ACE: An Authenticated Encryption and Hash Algorithm

Submission to the NIST LWC Competition

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Chapter 1

Introduction

ACE, often known as one of the strongest cards in a deck of cards, is a 320-bit lightweight permutation. It is designed to achieve a balance between hardware cost and software efficiency for both Authenticated Encryption with Associated Data (henceforth "AEAD") and hashing functionalities, while providing sufficient security margins. To accomplish these goals, ACE components and its mode of operation are adopted from well known and analyzed cryptographic primitives. In a nutshell, the design of ACE, its security, functionalities and the features it offers are described as follows.

- **ACE core operations**. Bitwise XORs and ANDs, left cyclic shifts and 64-bit word shuffles

- **ACE nonlinear layer**. Unkeyed round-reduced Simeck block cipher [30] with block-size of 64-bits, which provides good cryptographic properties and low hardware cost

- **ACE linear layer**. Five 64-bit words are shuffled in an $(3, 2, 0, 4, 1)$ order, which offers good resistance against differential and linear cryptanalysis

- **ACE security**. Simple analysis and security bounds provided using automated tools such as CryptoSMT solver [25] and Gurobi [1]

- **Functionality**. All-in-one primitive, provides both AEAD and hashing functionalities using the same hardware circuit

- **ACE mode of operation**. Unified sponge duplex mode [5]

- **Security of ACE modes**. 128-bit security

- **Hardware performance**. Efficient in hardware. Achieves a throughput of 360 Mbps and has an area of 4250 GE in a 65 nm ASIC. Implementation results are presented for four ASIC libraries and two FPGAs along with parallel implementations.

- **Software performance**. Bit-sliced implementation of ACE permutation achieves a speed of 9.97 cycles/byte

1.1 Notations

Notation	Description
$X \odot Y, X \oplus Y, X \| Y$	bitwise AND, XOR and concatenation of X and Y
$\|X\|$	length of X in bits
$\{0,1\}^n, \{0,1\}^\star, \phi$	length n bitstring, variable length bitstring, empty string
$1^n, 0^n$	length n bitstring with all 1's, 0's
L^i	left cyclic shift operator, i.e., for $x \in \{0,1\}^n$, $\mathsf{L}^i(x) = (x_i, x_{i+1}, \ldots, x_{n-1}, x_0, x_1, \ldots, x_{i-1})$
word/block	a 64-bit binary string
S	320 bit state of ACE
S_r, S_c	r-bit rate part and c-bit capacity part of S ($r = 64, c = 256$)
A, B, C, D, E	five 64-bit words of S, i.e., $S = A\|B\|C\|D\|E$
S^i	state at i-th iteration (also step) of ACE permutation
$A[j]$	j-th byte of word A starting from right
A_1^i, A_0^i	right and left half of word A^i
K, N, T	key, nonce and tag
k, n, t	length of key, nonce and tag in bits ($k = n = t = 128$)
AD, M, C	associated data, plaintext and ciphertext (in blocks AD_i, M_i, C_i)
IV, iv	fixed initialization vector and its length in bits
H, h	message digest (in blocks H_i) and its length $h = 256$
ℓ_X	length of X in words where $X \in \{AD, M, C\}$
step	one round of ACE permutation (see Figure 2.1)
round	one round of Simeck unkeyed function (see Figure 2.2)
SB-64	nonlinear operation of ACE permutation
u	number of rounds, $u = 8$
s	number of steps, $s = 16$
rc_0^i, rc_1^i, rc_2^i	8-bit round constants
sc_0^i, sc_1^i, sc_2^i	8-bit step constants
ACE-$\mathcal{AE}$-k	ACE AEAD algorithm ($k = 128$)
ACE-$\mathcal{H}$-h	ACE Hash algorithm ($h = 256$)

1.2   Outline

The rest of the document is organized as follows. In Chapter 2, we present the complete specification of the ACE permutation, ACE AEAD and ACE hash algrithms. We summarize the security claims of our submission in Chapter 3 and provide the detailed security analyis in Chapter 4. In Chapter 5, we present the rationale behind our design and justify the parameter choices. The details of our hardware implementations and performance results in ASIC and FPGA are provided in Chapter 6. In Chapter 7, we discuss the efficiency of ACE in software including bit-sliced and microcontroller implementations. Finally, we conclude with references and test vectors in Appendix B.

