Optimized Software Implementations of CRYSTALS-Kyber, NTRU, and Saber Using NEON-Based Special Instructions of ARMv8

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Introduction

- NEON is an alternative name for Advanced Single Instruction Multiple Data (ASIMD) extension to the ARM Instruction Set Architecture, mandatory since ARMv7-A.
- NEON provides 32x128-bit vector registers.
 Compared with Single Instruction Single Data (SISD), ASIMD can have ideal speed-up in the range 2..16 (for 64..8-bit operands).



Apple M1: part of new MacBook Air, MacBook Pro, Mac Mini, iMac, and iPad Pro



Broadcom SoC, BCM2711: part of the Raspberry Pi 4 single-board computer

Introduction

- Most software implementations of PQC candidates on:
 - Intel/AMD (w/ AVX2 extension)
 - Cortex-M4 (w/ DSP extension)¹
- Lack of NEON implementations on ARMv7 and ARMv8 architectures



¹ M. J. Kannwischer, J. Rijneveld, P. Schwabe, and K. Stoffelen, pqm4 - Post-quantum crypto library for the ARM Cortex-M4, https://github.com/mupq/pqm4

Introduction

- Our goal is to fill the gap between low-power embedded processors and high-performance x86-64 platforms.
- We developed constant-time,
 optimized ARMv8 implementations
 of 3 KEM finalists:
 - CRYSTALS-Kyber
 - NTRU
 - Saber



Polynomial Multiplication



Optimal Choice of Algorithms



Based on the analysis of algorithms, their parameters, and AVX2 implementations for the 3 lattice-based KEMs finalists

5 Steps of Toom-4

 $A(x) = x^{\frac{3n}{4}} \sum_{i=\frac{3n}{4}}^{n-1} a_i x^{(i-\frac{3n}{4})} + \dots + x^{\frac{n}{4}} \sum_{i=\frac{n}{4}}^{\frac{2n}{4}-1} a_i x^{(i-\frac{n}{4})} + \sum_{i=0}^{\frac{n}{4}-1} a_i x^i$ 1. Splitting $= \alpha_3 \cdot x^{\frac{3n}{4}} + \alpha_2 \cdot x^{\frac{2n}{4}} + \alpha_1 \cdot x^{\frac{n}{4}} + \alpha_0$ 3. Pointwise 2. Evaluation multiplication $\begin{bmatrix} \mathcal{A}(0) \\ \mathcal{A}(1) \\ \mathcal{A}(-1) \\ \mathcal{A}(\frac{1}{2}) \\ \mathcal{A}(\frac{1}{2}) \\ \mathcal{A}(-\frac{1}{2}) \\ \mathcal{A}(2) \\ \mathcal{A}(\infty) \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ -1 & 1 & -1 & 1 \\ \frac{1}{8} & \frac{1}{4} & \frac{1}{2} & 1 \\ -\frac{1}{8} & \frac{1}{4} & -\frac{1}{2} & 1 \\ \frac{1}{8} & \frac{1}{4} & -\frac{1}{2} & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} \alpha_3 \\ \alpha_2 \\ \alpha_1 \\ \alpha_0 \end{bmatrix} \qquad \begin{bmatrix} \mathcal{C}(0) \\ \mathcal{C}(1) \\ \mathcal{C}(-1) \\ \mathcal{C}(\frac{1}{2}) \\ \mathcal{C}(-\frac{1}{2}) \\ \mathcal{C}(\infty) \end{bmatrix} = \begin{bmatrix} \mathcal{A}(0) \\ \mathcal{A}(1) \\ \mathcal{A}(-1) \\ \mathcal{A}(\frac{1}{2}) \\ \mathcal{A}(\frac{1}{2}) \\ \mathcal{A}(2) \\ \mathcal{A}(\infty) \end{bmatrix} \cdot \begin{bmatrix} \mathcal{B}(0) \\ \mathcal{B}(1) \\ \mathcal{B}(-1) \\ \mathcal{B}(\frac{1}{2}) \\ \mathcal{B}(2) \\ \mathcal{B}(\infty) \end{bmatrix}$

