DAGS: KEY ENCAPSULATION USING DYADIC GS CODES

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Based on the hardness of decoding random linear codes (syndrome decoding problem).

Follows McEliece/Niederreiter framework.

Very efficient computation.

Natural implementation features thanks to binary vectors arithmetic.

Drawback: large keys (around 1 MByte).

WHY STRUCTURED CODES

Try to tackle the large key issue.

Idea: public matrix with compact description.

Quasi-Cyclic Codes (as seen before).

Quasi-Dyadic Codes (Misoczki, Barreto '09).



Several code families have QD description:

If dyadic signature and code support verify certain conditions...

...then Dyadic \cap Cauchy \cap Goppa.

Alternant codes with non-trivial intersection with Goppa codes.

Admit parity-check which is superposition of *s* blocks of size $t \times n$.

Each block H_{ℓ} has *ij*-th element $\frac{Z_j}{(v_j - u_{\ell})^i}$, (distinct) nonzero elements of \mathbb{F}_{q^m} .

If t = 1 this is a Goppa code.

Can generate QD-GS codes using (modified) algorithm for QD Goppa (P. '12).

Efficient decoder, similar performance, more flexibility.

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- SK: parity-check matrix H in alternant form over \mathbb{F}_{q^m} .
- PK: generator matrix G in systematic form over \mathbb{F}_q .

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- Choose random word $\boldsymbol{m} \in \mathbb{F}_{q}^{k'}$.
- Compute $(\rho \parallel \sigma) = \mathcal{G}(\boldsymbol{m})$ and $\boldsymbol{d} = \mathcal{H}(\boldsymbol{m})$.
- Generate error vector $\boldsymbol{e} \in \mathbb{F}_q^n$ of weight w from seed σ .
- Output $(\boldsymbol{c}, \boldsymbol{d})$ where $\boldsymbol{c} = (\rho \parallel \boldsymbol{m})G + \boldsymbol{e}$ and set $\boldsymbol{k} = \mathcal{K}(\boldsymbol{m})$.

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DECAPSULATION

- Recover codeword $((\rho' \parallel \mathbf{m}')$ and error $\mathbf{e}')$ from $Decode(\mathbf{c})$.
- Recompute $\mathcal{G}(\boldsymbol{m}')$, $\mathcal{H}(\boldsymbol{m}')$ and \boldsymbol{e}'' , then compare.
- Return \perp if decoding fails or any check fails, else return $\mathbf{k} = \mathcal{K}(\mathbf{m}')$.

ABOUT DAGS

Uses McEliece framework and IND-CCA KEM transform (Hofheinz, Hövelmanns, Kiltz '17).

Leverages "randomized" IND-CPA McEliece variant for tighter security proof.

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Alternant matrix is reconstructed on the fly together with syndrome computation.

This results in a small private key without computational overhead.

There exist structural attacks targeting structured alternant codes: FOPT and variants

(Faugère, Otmani, Perret, Tillich '10).

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No broken QD-GS parameters to date.

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- Small m
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Parameters (sizes in bytes):

q	т	n	k	k'	S	t	W	PK	SK	Ciphertext	Sec. Level
2 ⁵	2	832	416	26	2 ⁴	13	104	6,760	2,496	552	1
2 ⁶	2	1216	512	43	2 ⁵	11	176	8,448	3,648	944	3
2 ⁶	2	2112	704	43	2 ⁶	11	352	11,616	6,336	1,616	5

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Accurate complexity analysis of algebraic attacks is ongoing/future project.

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Some delicate points:

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 - Price to pay is actually fairly small

Thank you

www.dags-project.org

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