Chapter 2

Specification

2.1 Parameters

ACE is a 320-bit permutation that operates in a unified duplex sponge mode [5] and offers both AEAD and hashing functionalities in a single hardware circuit. The AEAD algorithm (ACE-$\mathcal{AE}$-k) and the hash algorithm (ACE-$\mathcal{H}$-h) are parameterized by the size k of the secret key and the length of the message digest h in bits, respectively. Both the algorithms process the same amount of data per permutation call (i.e, rate r is same) and hence r value is ignored in the individual parameters' description.

2.1.1 ACE AEAD algorithm

The AEAD algorithm ACE-$\mathcal{AE}$-k is a combination of two algorithms, an authenticated encryption algorithm ACE-$\mathcal{E}$ and the verified decryption algorithm ACE-$\mathcal{D}$.

An authenticated encryption algorithm ACE-$\mathcal{E}$ takes as input a secret key K of length k bits, a public message number N (nonce) of size n bits, a block header AD (a.k.a, associated data) and a message M. The output of ACE-$\mathcal{E}$ is an authenticated ciphertext C of same length as M, and an authentication tag T of size t bits. Mathematically, ACE-$\mathcal{E}$ is defined as

$$\text{ACE-}\mathcal{E} : \{0,1\}^k \times \{0,1\}^n \times \{0,1\}^* \times \{0,1\}^* \to \{0,1\}^* \times \{0,1\}^t$$

with

$$\text{ACE-}\mathcal{E}(K, N, AD, M) = (C, T).$$

The decryption and verification algorithm takes as input the secret key K, nonce N, associated data AD, ciphertext C and tag T, and outputs the plaintext M of same length as C only if the verification of tag is correct, and $\perp$ (error symbol) if the tag verification fails. More formally,

$$\text{ACE-}\mathcal{D}(K, N, AD, C, T) \in \{M, \perp\}.$$

2.1.2   **ACE** Hash algorithm

A hash algorithm takes message M and a pre-defined initialization vector IV of length iv bits as inputs, and returns a fixed size output H, called hash or message digest. Formally, the hash algorithm using ACE permutation is specified by

$$\mathsf{ACE}\text{-}\mathcal{H}\text{-}h : \{0,1\}^* \times \{0,1\}^{iv} \to \{0,1\}^h$$

with $H = \mathsf{ACE}\text{-}\mathcal{H}\text{-}h(M, IV)$.

Note that IV and N refer to two different things. IV is for a hash function and is fixed, while N is for an AEAD algorithm and never repeated for a fixed key.

2.2   Recommended Parameter Set

In Table 2.1, we list the recommended parameter set for the AEAD and hash fuction-alities using the ACE permutation. The length of each parameter is given in bits and d denotes the amount of allowed data (including both AD and M) before a re-keying is required.

Table 2.1: Recommended parameter set for $\mathsf{ACE}\text{-}\mathcal{AE}\text{-}128$ and $\mathsf{ACE}\text{-}\mathcal{H}\text{-}256$

Functionality	Algorithm	r	k	n	t	$\log_2(d)$	h	iv
AEAD	ACE-$\mathcal{AE}$-128	64	128	128	128	124	-	-
Hash	ACE-$\mathcal{H}$-256	64	-	-	-	-	256	24

2.3   The **ACE** Permutation

ACE is an iterative permutation that takes a 320-bit state as an input and outputs a 320-bit state after iterating the step function ACE-step for $s = 16$ times (Figure 2.1). The nonlinear operation SB-64 is applied on even indexed words (i.e., A, C and E, see Figure 2.1) and hence the permutation name. We present the algorithmic description of ACE in Algorithm 1.