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5 Steps of Toom-4

4. Interpolation

$$\begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \theta_3 \\ \theta_4 \\ \theta_5 \\ \theta_6 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 & 1 & -1 & 1 \\ \frac{1}{64} & \frac{1}{32} & \frac{1}{16} & \frac{1}{8} & \frac{1}{4} & \frac{1}{2} & 1 \\ \frac{1}{64} & -\frac{1}{32} & \frac{1}{16} & -\frac{1}{8} & \frac{1}{4} & -\frac{1}{2} & 1 \\ \frac{1}{64} & 32 & 16 & 8 & 4 & 2 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \cdot \begin{bmatrix} \mathcal{C}(0) \\ \mathcal{C}(1) \\ \mathcal{C}(-1) \\ \mathcal{C}(\frac{1}{2}) \\ \mathcal{C}(-\frac{1}{2}) \\ \mathcal{C}(2) \\ \mathcal{C}(\infty) \end{bmatrix}$$
where $\mathcal{C}(\mathcal{X}) = \sum_{i=0}^{6} \theta_i \mathcal{X}^i$

5. Merging

$$C(x) = \sum_{i=0}^{2n-1} a_i x^i = \sum_{i=0}^{6} \theta_i x^{in/4}$$

Toom-Cook: Splitting & Evaluation



Toom-Cook Implementation: Saber



Schoolbook 16 x 16: Pointwise Multiplication

Toom-Cook Implementation: NTRU-HPS821



Schoolbook 16 x 16: Pointwise Multiplication

Toom-Cook Implementation: NTRU and Saber



For multiple layers of Split-Evaluate/Interpolate-Merge:

• unroll these layers to save load/store instructions

SIMD Batch Schoolbook Multiplication



- In order to perform a <u>batch multiplication</u>, a matrix of k polynomials with k coefficients has to be transposed before and after the multiplication
- Optimal value of k was determined to be 16

The 8x8 Matrix Transpose Operation



- The transpose operation enables performing the same operation on the same coefficients of 8 polynomials in parallel
- The 8 x 8 matrix transpose requires 27 out of 32 NEON 128-bit registers

The 16x16 Matrix Transpose Operation



- 16 x 16 matrix transpose requires memory
- To transpose 16 x 16 efficiently, transpose only 8 x 8 matrices and remember the location of each 8 x 8 block

Number Theoretic Transform

Complete NTT

$$C(x) = A(x) \times B(x)$$

= $\mathcal{NTT}^{-1}(\mathcal{C}) = \mathcal{NTT}^{-1}(\mathcal{A} * \mathcal{B}) = \mathcal{NTT}^{-1}(\mathcal{NTT}(A) * \mathcal{NTT}(B))$

where A(x), B(x), $C(x) \in \mathbb{Z}_q[x]/(x^n + 1)$ and $q \equiv 1 \mod 2n$

Number Theoretic Transform



Example of levels

Example of reordering indices between levels



NTT Implementation: CRYSTALS-Kyber and Saber



- Utilize Load and Interleave instructions for Level 0-1
- Use transpose instructions for Level 2-3
- Twist store registers in Level 4

NTT Implementation: CRYSTALS-Kyber and Saber



NTT Implementation: CRYSTALS-Kyber and Saber

- Apply to NTT/FFT based submissions
- 16-bit coefficients can reach level 6
- 32-bit coefficients can reach level 5.



NTT Implementation: Multiply and Modular Reduction

Algorithm 2: Vectorized multiplication modulo a 16-bit q



- NEON dependency chain: vuzp and vmull (vector unzip and vector multiply) Lack of an instruction similar to AVX2 vpmulhw:
- Multiply Packed Unsigned Word Integers and Store the high 16-bits of Result
- Compared to AVX2, our implementation uses additionally
 - 2 MUL and 3 UNZIP instructions

Benchmarking Methodology

Apple M1 System on Chip	Firestorm core, 3.2 GHz ¹ , MacBook Air
Broadcom BCM2711 System on Chip	Cortex-A72 core, 1.5 GHz, Raspberry Pi 4
Operating System	MacOS 11.4, Arch Linux (March 25, 2021)
Compiler	clang 12.0 (MacBook Air), clang 11.1 (Raspberry Pi 4)
Compiler Options	-O3 -mtune=native -fomit-frame-pointer
Cycles count on Cortex-A72	PAPI ²
Cycles count on Apple M1	Modified ³ from Dougall Johnson's work ⁴
Iterations	10,000,000 on Apple M1 to force CPU to run on high-performance "FireStorm" core; 1,000,000 otherwise

