

# **Combinatorial Testing**

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### **Tutorial Overview**

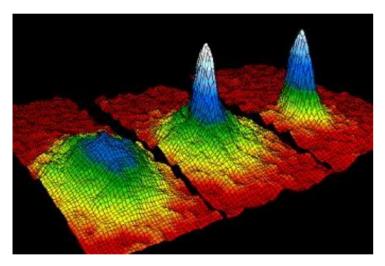


- 1. Why are we doing this?
- 2. What is combinatorial testing?
- 3. How is it used and how long does it take?
- 4. What tools are available?
- 5. What's next?

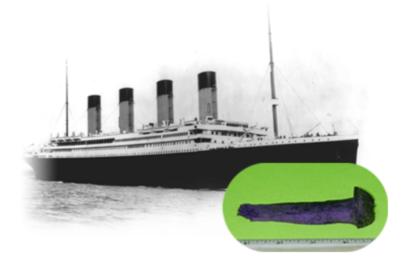
### What is NIST and why are we doing this?

- A US Government agency
- The nation's measurement and testing laboratory – 3,000 scientists, engineers, and support staff including 3 Nobel laureates





Research in physics, chemistry, materials, manufacturing, computer science





Analysis of engineering failures, including buildings, materials, and ...

## **Software Failure Analysis**



- We studied software failures in a variety of fields including 15 years of FDA medical device recall data
- What causes software failures?
  - logic errors?
  - calculation errors?
  - interaction faults?
  - inadequate input checking? Etc.
- What testing and analysis would have prevented failures?
- Would statement coverage, branch coverage, all-values, all-pairs etc. testing find the errors?



### **Software Failure Internals**



How does an interaction fault manifest itself in code?

Example: pressure < 10 & volume > 300 (2-way interaction)

```
if (pressure < 10) {</pre>
    // do something
    if (volume > 300) { faulty code! BOOM! }
    else { good code, no problem}
else {
    // do something else
```

# Pairwise testing is popular, but is it enough?



- Pairwise testing commonly applied to software
- Intuition: some problems only occur as the result of an interaction between parameters/components
- Pairwise testing finds about 50% to 90% of flaws
  - Cohen, Dalal, Parelius, Patton, 1995 90% coverage with pairwise, all errors in small modules found
  - Dalal, et al. 1999 effectiveness of pairwise testing, no higher degree interactions
  - Smith, Feather, Muscetolla, 2000 88% and 50% of flaws for 2 subsystems

90% of flaws.
Sounds pretty good!



### Finding 90% of flaws is pretty good, right?



"Relax, our engineers found 90 percent of the flaws."

I don't think I want to get on that plane.

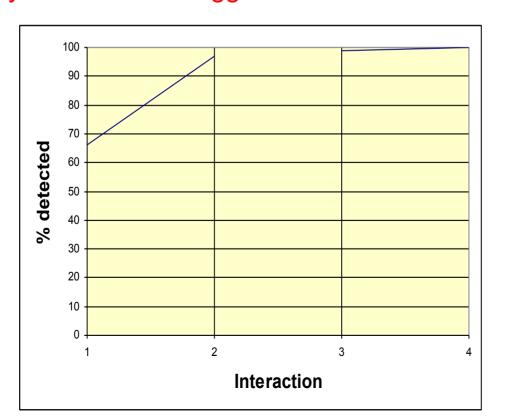




### How about hard-to-find flaws?



- •Interactions e.g., failure occurs if
- pressure < 10 (1-way interaction)</li>
- pressure < 10 & volume > 300 (2-way interaction)
- pressure < 10 & volume > 300 & velocity = 5 (3-way interaction)
- The most complex failure reported required
   4-way interaction to trigger





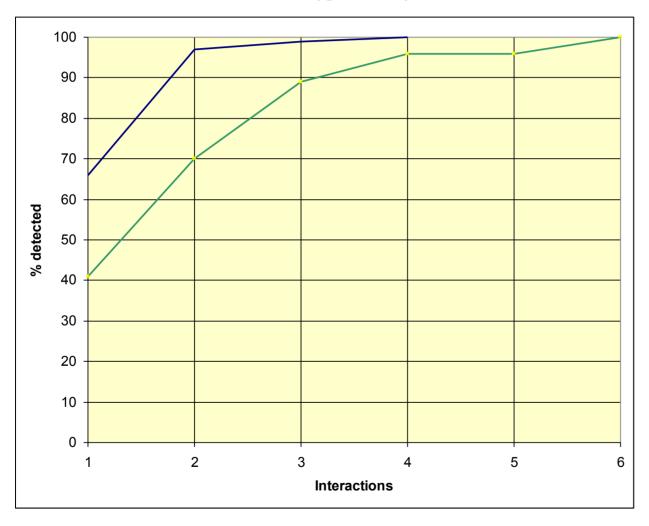
Interesting, but that's just one kind of application.



## How about other applications?



### Browser (green)



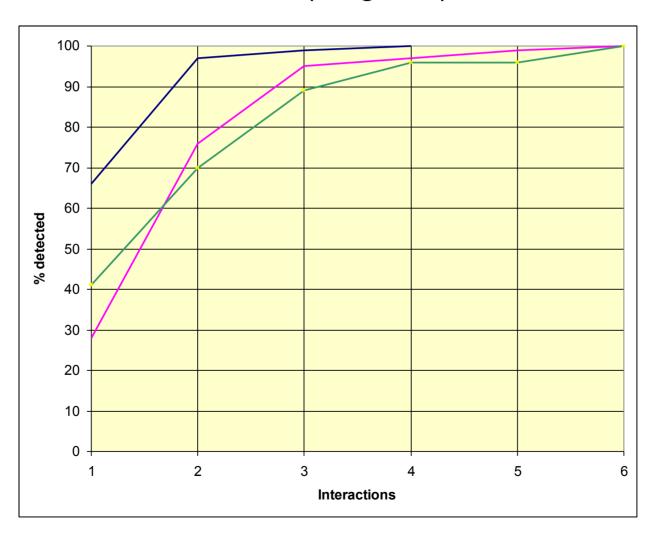
These faults more complex than medical device software!!

Why?

## And other applications?



### Server (magenta)

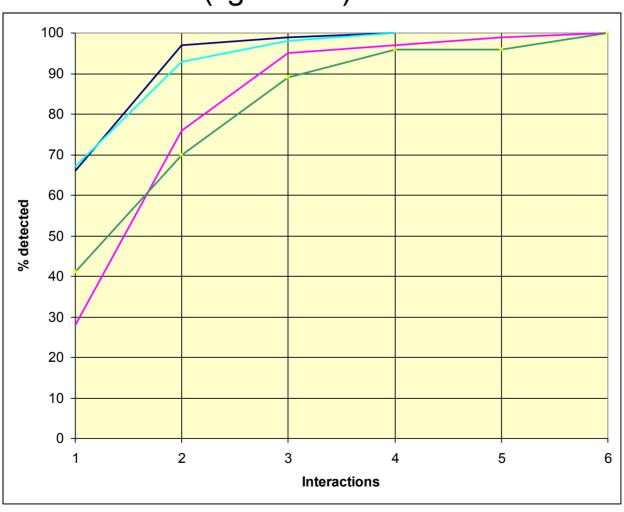


### Still more?



### NASA distributed database

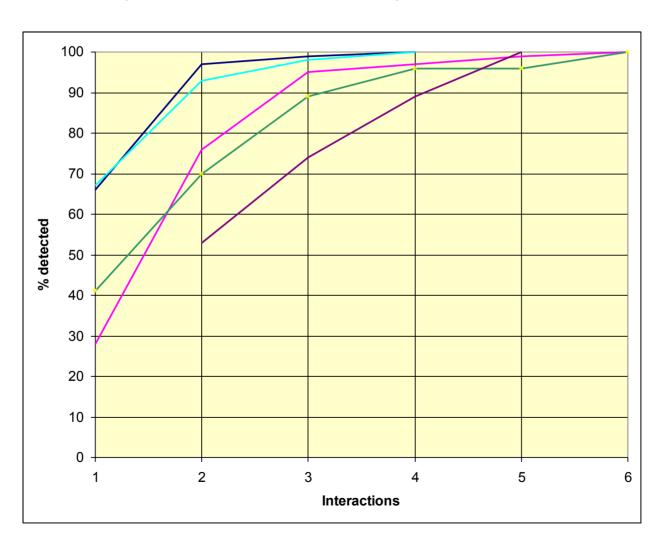
(light blue)