2.3.1   The nonlinear function SB-64

In ACE, we use unkeyed reduced-round Simeck block cipher [30] with block size 64 and $u = 8$ as the nonlinear operation, and denote it by SB-64. Below we provide the details of SB-64, henceforth referred to as Simeck sbox.

Figure 2.1: ACE-step

Definition 1 (SB-64: Simeck sbox [5]) *Let* $rc = (q_7, q_6, \ldots, q_0)$ *where* $q_j \in \{0, 1\}$ *and* $0 \leq j \leq 7$. *A Simeck sbox is a permutation of a 64-bit input, constructed by iterating the Simeck-64 block cipher for 8 rounds with round constant addition* $\gamma_j = 1^{31} || q_j$ *in place of key addition.*

Figure 2.2: Simeck sbox (SB-64)

An illustrated description of the Simeck sbox is shown in Figure 2.2 and is given by

$$(x_9 || x_8) \leftarrow \mathsf{SB\text{-}64}(x_1 || x_0, rc)$$

where

$$x_j \leftarrow f_{(5,0,1)}(x_{j-1}) \oplus x_{j-2} \oplus \gamma_{j-2}, \ 2 \leq j \leq 9$$

and $f_{(5,0,1)} : \{0, 1\}^{32} \rightarrow \{0, 1\}^{32}$ is defined as

$$f_{(5,0,1)}(x) = (\mathsf{L}^5(x) \odot x) \oplus \mathsf{L}^1(x).$$

2.3.2   Round and step constants

The step function of ACE is parameterized by two sets of triplets (rc_0^i, rc_1^i, rc_2^i) and (sc_0^i, sc_1^i, sc_2^i) where each rc_j^i and sc_j^i is of length 8 bits and $j = 0, 1, 2$. We call them

---

Algorithm 1 ACE permutation

1: Input: $S^0 = A^0||B^0||C^0||D^0||E^0$

2: Output: $S^{16} = A^{16}||B^{16}||C^{16}||D^{16}||E^{16}$

3: **for** $i = 0$ to 15 **do**:

4:        $S^{i+1} \leftarrow$ ACE-step(S^i)

5: **return** S^{16}

6: **Function** ACE-step(S^i):

7:        $A^i \leftarrow$ SB-64$(A^i_1||A^i_0, rc^i_0)$

8:        $C^i \leftarrow$ SB-64$(C^i_1||C^i_0, rc^i_1)$

9:        $E^i \leftarrow$ SB-64$(E^i_1||E^i_0, rc^i_2)$

10:       $B^i \leftarrow B^i \oplus C^i \oplus (1^{56}||sc^i_0)$

11:       $D^i \leftarrow D^i \oplus E^i \oplus (1^{56}||sc^i_1)$

12:       $E^i \leftarrow E^i \oplus A^i \oplus (1^{56}||sc^i_2)$

13:       $A^{i+1} \leftarrow D^i$

14:       $B^{i+1} \leftarrow C^i$

15:       $C^{i+1} \leftarrow A^i$

16:       $D^{i+1} \leftarrow E^i$

17:       $E^{i+1} \leftarrow B^i$

18:       **return** $(A^{i+1}||B^{i+1}||C^{i+1}||D^{i+1}||E^{i+1})$

19: **Function** SB-64$(x_1||x_0, rc)$:

20:       $rc = (q_7, q_6, \ldots, q_0)$

21:       **for** $j = 2$ to 9 **do**

22:       $x_j \leftarrow (\mathsf{L}^5(x_{j-1}) \odot x_{j-1}) \oplus \mathsf{L}^1(x_{j-1}) \oplus x_{j-2} \oplus (1^{31}||q_{j-2})$

23:       **return** $(x_9||x_8)$

---

round constants and step constants, respectively. As shown in Figure 2.1, the round constant triplet (rc^i_0, rc^i_1, rc^i_2) is used within the Simeck sboxes while the step constant (sc^i_0, sc^i_1, sc^i_2) is XORed to the words B, D and E.