- ¹ <u>https://www.anandtech.com/show/16252/mac-mini-apple-m1-tested</u>
- ² D. Terpstra, H. Jagode, H. You, and J. Dongarra, "Collecting Performance Data with PAPI-C," in Tools for High Performance Computing, 2009
- ³ <u>https://github.com/GMUCERG/PQC_NEON/blob/main/neon/kyber/m1cycles.c</u>
- ⁴ <u>https://github.com/dougallj</u>

Toom-Cook vs. NTT for Saber

All values in cycles

Apple M1		Encaj	р	Decap					
3.2 Ghz	Toom	NTT	Toom/	NTT	Toom	NTT	Toom/	NTT	
lightsaber	37,187	$43,\!565$		85%	$35,\!318$	44,631		79%	
saber	59,838	$68,\!867$		87%	$57,\!955$	71,110		82%	
firesaber	87,899	$102,\!206$		86%	86,724	$106,\!553$		81%	

Cortex-A72		Encap)	Decap					
$1.5 \mathrm{Ghz}$	Toom	NTT	Toom/NTT	Toom	NTT	Toom/NTT			
lightsaber	131,318	130,097	101%	136,827	$131,\!187$	104%			
saber	210,383	213,574	99%	218,667	$215,\!364$	102%			
firesaber	307,360	$321,\!637$	96%	323,870	$329,\!566$	98%			

Dependencies degrade performance of NTT on high-performance processors. On Apple M1, Toom-Cook better by 13-21% On Cortex-A72 a tie. **We select Toom-Cook for the implementation of Saber.**

Ranking baseline C implementations

Bank		C Cortex-A72					Bank	C Apple M1					
Malik	E		↑	D	$kc \uparrow$		Hallk	\mathbf{E}	kc	↑	D	kc	↑
1	lightsaber	154.8	1.00	lightsaber	165.9	1.00	1	lightsaber	50.9	1.00	lightsaber	54.9	1.00
2	kyber512	184.5	1.19	kyber512	223.4	1.35	2	2 kyber512		1.49	kyber512	89.5	1.63
3	ntru-hrss701	458.7	2.96	ntru-hps677	1,346.7	8.12	3	ntru-hrss701	152.4	3.00	ntru-hps677	430.4	7.84
4	ntru-hps677	570.8	3.69	ntru-hrss701	$1,\!353.4$	8.16	4	ntru-hps677	183.1	3.60	ntru-hrss701	439.9	8.01
1	saber	273.4	1.00	saber	294.5	1.00	1	saber	90.4	1.00	saber	96.2	1.00
2	kyber768	298.9	1.09	kyber768	349.1	1.19	2	kyber768	119.8	1.32	kyber768	137.8	1.43
3	ntru-hps821	748.1	2.74	ntru-hps821	$1,\!830.0$	6.21	3	ntru-hps821	245.3	2.71	ntru-hps821	586.5	6.10
1	firesaber	427.3	1.00	firesaber	460.9	1.00	1	firesaber	140.9	1.00	firesaber	150.8	1.00
2	kyber1024	440.6	1.03	kyber1024	503.8	1.09	2	kyber1024	175.4	1.24	kyber1024	198.4	1.31

Encapsulation and Decapsulation ranking of baseline C implementations:

- 1. Saber
- 2. CRYSTALS-Kyber
- 3. NTRU (Levels 1 & 3 only)

Consistent between Cortex-A72 and Apple M1.

Ranking: NEON implementation

Rank	n	eon Cor	tex-A7	2			Dank	neon Apple M1					
	E	kc	\uparrow	D	kc	1	Kank	E	kc	↑	D	kc	\uparrow
1	ntru-hrss701	93.6	1.00	kyber512	94.1	1.00	1	ntru-hrss701	22.7	1.00	kyber512	29.4	1.00
2	kyber512	95.3	1.02	lightsaber	131.2	1.39	2	kyber512	32.5	1.43	lightsaber	35.3	1.20
3	lightsaber	130.1	1.39	ntru-hps677	205.8	2.19	3	lightsaber	37.2	1.63	ntru-hps677	54.5	1.85
4	ntru-hps677	181.7	1.94	ntru-hrss701	262.9	2.79	4	ntru-hps677	60.1	2.64	ntru-hrss701	60.7	2.06
1	kyber768	151.0	1.00	kyber768	149.8	1.00	1	kyber768	49.2	1.00	kyber768	45.7	1.00
2	saber	213.6	1.41	saber	215.4	1.44	2	saber	59.9	1.22	saber	58.0	1.27
3	ntru-hps821	232.6	1.54	ntru-hps821	274.5	1.83	3	ntru-hps821	75.7	1.54	ntru-hps821	69.0	1.51
1	kyber1024	223.8	1.00	kyber1024	220.7	1.00	1	kyber1024	71.6	1.00	kyber1024	67.1	1.00
2	firesaber	321.6	1.44	firesaber	329.6	1.49	2	firesaber	87.9	1.23	firesaber	86.7	1.29