### **Even more?**



# Traffic Collision Avoidance System module (seeded errors) (purple)

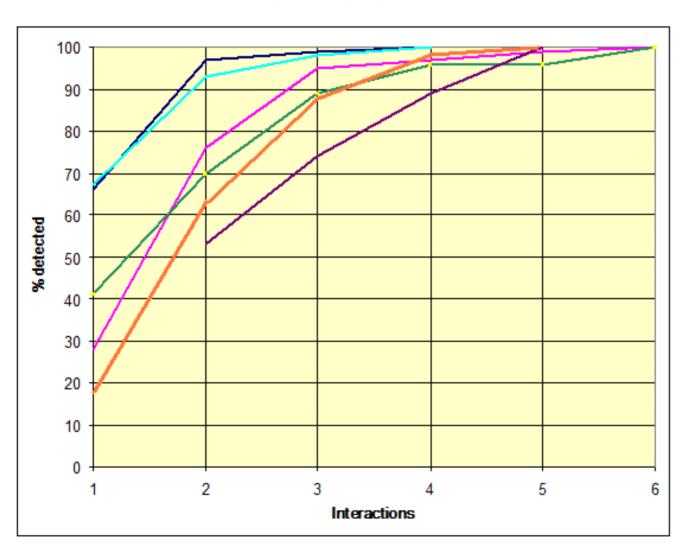


## **Finally**



### Network security (Bell, 2006)

(orange)

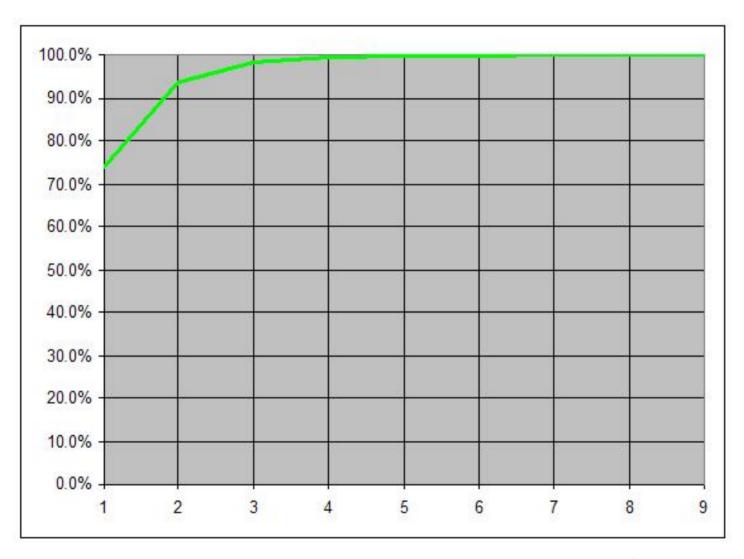


Curves appear to be similar across a variety of application domains.

Why this distribution?

### What causes this distribution?

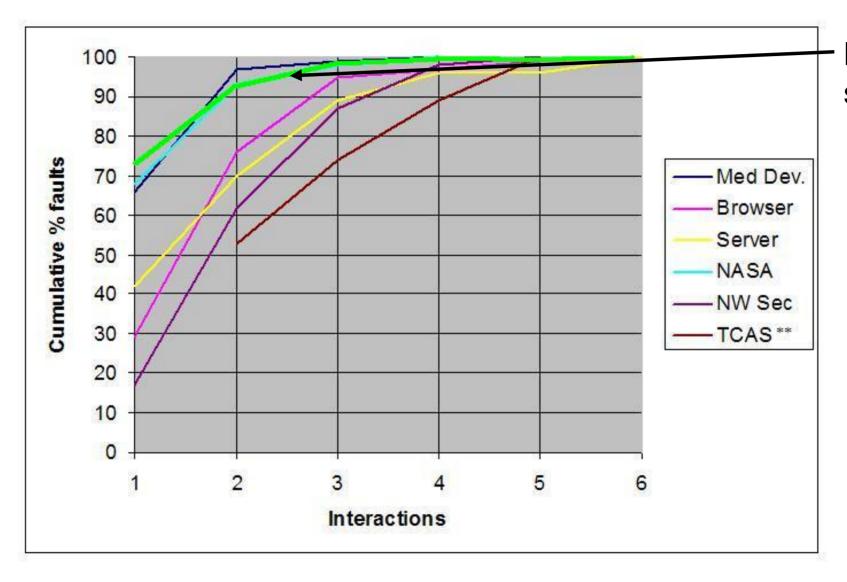




One clue: branches in avionics software. 7,685 expressions from *if* and *while* statements

# Comparing with Failure Data





Branch statements



# So, how many parameters are involved in really tricky faults?

- Maximum interactions for fault triggering for these applications was 6
- Much more empirical work needed
- Reasonable evidence that maximum interaction strength for fault triggering is relatively small

How does it help me to know this?





### How does this knowledge help?

Biologists have a "central dogma", and so do we:

If all faults are triggered by the interaction of *t* or fewer variables, then testing all *t*-way combinations can provide strong assurance

(taking into account: value propagation issues, equivalence partitioning, timing issues, more complex interactions, ...)

Still no silver bullet. Rats!



### **Tutorial Overview**



1. Why are we doing this?

# 2.What is combinatorial testing?

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# What is combinatorial testing? A simple example

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## **How Many Tests Would It Take?**

- There are 10 effects, each can be on or off
- All combinations is  $2^{10} = 1,024$  tests
- What if our budget is too limited for these tests?
- Instead, let's look at all 3-way interactions ...



# **Now How Many Would It Take?**

- There are  $\begin{bmatrix} 10 \\ 3 \end{bmatrix}$  = 120 3-way interactions. Naively 120 x 2<sup>3</sup> = 960 tests.
- Since we can pack 3 triples into each test, we need no more than 320 tests.
- Each test exercises many triples:

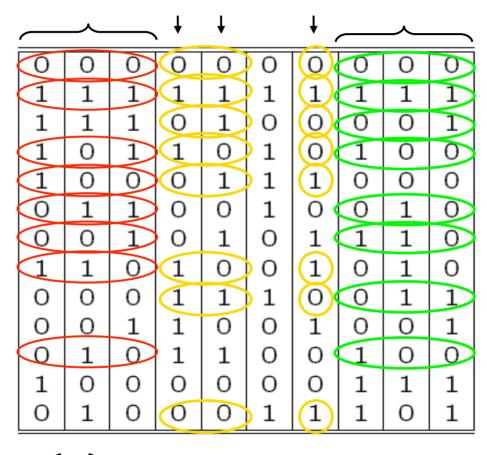
We can pack a lot into one test, so what's the smallest number of tests we need?



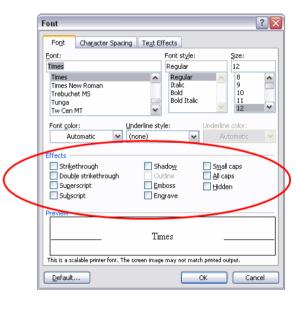
# A covering array

All triples in only 13 tests, covering  $\begin{bmatrix} 10\\3 \end{bmatrix} 2^3 = 960$  combinations

Each row is a test:



Each column is a parameter:

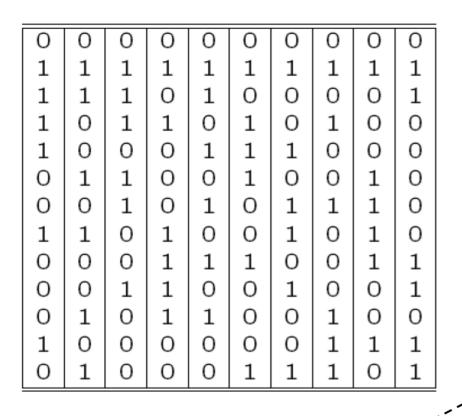


Each test covers  $\binom{10}{3}$  = 120 3-way combinations

Finding covering arrays is NP hard





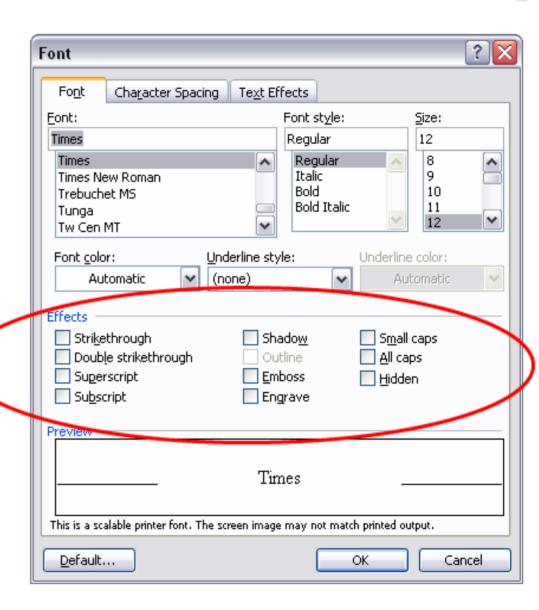


0 = effect off

1 = effect on

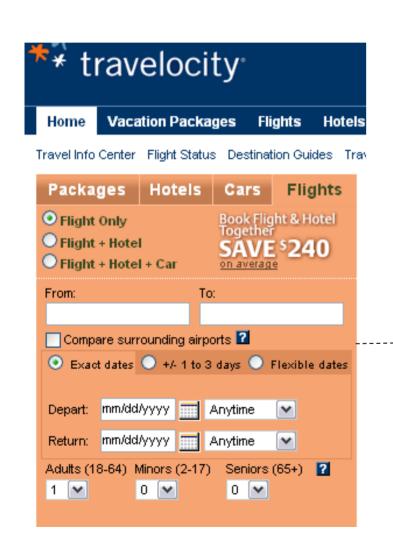
13 tests for all 3-way combinations

 $2^{10}$  = **1,024** tests for all combinations





## **Another familiar example**



#### No silver bullet because:

Many values per variable Need to abstract values

But we can still increase information per test

Plan: flt, flt+hotel, flt+hotel+car

From: CONUS, HI, Europe, Asia ...

To: CONUS, HI, Europe, Asia ...

Compare: yes, no

Date-type: exact, 1to3, flex

Depart: today, tomorrow, 1yr, Sun, Mon ...

Return: today, tomorrow, 1yr, Sun, Mon ...

Adults: 1, 2, 3, 4, 5, 6

Minors: 0, 1, 2, 3, 4, 5

Seniors: 0, 1, 2, 3, 4, 5

# A larger example

Suppose we have a system with on-off switches:





### How do we test this?

34 switches =  $2^{34}$  = 1.7 x  $10^{10}$  possible inputs = 1.7 x  $10^{10}$  tests





# What if we knew no failure involves more than 3 switch settings interacting?

- 34 switches =  $2^{34}$  = 1.7 x  $10^{10}$  possible inputs = 1.7 x  $10^{10}$  tests
- If only 3-way interactions, need only 33 tests
- For 4-way interactions, need only 85 tests





### **Tutorial Overview**

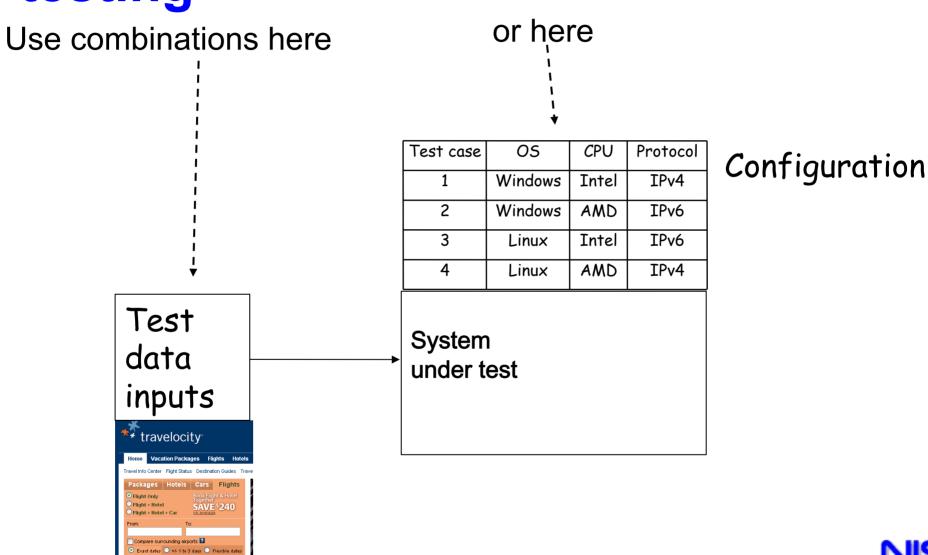


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# Two ways of using combinatorial testing





### **Testing Configurations**

- Example: app must run on any configuration of OS, browser, protocol, CPU, and DBMS
- Very effective for interoperability testing

Test	os	Browser	Protocol	CPU	DBMS
1	XP	ΙΕ	IPv4	Intel	MySQL
2	XP	Firefox	IPv6	AMD	Sybase
3	XP	IE	IPv6	Intel	Oracle
4	OS X	Firefox	IPv4	AMD	MySQL
5	OS X	ΙΕ	IPv4	Intel	Sybase
6	OS X	Firefox	IPv4	Intel	Oracle
7	RHL	ΙΕ	IPv6	AMD	MySQL
8	RHL	Firefox	IPv4	Intel	Sybase
9	RHL	Firefox	IPv4	AMD	Oracle
10	OS X	Firefox	IPv6	AMD	Oracle



### Combinatorial testing with existing test set

- Use t-way coverage for system configuration values
- 2. Apply existing tests

Test case	OS	CPU	Protocol
1	Windows	Intel	IPv4
2	Windows	AMD	IPv6
3	Linux	Intel	IPv6
4	4 Linux		IPv4

Common practice in telecom industry



### **Modeling & Simulation Application**

- "Simured" network simulator
  - Kernel of ~ 5,000 lines of C++ (not including GUI)
- Objective: detect configurations that can produce deadlock:
  - Prevent connectivity loss when changing network
  - Attacks that could lock up network
- Compare effectiveness of random vs. combinatorial inputs
- Deadlock combinations discovered
- Crashes in >6% of tests w/ valid values (Win32 version only)

### **Simulation Input Parameters**

	Parameter	Values
1	DIMENSIONS	1,2,4,6,8
2	NODOSDIM	2,4,6
3	NUMVIRT	1,2,3,8
4	NUMVIRTINJ	1,2,3,8
5	NUMVIRTEJE	1,2,3,8
6	LONBUFFER	1,2,4,6
7	NUMDIR	1,2
8	FORWARDING	0,1
9	PHYSICAL	true, false
10	ROUTING	0,1,2,3
11	DELFIFO	1,2,4,6
12	DELCROSS	1,2,4,6
13	DELCHANNEL	1,2,4,6
14	DELSWITCH	1,2,4,6

5x3x4x4x4x4x2x2x 2x4x4x4x4x4 = 31,457,280 configurations

Are any of them dangerous?

If so, how many?

Which ones?