In Table 2.2 we list the hexadecimal values of the constants and show the procedure to generate these constants in Section 5.6.2.

Table 2.2: Round and step constants of ACE

Step i	Round constants (rc^i_0, rc^i_1, rc^i_2)	Step constants (sc^i_0, sc^i_1, sc^i_2)
0 - 3	(07, 53, 43), (0a, 5d, e4), (9b, 49, 5e), (e0, 7f, cc)	(50, 28, 14), (5c, ae, 57), (91, 48, 24), (8d, c6, 63)
4 - 7	(d1, be, 32), (1a, 1d, 4e), (22, 28, 75), (f7, 6c, 25)	(53, a9, 54), (60, 30, 18), (68, 34, 9a), (e1, 70, 38)
8 - 11	(62, 82, fd), (96, 47, f9), (71, 6b, 76), (aa, 88, a0)	(f6, 7b, bd), (9d, ce, 67), (40, 20, 10), (4f, 27, 13)
12 - 15	(2b, dc, b0), (e9, 8b, 09), (cf, 59, 1e), (b7, c6, ad)	(be, 5f, 2f), (5b, ad, d6), (e9, 74, ba), (7f, 3f, 1f)

2.4 AEAD Algorithm: **ACE-$\mathcal{AE}$-128**

In Algorithm 2, we present a high-level overview of ACE-$\mathcal{AE}$-128. The encryption (ACE-$\mathcal{E}$) and decryption (ACE-$\mathcal{D}$) processes of ACE-$\mathcal{AE}$-128 are shown in Figure 2.3. In what follows, we first illustrate the position of rate and capacity bytes of the state, and the padding rule. We then describe each phase of ACE-$\mathcal{E}$ and ACE-$\mathcal{D}$.

Algorithm 2 ACE-$\mathcal{AE}$-128 algorithm

1: Authenticated encryption ACE-$\mathcal{E}(K, N, AD, M)$:
2:     $S \leftarrow \mathsf{Initialization}(N, K)$
3:     **if** $|AD| \neq 0$ **then:**
4:        $S \leftarrow \mathsf{Processing\text{-}Associated\text{-}Data}(S, AD)$
5:     $(S, C) \leftarrow \mathsf{Encyption}(S, M)$
6:     $T \leftarrow \mathsf{Finalization}(S, K)$
7:     **return** (C, T)

8: $\mathsf{Initialization}(N, K)$:
9:     $S \leftarrow \mathsf{load\text{-}\mathcal{AE}}(N, K)$
10:     $S \leftarrow \mathsf{ACE}(S)$
11:     **for** $i = 0$ to 1 **do:**
12:        $S \leftarrow (S_r \oplus K_i, S_c)$
13:        $S \leftarrow \mathsf{ACE}(S)$
14:     **return** S

15: $\mathsf{Processing\text{-}Associated\text{-}Data}(S, AD)$:
16:     $(AD_0 || \cdots || AD_{\ell_{AD}-1}) \leftarrow \mathsf{pad_r}(AD)$
17:     **for** $i = 0$ to $\ell_{AD} - 1$ **do:**
18:        $S \leftarrow (S_r \oplus AD_i, S_c \oplus 0^{c-2}||01)$
19:        $S \leftarrow \mathsf{ACE}(S)$
20:     **return** S

21: $\mathsf{Encryption}(S, M)$:
22:     $(M_0 || \cdots || M_{\ell_M-1}) \leftarrow \mathsf{pad_r}(M)$
23:     **for** $i = 0$ to $\ell_M - 1$ **do:**
24:        $C_i \leftarrow M_i \oplus S_r$
25:        $S \leftarrow (C_i, S_c \oplus 0^{c-2}||10)$
26:        $S \leftarrow \mathsf{ACE}(S)$
27:     $C_{\ell_M-1} \leftarrow \mathsf{trunc\text{-}msb}(C_{\ell_M-1}, |M| \bmod r)$
28:     $C \leftarrow (C_0, C_1, \ldots, C_{\ell_M-1})$
29:     **return** (S, C)