Decapsulation ranking of NEON implementations at Levels 1, 3 and 5 Encapsulation ranking of NEON implementations at Level 3 and 5: 1. CRYSTALS-Kyber Exception: Encapsulat

- 2. Saber
- 3. NTRU (Levels 1 & 3 only)

Consistent between Cortex-A72 and Apple M1.

Exception: Encapsulation at Level 1

- 1. NTRU
- 2. CRYSTALS-Kyber
- 3. Saber

Ranking: C versus NEON

Dank		C Corte	x-A72				Bank	neon Cortex-A72					
панк	${f E}$	kc		D	kc	↑		${f E}$	kc	↑	D	kc	↑
1	lightsaber	154.8	1.00	lightsaber	165.9	1.00	1	ntru-hrss701	93.6	1.00	kyber512	94.1	1.00
2	kyber512	184.5	1.19	kyber512	223.4	1.35	2	kyber512	95.3	1.02	lightsaber	131.2	1.39
3	ntru-hrss701	458.7	2.96	ntru-hps677	$1,\!346.7$	8.12	3	lightsaber	130.1	1.39	ntru-hps677	205.8	2.19
4	ntru-hps677	570.8	3.69	ntru-hrss701	$1,\!353.4$	8.16	4	ntru-hps677	181.7	1.94	ntru-hrss701	262.9	2.79
1	saber	273.4	1.00	saber	294.5	1.00	1	kyber768	151.0	1.00	kyber768	149.8	1.00
2	kyber768	298.9	1.09	kyber768	349.1	1.19	2	saber	213.6	1.41	saber	215.4	1.44
3	ntru-hps821	748.1	2.74	ntru-hps821	$1,\!830.0$	6.21	3	ntru-hps821	232.6	1.54	ntru-hps821	274.5	1.83
1	firesaber	427.3	1.00	firesaber	460.9	1.00	1	kyber1024	223.8	1.00	kyber1024	220.7	1.00
2	kyber1024	440.6	1.03	kyber1024	503.8	1.09	2	firesaber	321.6	1.44	firesaber	329.6	1.49

Why do the rankings of Saber and CRYSTALS-Kyber switch places between the baseline C and NEON implementations?

<u>Answer:</u> Performance of polynomial multiplication in vector by vector and matrix by vector multiplications

Saber vs. Kyber



NEON vs. Baseline Speed-Up

Algorithm	ref	(kc)	neon	(kc)	ref/	neon
	\mathbf{E}	D	\mathbf{E}	D	\mathbf{E}	D
lightsaber	50.9	54.9	37.2	35.3	1.37	1.55
kyber512	75.7	89.5	32.6	29.4	2.33	3.04
ntru-hps 677	183.1	430.4	60.1	54.6	3.05	7.89
ntru-hrss701	152.4	439.9	22.8	60.8	6.68	7.24
saber	90.4	96.2	59.9	58.0	1.51	1.66
kyber768	119.8	137.8	49.2	45.7	2.43	3.02
ntru-hps 821	245.3	586.5	75.7	69.0	3.24	8.49
firesaber	140.9	150.8	87.9	86.7	1.60	1.74
kyber1024	175.4	198.4	71.6	67.1	2.45	2.96

Ranking: AVX2

Bank	avx2	avx2 AMD EPYC 7742									
Malik	\mathbf{E}	kc	↑	D	kc	\uparrow					
1	ntru-hrss701	20.4	1.00	kyber512	22.5	1.00					
2	ntru-hps677	25.9	1.27	lightsaber	42.1	1.87					
3	kyber512	28.3	1.39	ntru-hps677	45.7	2.03					
4	lightsaber	41.9	2.05	ntru-hrss701	47.6	2.11					
1	ntru-hps821	29.9	1.00	kyber768	35.2	1.00					
2	kyber768	43.4	1.45	saber	57.3	1.63					
3	saber	70.9	2.37	ntru-hps821	70.7	2.01					
1	kyber1024	63.0	1.00	kyber1024	53.1	1.00					
2	firesaber	103.3	1.64	firesaber	103.7	1.95					