### **Network Deadlock Detection**

# Deadlocks Detected: combinatorial

			1000	2000	4000	8000
t	Tests	500 pkts	pkts	pkts	pkts	pkts
2	28	0	0	0	0	0
3	161	2	3	2	3	3
4	752	14	14	14	14	14

## Average Deadlocks Detected: random

			1000	2000	4000	8000
t	Tests	500 pkts	pkts	pkts	pkts	pkts
2	28	0.63	0.25	0.75	0.50	0.75
3	161	3	3	3	3	3
4	752	10.13	11.75	10.38	13	13.25





### **Network Deadlock Detection**

Detected 14 configurations that can cause deadlock:  $14/31,457,280 = 4.4 \times 10^{-7}$ 

Combinatorial testing found more deadlocks than random, including some that might never have been found with random testing

Why do this testing? Risks:

- accidental deadlock configuration: low
- deadlock config discovered by attacker: much higher (because they are looking for it)

## **Testing inputs**

- Traffic Collision Avoidance System (TCAS) module
  - Used in previous testing research
  - 41 versions seeded with errors
  - 12 variables: 7 boolean, two 3-value, one 4value, two 10-value
  - All flaws found with 5-way coverage
  - Thousands of tests generated by model checker in a few minutes







#### **Tests generated**

t Test cases

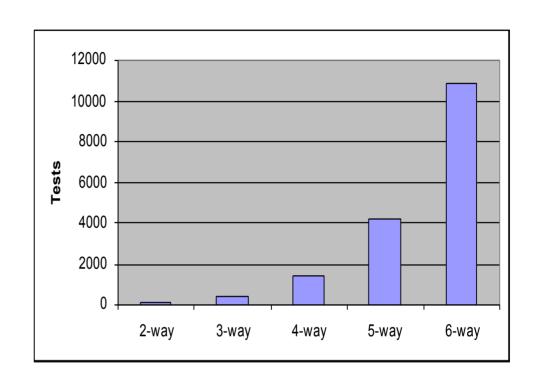
2-way: 156

3-way: 461

4-way: 1,450

5-way: 4,309

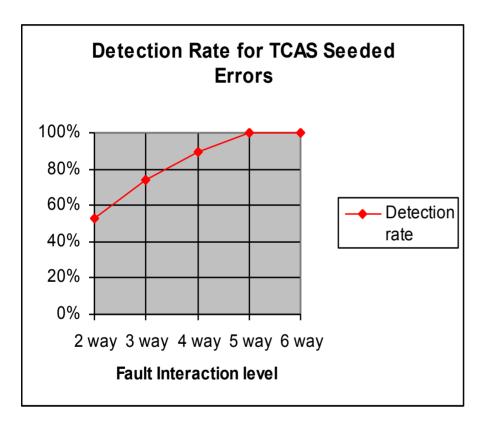
6-way: 11,094

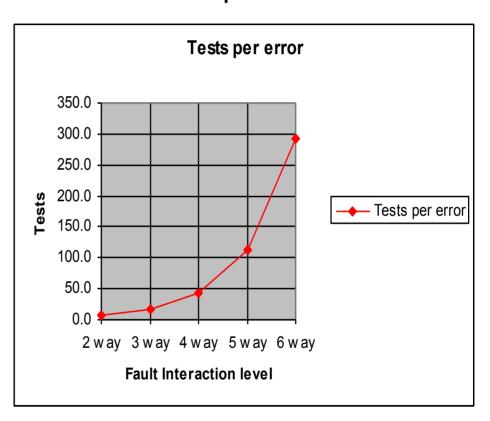


#### Results



- Roughly consistent with data on large systems
- But errors harder to detect than real-world examples

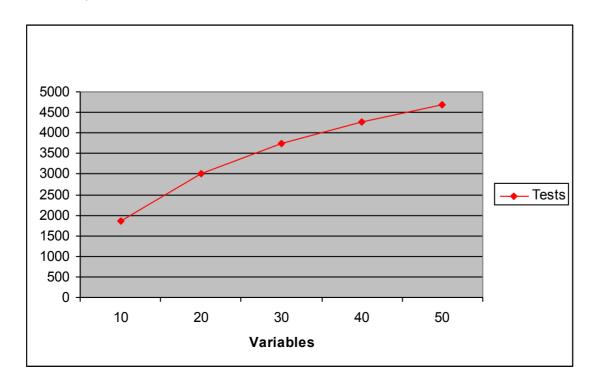




Bottom line for model checking based combinatorial testing: Expensive but can be highly effective

#### **Cost and Volume of Tests**

- Number of tests: proportional to v<sup>t</sup> log n
  for v values, n variables, t-way interactions
- . Thus:
  - •Tests increase exponentially with interaction strength *t* : BAD, but unavoidable
  - •But only logarithmically with the number of parameters : GOOD!
- Example: suppose we want all 4-way combinations of n parameters, 5 values each:





- Empirical data from the National Vulnerability Database
  - Investigated > 3,000 denial-of-service vulnerabilities reported in the NIST NVD for period of 10/06 – 3/07
  - Vulnerabilities triggered by:
    - Single variable 94.7%
       example: Heap-based buffer overflow in the SFTP protocol
       handler for Panic Transmit ... allows remote attackers to execute
       arbitrary code via a long ftps:// URL.
    - 2-way interaction 4.9%
       example: single character search string in conjunction with a single character replacement string, which causes an "off by one overflow"
    - 3-way interaction 0.4%
       example: Directory traversal vulnerability when register\_globals is
       enabled and magic\_quotes is disabled
       and .. (dot dot) in the page parameter





```
1.
     if (strcmp(conn[sid].dat->in RequestMethod, "POST") == 0) {
2.
            if (conn[sid].dat->in ContentLength<MAX POSTSIZE) {</pre>
     conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
sizeof(char));
           pPostData=conn[sid].PostData;
4.
5.
           do {
6.
                    rc=recv(conn[sid].socket, pPostData, 1024, 0);
                      .....
7.
                    pPostData+=rc;
8.
                    x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
10.
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
11.
```



```
if (strcmp(conn[sid].dat->in RequestMethod, "POST") == 0) {
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2.
            if (conn[sid].dat->in ContentLength<MAX POSTSIZE) {</pre>
     conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
3.
sizeof(char));
           pPostData=conn[sid].PostData;
4.
5.
           do {
6.
                    rc=recv(conn[sid].socket, pPostData, 1024, 0);
                      .....
7.
                    pPostData+=rc;
8.
                    x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
10.
11.
```



```
true branch
     if (strcmp(conn[sid].dat->in RequestMethod, "POST")==0) {
1.
2.
            if (conn[sid].dat->in ContentLength<MAX POSTSIZE) {</pre>
     conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
sizeof(char));
           pPostData=conn[sid].PostData;
4.
5.
           do {
6.
                    rc=recv(conn[sid].socket, pPostData, 1024, 0);
                      .....
7.
                   pPostData+=rc;
8.
                    x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
10.
11.
```



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2.
                                                                    true branch
3.
            conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
sizeof(char));
           pPostData=conn[sid].PostData;
4.
           do {
5.
6.
                   rc=recv(conn[sid].socket, pPostData, 1024, 0);
                      .....
7.
                   pPostData+=rc;
8.
                   x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
10.
11.
```



