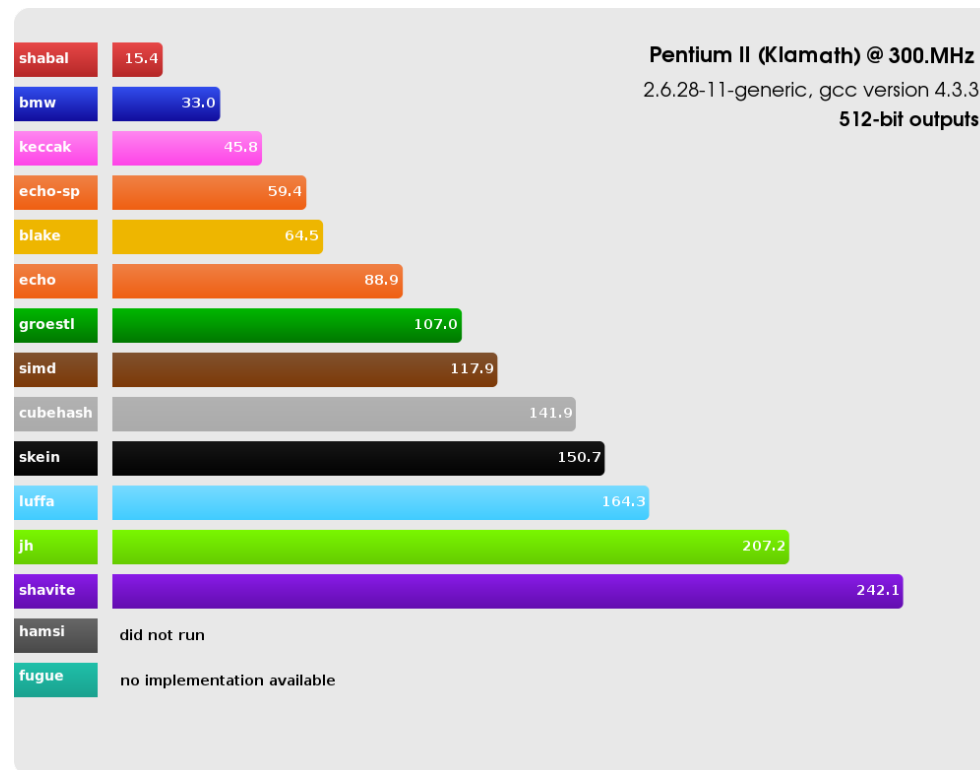
## Analysis of weakened variants

- (second)-preimage attack in  $2^{497}$  in time and  $2^{400}$  in memory for 32 out of 48 rounds and without the final transformation in the inner permutation [Shabal team 09][Isobe, Shirai 10];
- (second)-preimage attack in  $2^{497}$  in time and  $2^{272}$  in memory for 24 out of 48 rounds and for a permutation with 768-bit inputs (instead of 896) [Isobe, Shirai 10].

## Software performances

Smallest number of 32-bit arithmetic instructions per hashed bit  
[Jos, Stefan 10]