For **D**ecapsulation, the rankings across all security levels are:

1. CRYSTALS-Kyber, 2.Saber, 3. NTRU (Levels 1 & 3 only)

For Encapsulation, at levels 1 and 3, the rankings are:

1. NTRU, 2. CRYSTALS-Kyber, 3. Saber

For Encapsulation, at level 5, the ranking is:

1. CRYSTALS-Kyber, 2. Saber

NEON vs. AVX2 in Cycles

Algorithm	neon (kc)		AVX2	$k \ (kc)$	AVX2/neon		
	\mathbf{E}	D	\mathbf{E}	D	\mathbf{E}	D	
lightsaber	37.2	35.3	41.9	42.2	1.13	1.19	
kyber512	32.6	29.4	28.4	22.6	0.87	0.77	
ntru-hps 677	60.1	54.6	26.0	45.7	0.43	0.84	
ntru-hrss701	22.8	60.8	20.4	47.7	0.90	0.78	
saber	59.9	58.0	70.9	70.7	1.18	1.22	
kyber768	49.2	45.7	43.4	35.2	0.88	0.77	
ntru-hps 821	75.7	69.0	29.9	57.3	0.39	0.83	
firesaber	87.9	86.7	103.3	103.7	1.18	1.20	
kyber1024	71.6	67.1	$\begin{bmatrix} -63.0 \end{bmatrix}$	53.1	$\boxed{0.88}$	-0.79	

Result for AVX2 AMD EPYC 7742 taken from **supercop-20210125**

Frequency Scaling Effect Apple M1 @ **3.2 GHz** versus Intel Core i7-8750H **4.1 GHz**

Apple M1	ref (kc)		neon	neon (kc)		AVX $2 (kc)$		'neon	AVX2/neon	
Core i7-8750H	\mathbf{E}	D	\mathbf{E}	D	\mathbf{E}	D	\mathbf{E}	D	\mathbf{E}	D
NTRU-HPS677	183.1	430.4	60.1	54.6	47.6	32.5	3.05	7.89	0.79	0.60
NTRU-HRSS701	152.4	439.9	22.8	60.8	28.8	33.9	6.68	7.24	1.26	0.56
LIGHTSABER	50.9	54.9	37.2	35.3	35.1	32.3	1.37	1.55	0.94	0.91
KYBER512	75.7	89.5	32.6	29.4	23.2	17.5	2.33	3.04	0.71	0.59
NTRU-HPS821	245.3	586.5	75.7	69.0	56.1	40.7	3.24	8.49	0.74	0.59
SABER	90.4	96.2	59.9	58.0	54.3	53.8	1.51	1.66	0.91	0.93
KYBER768	119.8	137.8	49.2	45.7	33.9	26.0	2.43	3.02	0.69	0.57
FIRESABER	140.9	150.8	87.9	86.7	78.9	78.1	1.60	1.74	0.90	0.90
KYBER1024	175.4	198.4	71.6	67.1	45.2	35.5	2.45	2.96	0.63	0.53

Frequency Scaling Effect Apple M1 @ **3.2 GHz** versus Intel Core i7-8750H **4.1 GHz**

Saber: AVX2 vs. NEON Level 1 Level 3 Level 5



Time measured with the ns accuracy using clock_gettime() on a MacBook Air and a PC laptop 32

Conclusions: Toom-Cook and NTT

- The polynomial multiplication performance affects the C baseline and NEON rankings in case of Saber and Kyber.
- Proposed optimal Toom-Cook strategy tailored for NTRU and Saber parameters.
- Missing instruction equivalent to AVX2 vpmulhw causes dependencies and worse performance

Conclusions

- First optimized implementation of CRYSTALS-Kyber, NTRU, and Saber targeting ARMv8.
- Largest speed-up for NTRU, followed by CRYSTALS-Kyber, and Saber
- The rankings of lattice-based PQC KEM finalists in terms of speed in software are similar for the NEON implementations and AVX2 implementations

Decapsulation: 1. CRYSTALS-Kyber, 2.Saber, 3. NTRU (L1 & 3 only) Encapsulation: 1. NTRU (L1 & 3 only), 2. CRYSTALS-Kyber, 3. Saber

Thanks for your attention!

Our source code is available at: https://github.com/GMUCERG/PQC_NEON