```
if (strcmp(conn[sid].dat->in RequestMethod, "POST")==0) {
1.
            if (conn[sid].dat->in ContentLength<MAX POSTSIZE)
                                                                  true branch
2.
3.
            conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
sizeof(char));
                           Allocate -1000 + 1024 bytes = 24 bytes
           pPostData=conn[sid].PostData;
4.
           do {
5.
6.
                   rc=recv(conn[sid].socket, pPostData, 1024, 0);
                     .....
7.
                   pPostData+=rc;
8.
                   x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
10.
11.
```



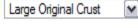
```
if (strcmp(conn[sid].dat->in RequestMethod, "POST")==0) {
1.
            if (conn[sid].dat->in ContentLength<MAX POSTSIZE)</pre>
                                                                   true branch
2.
3.
            conn[sid].PostData=calloc(conn[sid].dat->in ContentLength+1024,
sizeof(char));
                           Allocate -1000 + 1024 bytes = 24 bytes
           pPostData=conn[sid].PostData;
4.
           do {
5.
                                                                       Boom!
                   rc=recv(conn[sid].socket, pPostData, 1024, 0)
6.
                     .....
7.
                   pPostData+=rc;
8.
                   x+=rc;
9.
           } while ((rc==1024)||(x<conn[sid].dat->in ContentLength));
     conn[sid].PostData[conn[sid].dat->in ContentLength]='\0';
10.
11.
```

#### **Ordering Pizza**



Step 1 Select your favorite size and pizza crust.







Select your favorite pizza toppings from the pull down. Whole toppings cover the entire pizza. First ½ and second

1/2 toppings cover half the pizza. For a regular cheese pizza, do not add toppings.

I want to add or remove toppings on this pizza -- add on whole or half pizza.

Extra
Cheese
Remove
Remove
Remove
Remove

6x2<sup>17</sup>x2<sup>17</sup>x2<sup>17</sup>x4x3x2x2x5x2 = WAY TOO MUCH TO TEST

Add toppings whole pizza Add toppings 1st half

Simplified pizza ordering:

6x4x4x4x4x3x2x2x5x2

= 184,320 possibilities

Step 3 Select your pizza instructions.

☑ I want to add special instructions for this pizza -- light, extra or no sauce; light or no cheese; well done bake

Regular Sauce Normal Cheese Normal Bake Normal Cut

Step 4 Add to order.

Quantity 1



#### **Ordering Pizza Combinatorially**



Simplified pizza ordering:

6x4x4x4x4x3x2x2x5x2 = 184,320 possibilities

2-way tests: 32

3-way tests: 150

4-way tests: 570

5-way tests: 2,413

6-way tests: 8,330

If all failures involve 5 or fewer parameters, then we can have confidence after running all 5-way tests.

So what? Who has time to check 2,413 test results?



# How to automate checking correctness of output

- Creating test data is the easy part!
- How do we check that the code worked correctly on the test input?
  - Crash testing server or other code to ensure it does not crash for any test input (like 'fuzz testing')
    - Easy but limited value
  - Embedded assertions incorporate assertions in code to check critical states at different points in the code, or print out important values during execution
  - Full scale model-checking using mathematical model of system and model checker to generate expected results for each input
    - expensive but tractable



#### **Crash Testing**

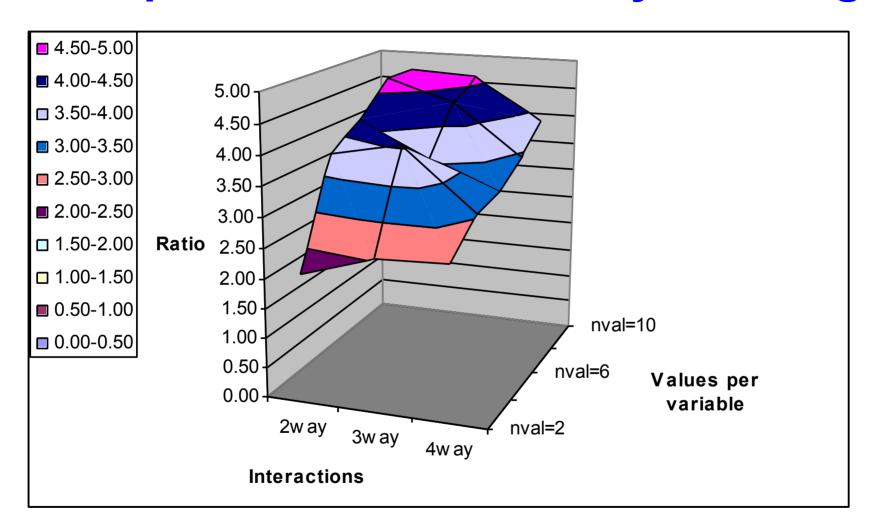
- Like "fuzz testing" send packets or other input to application, watch for crashes
- Unlike fuzz testing, input is non-random; cover all t-way combinations
- May be more efficient random input generation requires several times as many tests to cover the t-way combinations in a covering array

Limited utility, but can detect high-risk problems such as:

- buffer overflows
- server crashes



# Ratio of Random/Combinatorial Test Set Required to Provide t-way Coverage





#### **Embedded Assertions**

#### Simple example:

assert( x != 0); // ensure divisor is not zero

#### Or pre and post-conditions:

/requires amount >= 0;

/ensures balance == \old(balance) - amount && \result == balance;



#### **Embedded Assertions**

#### Assertions check properties of expected result:

```
ensures balance == \old(balance) - amount && \result == balance;
```

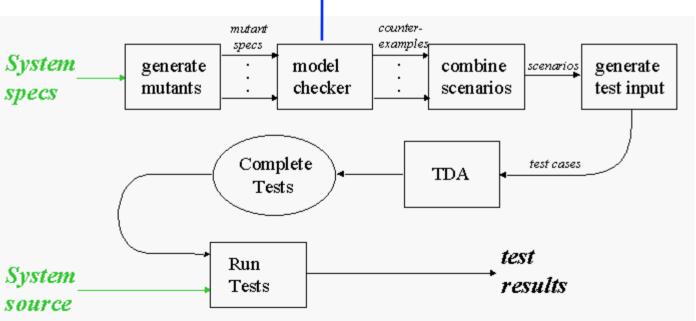
- •Reasonable assurance that code works correctly across the range of expected inputs
- May identify problems with handling unanticipated inputs
- Example: Smart card testing
  - Used Java Modeling Language (JML) assertions
  - Detected 80% to 90% of flaws





#### Using model checking to produce tests





- Model-checker test production: if assertion is not true, then a counterexample is generated.
- This can be converted to a test case.

Black & Ammann, 1999

#### Model checking example



```
-- specification for a portion of tcas - altitude separation.
-- The corresponding C code is originally from Siemens Corp. Research
-- Vadim Okun 02/2002
MODULE main
VAR
  Cur Vertical Sep : { 299, 300, 601 };
  High Confidence : boolean;
. . .
init(alt sep) := START ;
  next(alt sep) := case
    enabled & (intent not known | !tcas equipped) : case
      need upward RA & need downward RA : UNRESOLVED;
      need upward RA: UPWARD RA;
      need downward RA : DOWNWARD RA;
      1 : UNRESOLVED;
    esac;
    1 : UNRESOLVED;
  esac;
SPEC AG ((enabled & (intent not known | !tcas equipped) & !
need downward RA & need upward RA) -> AX (alt sep = UPWARD RA))
-- "FOR ALL executions,
-- IF enabled & (intent not known ....
-- THEN in the next state alt sep = UPWARD RA"
```

#### **Computation Tree Logic**



```
The usual logic operators, plus temporal:
    A \phi - All: \phi holds on all paths starting from the
  current state.
    E \phi - Exists: \phi holds on some paths starting from
  the current state.
    G \phi - Globally: \phi has to hold on the entire
  subsequent path.
    F \phi - Finally: \phi eventually has to hold
    X \phi - Next: \phi has to hold at the next state
      [others not listed]
     execution paths
            states on the execution paths
  SPEC AG ((enabled & (intent not known | !
  tcas equipped) & !need downward RA & need upward RA)
  -> AX (alt sep = UPWARD RA))
"FOR ALL executions,
  IF enabled & (intent not known ....
```

THEN in the next state alt sep = UPWARD RA"

# What is the most effective way to integrate combinatorial testing with model checking?

- For k-way variable combinations, v1 & v2 & . . . & vk
- vi abbreviates "var1 = val1"
- Now combine this constraint with assertion to produce counterexamples. Some possibilities:

```
1.AG(v1 & v2 & ... & vk & P -> AX ! (R))
2.AG(v1 & v2 & ... & vk -> AX ! (1))
3.AG(v1 & v2 & ... & vk -> AX ! (R))
```



#### What happens with these assertions?

1. AG (v1 & v2 & ... & vk & P  $\rightarrow$  AX ! (R))

P may have a negation of one of the v<sub>i</sub>, so we get

$$0 \rightarrow AX ! (R))$$

always true, so no counterexample, no test.

This is too restrictive!

1. AG (v1 & v2 & ... & vk  $\rightarrow$  AX ! (1))

The model checker makes non-deterministic choices for variables not in v1..vk, so all R values may not be covered by a counterexample.

This is too loose!

2. AG(v1 & v2 & ... & vk -> AX ! (R))
Forces production of a counterexample for each R.

This is just right!



#### **Tradeoffs**



#### Advantages

- Tests rare conditions
- Produces high code coverage
- Finds faults faster
- May be lower overall testing cost

#### Disadvantages

- Very expensive at higher strength interactions (>4way)
- May require high skill level in some cases (if formal models are being used)

#### **Tutorial Overview**



- 1. Why are we doing this?
- 2. What is combinatorial testing?
- 3. What is it good for?
- 4. How much does it cost?

#### 5. What tools are available?

6. What's next?

#### New algorithms to make it practical

- Tradeoffs to minimize calendar/staff time:
- FireEye (extended IPO) Lei roughly optimal, can be used for most cases under 40 or 50 parameters
  - Produces minimal number of tests at cost of run time
  - Currently integrating algebraic methods
- Adaptive distance-based strategies Bryce dispensing one test at a time w/ metrics to increase probability of finding flaws
  - Highly optimized covering array algorithm
  - Variety of distance metrics for selecting next test
- PRMI Kuhn –for more variables or larger domains