→ Among the fastest two candidates on almost any platform



512-bit output, Pentium II <http://crypto.rd.francetelecom.com/ECH0/sha3/>

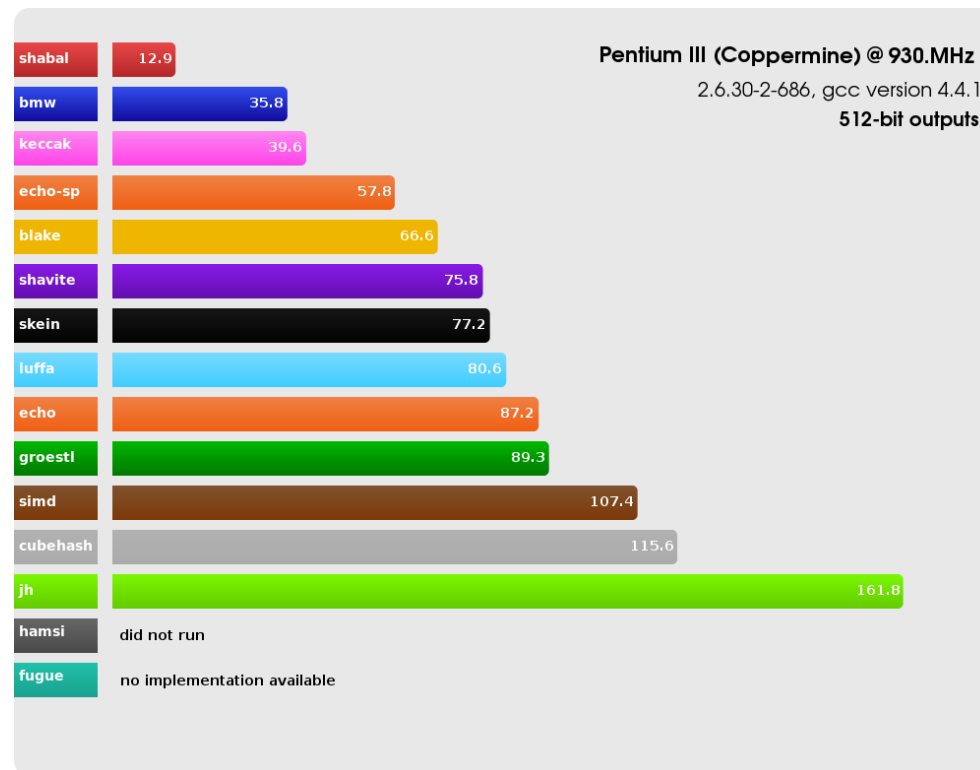
without 64-bit/AES/SIMD instructions.



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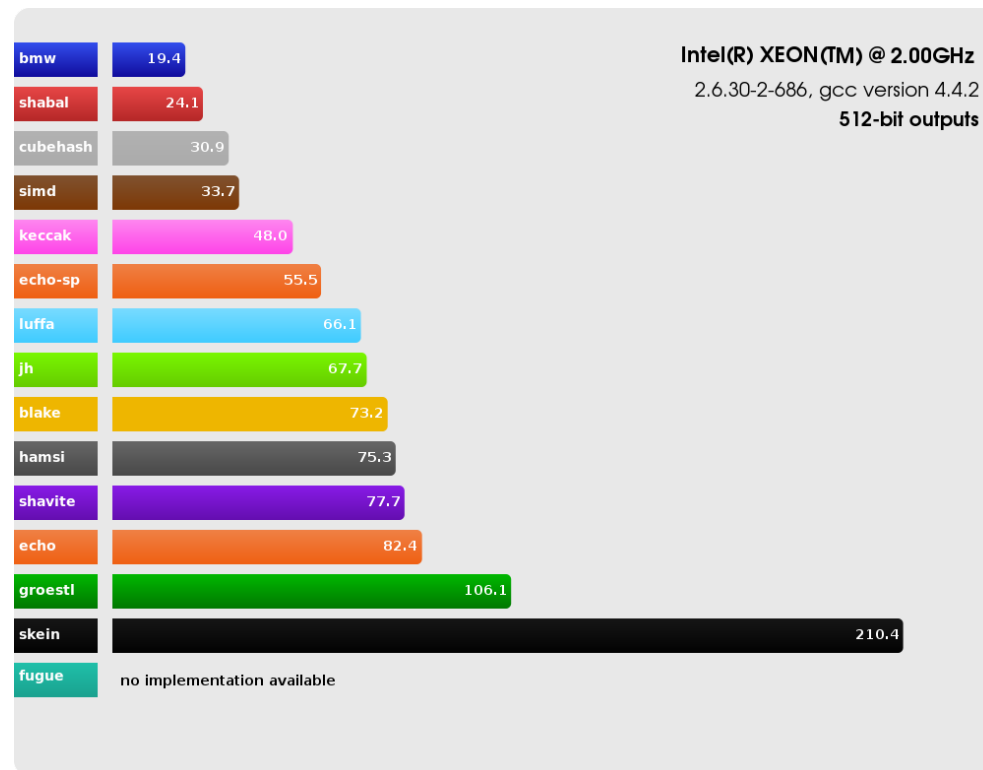


512-bit output, Pentium III <http://crypto.rd.francetelecom.com/ECH0/sha3/>  
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512-bit output, Xeon <http://crypto.rd.francetelecom.com/ECHO/sha3/>

without 64-bit/AES/SIMD instructions.