30: $\mathsf{pad_r}(X)$:
31:     $X \leftarrow X || 10^{r-1-(|X| \bmod r)}$
32:     **return** X

33: $\mathsf{trunc\text{-}lsb}(X, n)$:
34:     **return** $(x_{r-n}, x_{r-n+1}, \ldots, x_{r-1})$

1: Verified decryption ACE-$\mathcal{D}(K, N, AD, C, T)$:
2:     $S \leftarrow \mathsf{Initialization}(N, K)$
3:     **if** $|AD| \neq 0$ **then:**
4:        $S \leftarrow \mathsf{Processing\text{-}Associated\text{-}Data}(S, AD)$
5:     $(S, M) \leftarrow \mathsf{Decyption}(S, C)$
6:     $T' \leftarrow \mathsf{Finalization}(S, K)$
7:     **if** $T' \neq T$ **then:**
8:        **return** $\perp$
9:     **else:**
10:        **return** M

11: $\mathsf{Decryption}(S, C)$:
12:     $(C_0 || \cdots || C_{\ell_C-1}) \leftarrow \mathsf{pad_r}(C)$
13:     **for** $i = 0$ to $\ell_C - 2$ **do:**
14:        $M_i \leftarrow C_i \oplus S_r$
15:        $S \leftarrow (C_i, S_c \oplus 0^{c-2}||10)$
16:        $S \leftarrow \mathsf{ACE}(S)$
17:     $M_{\ell_C-1} \leftarrow S_r \oplus C_{\ell_C-1}$
18:     $C_{\ell_C-1} \leftarrow \mathsf{trunc\text{-}msb}(C_{\ell_C-1}, |C| \bmod r) || \mathsf{trunc\text{-}lsb}(M_{\ell_C-1}, r-|C| \bmod r)$
19:     $M_{\ell_C-1} \leftarrow \mathsf{trunc\text{-}msb}(M_{\ell_C-1}, |C| \bmod r)$
20:     $M \leftarrow (M_0, M_1, \ldots, M_{\ell_C-1})$
21:     $S \leftarrow \mathsf{ACE}(C_{\ell_C-1}, S_c \oplus 0^{c-2}||10)$
22:     **return** (S, M)

23: $\mathsf{Finalization}(S, K)$:
24:     **for** $i = 0$ to 1 **do:**
25:        $S \leftarrow \mathsf{ACE}(S_r \oplus K_i, S_c)$
26:     $T \leftarrow \mathsf{tagextract}(S)$
27:     **return** T

28: $\mathsf{trunc\text{-}msb}(X, n)$:
29:     **if** $n = 0$ **then:**
30:        **return** ϕ
31:     **else:**
32:        **return** $(x_0, x_1, \ldots, x_{n-1})$

(a) Authenticated encryption algorithm ACE-$\mathcal{E}$

(b) Verified decryption algorithm ACE-$\mathcal{D}$

Figure 2.3: Schematic diagram of ACE-$\mathcal{AE}$-128 AEAD algorithm

2.4.1 Rate and capacity part of state

The following 8 bytes constitute the S_r part of state and are used for both absorbing and squeezing.

$$A[7], A[6], A[5], A[4], C[7], C[6], C[5], C[4]$$

The rationale of these byte positions is explained in Section 5.8. The remaining bytes form the S_c part of state.

2.4.2 Padding

Padding is necessary when the length of the processed data is not a multiple of the rate r value. Since the key size is a multiple of r, we get two key blocks K_0 and K_1, so no padding is needed. Afterwards, the padding rule (10*), denoting a single 1 followed by the required number of 0's, is applied to the message M, so that its length after padding is a multiple of r. The resulting padded message is divided into ℓ_M r-bit blocks $M_0\|\cdots\|M_{\ell_M-1}$. A similar procedure is carried out on the associated data AD which results in ℓ_{AD} r-bit blocks $AD_0\|\cdots\|AD_{\ell_{AD}-1}$. In the case where no associated data is present, no processing is necessary. We summarize the padding rules for the message and associated data below.