  - Parallel, randomized algorithm, generates tests w/ a few tunable parameters; computation can be distributed
  - Better results than other algorithms for larger problems



#### **New algorithms**



- Smaller test sets faster, with a more advanced user interface
- First parallelized covering array algorithm
- More information per test

T-Way	IPOG		ІТСН (ІВМ)		Jenny (Open Source)		TConfig (U. of Ottawa)		TVG (Open Source)	
	Size	Time	Size	Time	Size	Time	Size	Time	Size	Time
2	100	0.8	120	0.73	108	0.001	108	>1 hour	101	2.75
3	400	0.36	2388	1020	413	0.71	472	>12 hour	9158	3.07
4	1363	3.05	1484	5400	1536	3.54	1476	>21 hour	64696	127
5 (	4226	18s	NA	>1 day	4580	43.54	NA	>1 day	313056	1549
6	10941	65.03	NA	>1 day	11625	470	NA	>1 day	1070048	12600

Traffic Collision Avoidance System (TCAS): 2<sup>7</sup>3<sup>2</sup>4<sup>1</sup>10<sup>2</sup>

Times in seconds

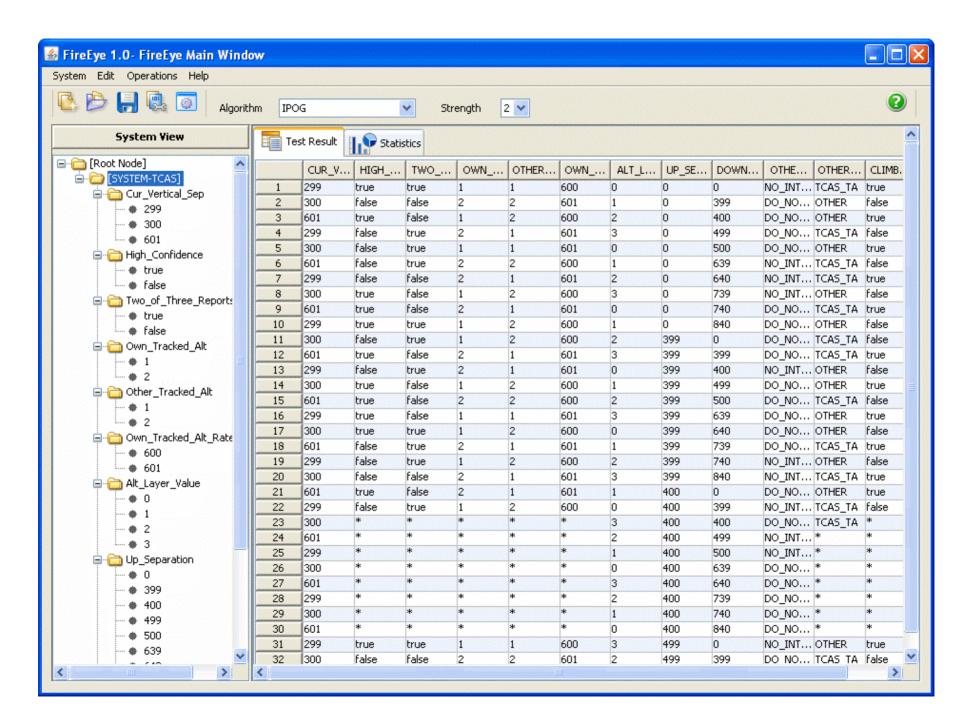
That's fast!

Unlike diet plans, results ARE typical!



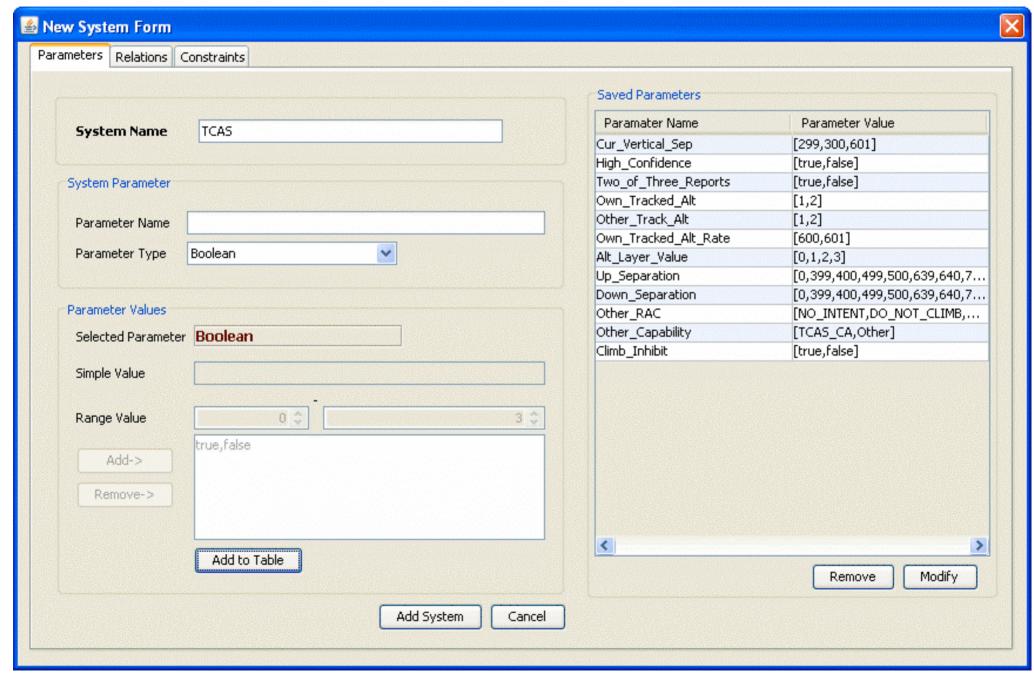
#### **ACTS Tool**





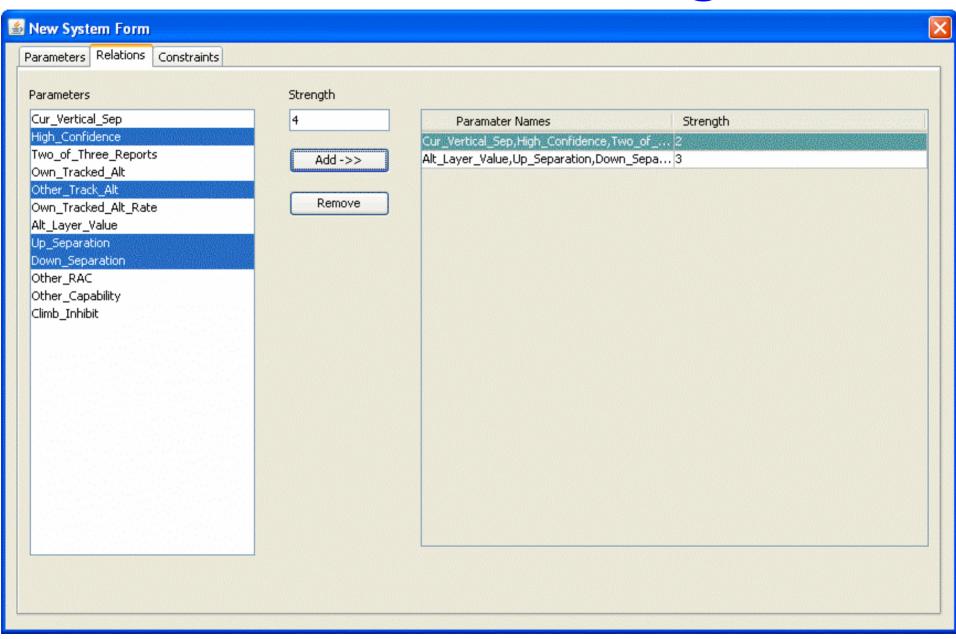


## Defining a new system



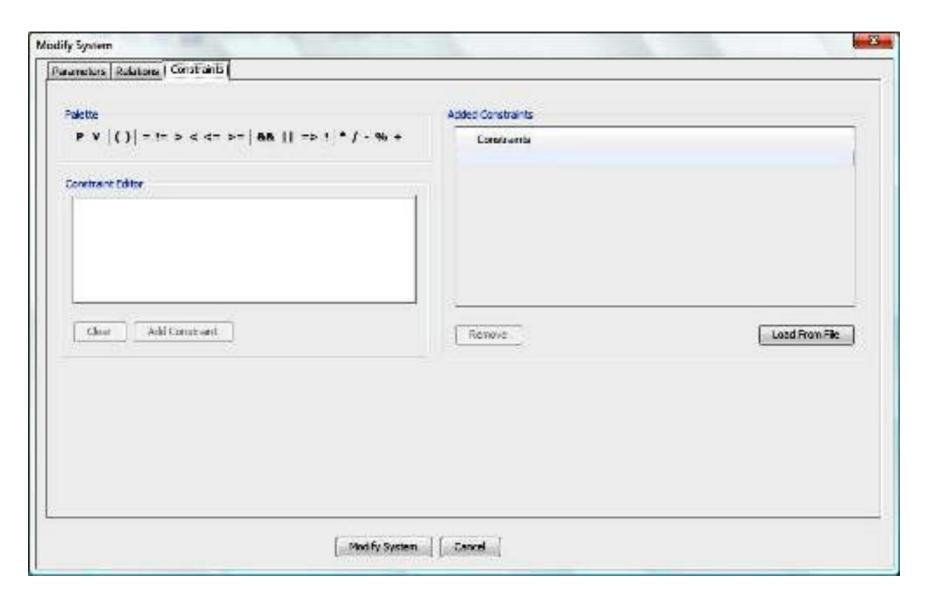


### Variable interaction strength



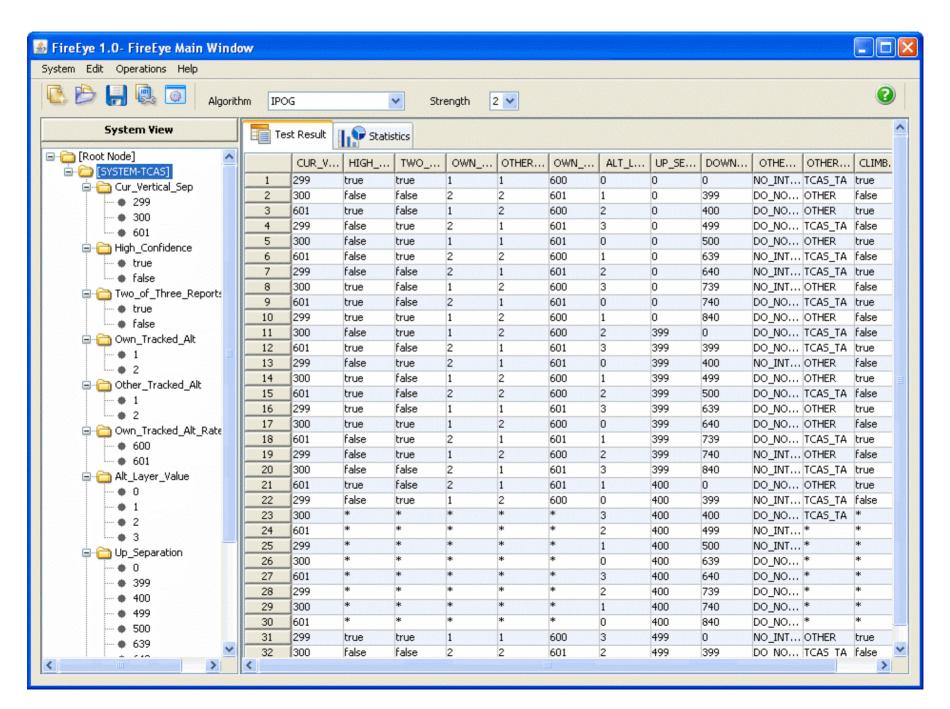


#### **Constraints**



## **Covering array output**





#### **Output**



- Variety of output formats:
  - XML
  - Numeric
  - CSV
  - Excel
- Separate tool to generate .NET configuration files from ACTS output
- Post-process output using Perl scripts, etc.

#### **Output options**



#### Mappable values

Degree of interaction

coverage: 2

Number of parameters: 12

Number of tests: 100

-----

#### **Human readable**

Degree of interaction coverage: 2

Number of parameters: 12

Maximum number of values per

parameter: 10

Number of configurations: 100

\_\_\_\_\_

#### Configuration #1:

```
1 = Cur Vertical Sep=299
```

2 = High Confidence=true

3 = Two of Three Reports=true

4 = Own Tracked Alt=1

5 = Other Tracked Alt=1

6 = Own Tracked Alt Rate=600

7 = Alt Layer Value=0

8 = Up Separation=0

9 = Down Separation=0

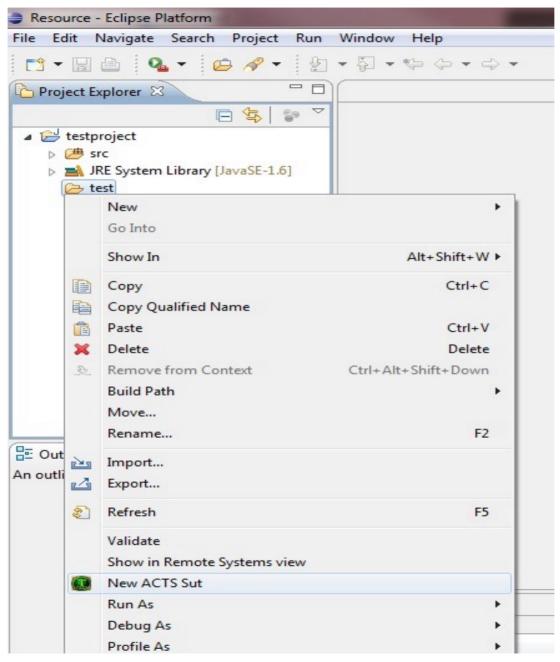
10 = Other RAC=NO INTENT

11 = Other Capability=TCAS CA

12 = Climb Inhibit=true



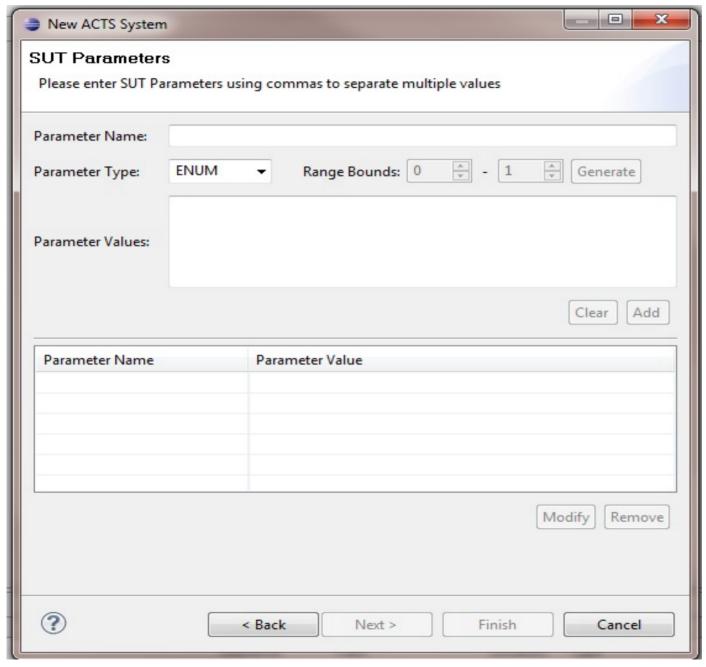
### **Eclipse Plugin for ACTS**



Work in progress



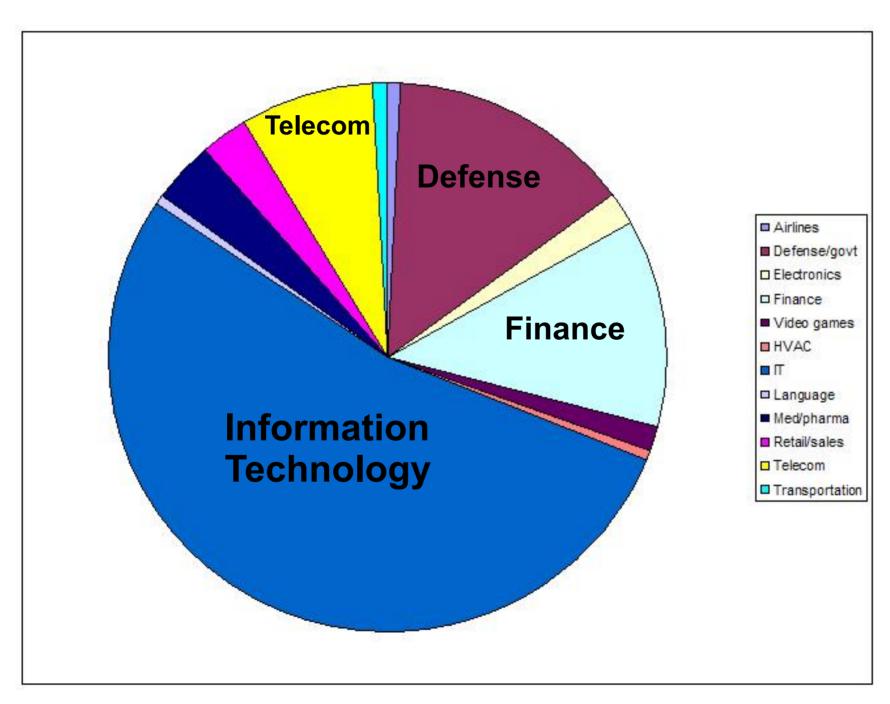
## **Eclipse Plugin for ACTS**



Defining parameters and values

#### **ACTS Users**





#### **Tutorial Overview**



- 1. Why are we doing this?
- 2. What is combinatorial testing?
- 3. How is it used and how long does it take?
- 4. What tools are available?

#### 5.What's next?

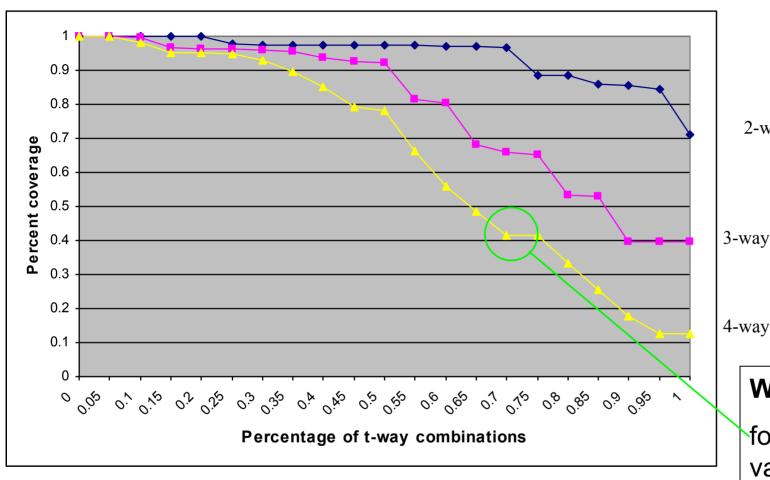
#### **Combinatorial Coverage Measurement**

Test s	Variables				
	а	b	С	d	
1	0	0	0	0	
2	0	1	1	0	
3	1	0	0	1	
4	0	1	1	1	
5	0	1	0	1	
6	1	0	1	1	
7	1	0	1	0	
8	0	1	0	0	

Variable pairs	Variable-value combinations covered	Coverage
ab	00, 01, 10	.75
ac	00, 01, 10	.75
ad	00, 01, 11	.75
bc	00, 11	.50
bd	00, 01, 10, 11	1.0
cd	00, 01, 10, 11	1.0



#### Combinatorial Coverage Measurement



Configuration coverage for 2<sup>79</sup>3<sup>1</sup>4<sup>1</sup>6<sup>1</sup>9<sup>1</sup> inputs.

- Measure coverage provided by existing test sets
- Compare across methodologies

#### What this means:

2-way

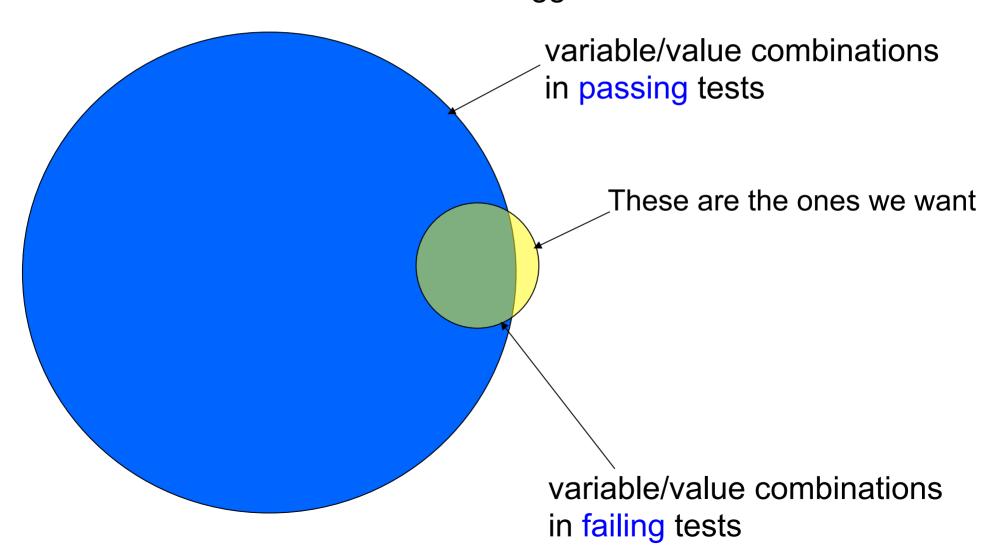
for 70% of 4-way variable combinations, tests cover at least 40% of variable-value configurations



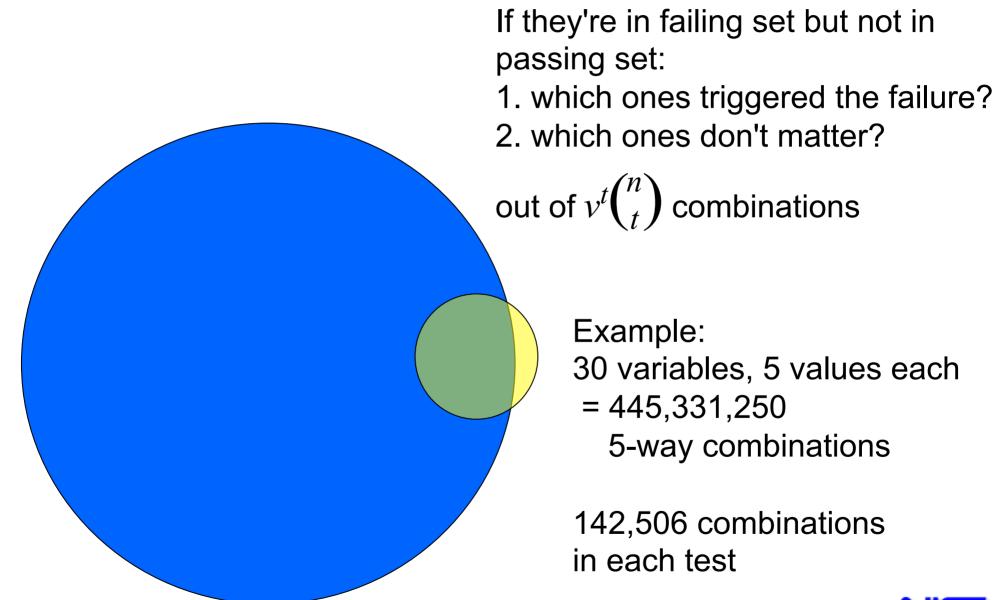
#### **Fault location**



Given: a set of tests that the SUT fails, which combinations of variables/values triggered the failure?



#### Fault location – what's the problem?





#### Conclusions



- Empirical research suggests that all software failures caused by interaction of few parameters
- Combinatorial testing can exercise all t-way combinations of parameter values in a very tiny fraction of the time needed for exhaustive testing
- New algorithms and faster processors make large-scale combinatorial testing possible
- Project could produce better quality testing at lower cost for US industry and government
- Beta release of tools available, to be open source
- New public catalog of covering arrays

#### **Future directions**



**Real-world examples** will help answer these questions What kinds of software does it work best on? What kinds of errors does it miss?

- Other applications:
  - Modelling and simulation
    - Testing the simulation
    - Finding interesting combinations: performance problems, denial of service attacks
- Maybe biotech applications. Others?

Please contact us if you are interested!

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http://csrc.nist.gov/acts

(Or just search "combinatorial testing". We're #1!)