## Shabal can be made very small



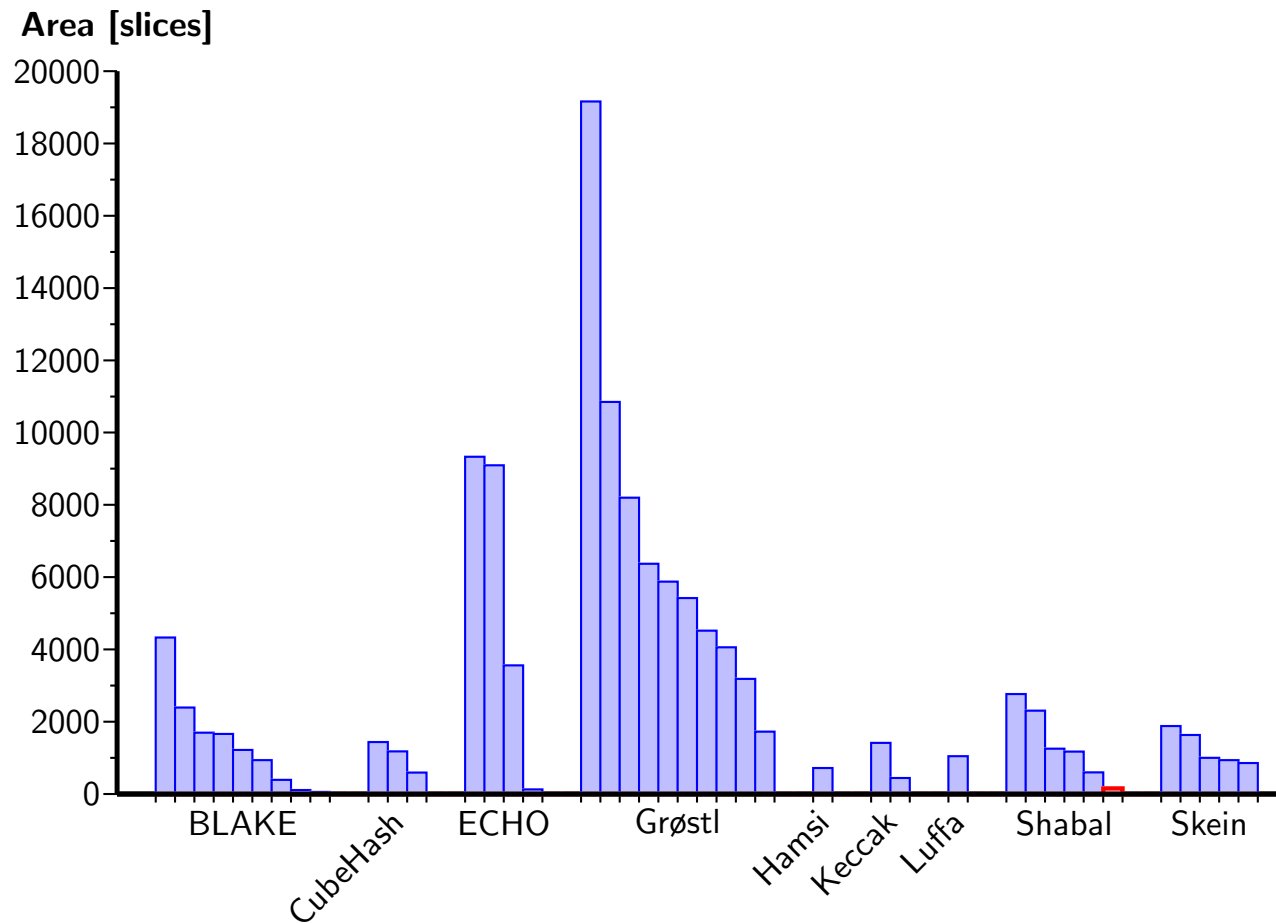
Compact implementation [Pornin 10].