$$
\begin{aligned}
\mathsf{pad_r}(M) \quad &\leftarrow M\|1\|0^{r-1-(|M| \bmod r)} \\
\mathsf{pad_r}(AD) \quad &\leftarrow \begin{cases} AD\|1\|0^{r-1-(|AD| \bmod r)} & \text{if } |AD| > 0 \\ \phi & \text{if } |AD| = 0 \end{cases}
\end{aligned}
$$

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Note that in case of AD or M whose length is a multiple of r, an additional r-bit padded block is appended to AD or M to distinguish between the processing of partial and complete blocks.

2.4.3 Loading key and nonce

The state is loaded byte-wise with 128-bit nonce $N = N_0||N_1$ and 128-bit key $K = K_0||K_1$, and the remaining eight bytes are set to zero. All nonce bytes are divided and loaded in the words B and E in a descending byte order. The key is loaded in words A and C in the same manner. The word D is initialized by the zero bytes. Symbolically, the state is initialized as follows.

$$A[7], A[6], \cdots, A[0] \leftarrow K_0[7], K_0[6], \cdots, K_0[0]$$
$$C[7], C[6], \cdots, C[0] \leftarrow K_1[7], K_1[6], \cdots, K_1[0]$$
$$B[7], B[6], \cdots, B[0] \leftarrow N_0[7], N_0[6], \cdots, N_0[0]$$
$$E[7], E[6], \cdots, E[0] \leftarrow N_1[7], N_1[6], \cdots, N_1[0]$$
$$D[7], D[6], \cdots, D[0] \leftarrow 0x00, 0x00, \cdots, 0x00$$

We use load-$\mathcal{AE}(N, K)$ to denote the process of loading the state with nonce N and key K bytes in the positions described above.

2.4.4 Initialization

The goal of this phase is to initialize the state S with public nonce N and secret key K. The state is first loaded using load-$\mathcal{AE}(N, K)$ as described above. Afterwards, the permutation ACE is applied to the state, and the two key blocks are absorbed into the state with ACE applied each time. The initialization steps are described below.

$$S \leftarrow \mathsf{ACE}(\mathsf{load\text{-}}\mathcal{AE}(N, K))$$
$$S \leftarrow \mathsf{ACE}(S_r \oplus K_0, S_c)$$
$$S \leftarrow \mathsf{ACE}(S_r \oplus K_1, S_c)$$

2.4.5 Processing associated data

If there is associated data, each AD_i block, $i = 0, \ldots, \ell_{AD} - 1$ is XORed with the S_r part of the internal state S, and one-bit domain separator is XORed to lsb of $E[0]$. Then, the ACE permutation is applied to the whole state.

$$S \leftarrow \mathsf{ACE}(S_r \oplus AD_i, S_c \oplus (0^{c-2}\|01)), \ i = 0, \ldots, \ell_{AD} - 1$$

This phase is defined in Algorithm 2.

2.4.6 Encryption

Similar to the processing of associated data, however, with a different domain separator, each message block M_i, $i = 0, \ldots, \ell_M - 1$ is XORed to the S_r part of the internal state

S resulting in the corresponding ciphertext C_i, which is extracted from the S_r part of the state. After the computation of each C_i, the whole internal state is permuted by applying ACE, i.e.,

$$C_i \;\; \leftarrow S_r \oplus M_i,$$
$$S \;\;\; \leftarrow \mathsf{ACE}(C_i, S_c \oplus (0^{c-2}\|10)), \; i = 0, \cdots, \ell_M - 1$$

The last ciphertext block $C_{\ell_M - 1}$ is truncated so that its length is equal to that of the last unpadded message block. The details of encryption procedure is given in Algorithm 2.