Code size: 698 bytes

109 MB/s on a 2.4 GHz Core2 machine.

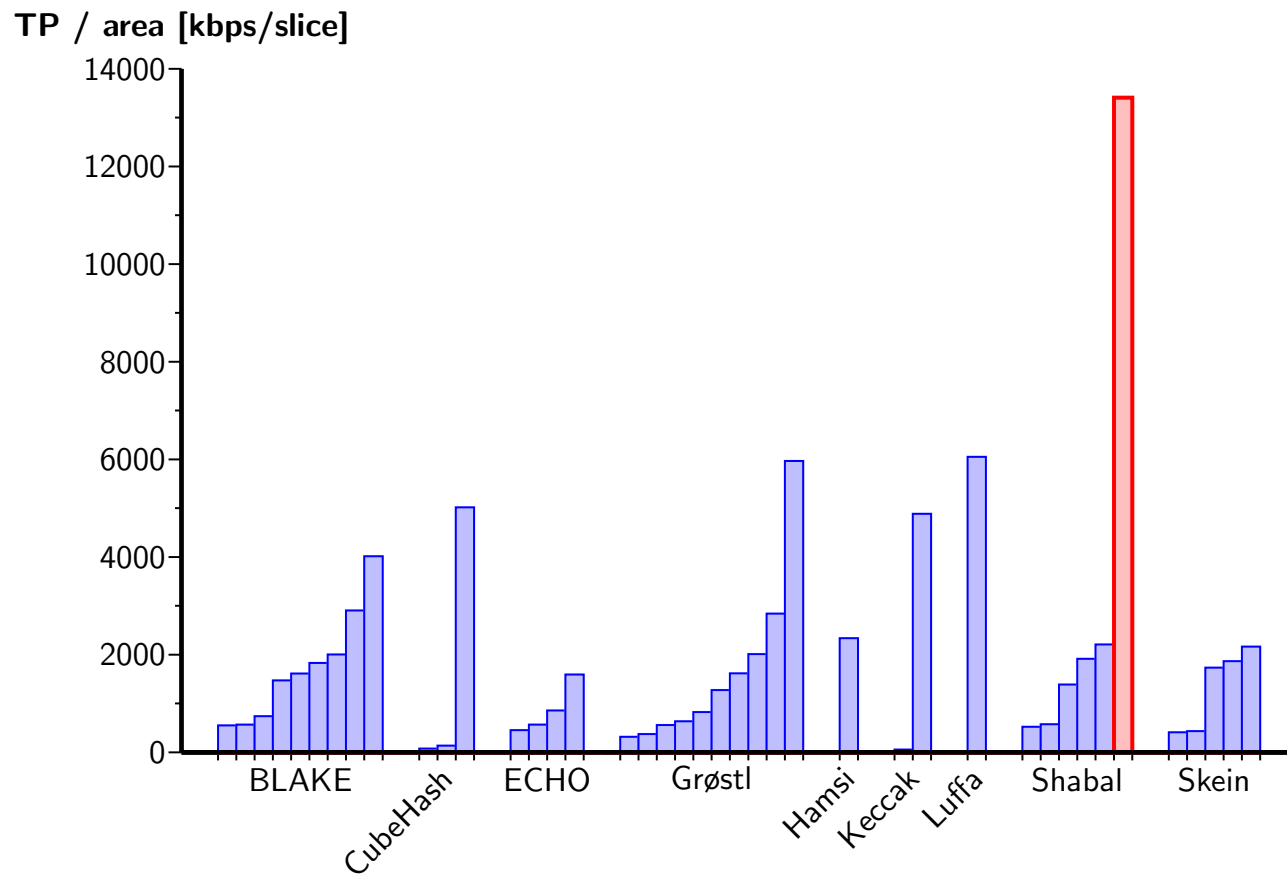
## Hardware performances on Xilinx

[Detrey-Gaudry-Khalfallah 10, presented at SAC 2010]



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## Why choosing Shabal?

- it has security proofs (indifferentiability, collision resistance and second-preimage resistance) which provide **important safety margins**;
- it has been studied by many external teams;
- single function for all output lengths;
- very fast software implementations (without any tricks);
- small footprint (in software and hardware).

## Why choosing Shabal?

Otherwise, he won't be happy...