2.4.7 Finalization

After the extraction of the last ciphertext block and a single call of ACE, the domain separator is reset to $0x00$ indicating the start of the finalization phase. Afterwards, the two key blocks are absorbed into the state. Finally, the tag is extracted from the same byte positions that are used for loading the key. The finalization steps are mentioned below and illustrated in Algorithm 2.

$$S \;\; \leftarrow \mathsf{ACE}(S_r \oplus K_i, S_c), \;\; i = 0, 1$$
$$T \;\; \leftarrow \mathsf{tagextract}(S).$$

The function $\mathsf{tagextract}(S)$ extracts the 128-bit tag $T = T_0 || T_1$ from the state bytes as follows.

$$T_0[7], T_0[6], \cdots, T_0[0] \leftarrow A[7], A[6], \cdots, A[0]$$
$$T_1[7], T_1[6], \cdots, T_1[0] \leftarrow C[7], C[6], \cdots, C[0]$$

2.4.8 Decryption

The decryption procedure is symmetrical to the encryption procedure and illustrated in Algorithm 2.

2.5 Hash Algorithm: ACE-$\mathcal{H}$-256

The hash algorithm ACE-$\mathcal{H}$-256 takes message M and a pre-defined initialization vector IV of length 24 bits as inputs, and then returns 256-bit message digest H. The depiction of the ACE-$\mathcal{H}$-256 is shown in Figure 2.4 and illustrated in Algorithm 3. We now describe each phase of ACE-$\mathcal{H}$-256 in detail.

Figure 2.4: Hash algorithm ACE-$\mathcal{H}$-256

2.5.1 Message padding

The padding rule (10^*) similar to ACE-$\mathcal{AE}$-128 is applied to the input message M, where a single 1 followed by 0's is appended to it such that its length after padding is a multiple of r. We denote the padding rule by

$$\mathsf{pad_r}(M) = M\|10^{r-1-(|M| \bmod r)}$$

The resulting padded message is then divided into ℓ_M r-bit blocks $M_0\|\cdots\|M_{\ell_M-1}$.

2.5.2 Loading initialization vector

The state is first initialized by $IV = h/2\|r\|r'$, where r' denotes the number of bits squeezed per permutation call ($r = r' = 64$ for ACE-$\mathcal{H}$-256). Eight bits are used to encode each of the used $h/2$, r and r' sizes [21] and loaded in word B as follows.

$$B[7] \leftarrow 0x80$$
$$B[6] \leftarrow 0x40$$
$$B[5] \leftarrow 0x40$$

The remaining bytes are set to $0x00$. We denote this process by load-$\mathcal{H}(IV)$.

2.5.3 Initialization

The load-$\mathcal{H}(IV)$ procedure loads the state with the IV. Then a single call of ACE completes the initialization phase.

$$S \quad \leftarrow \mathsf{ACE}(\text{load-}\mathcal{H}(IV))$$

2.5.4 Absorbing and squeezing

Each message block is absorbed by XORing it to the S_r part of the state (see Section 2.4.1), then the ACE permutation is applied. After absorbing all the message blocks, the h-bit output is extracted from the S_r part of the state r bits at a time followed by the application of the ACE permutation until a total of 4 extractions are completed.

Algorithm 3 ACE-$\mathcal{H}$-256 algorithm

1: ACE-$\mathcal{H}$-256(M, IV):
2:      $S \leftarrow$ Initialization(IV)
3:      $S \leftarrow$ Absorbing(S, M)
4:      $H \leftarrow$ Squeezing(S)
5:      **return** H

6: Initialization(IV):
7:      $S \leftarrow$ load-$\mathcal{H}(IV)$
8:      $S \leftarrow$ ACE(S)
9:      **return** S

10: pad$_\mathsf{r}(M)$:
11:      $M \leftarrow M || 10^{r-1-(|M| \bmod r)}$
12:      **return** M

1: Absorbing(S,M):
2:      $(M_0 || \cdots || M_{\ell_M - 1}) \leftarrow$ pad$_\mathsf{r}(M)$
3:      **for** $i = 0$ to $\ell_M - 1$ **do:**
4:          $S \leftarrow$ ACE$(S_r \oplus M_i, S_c)$
5:      **return** S

6: Squeezing(S):
7:      **for** $i = 0$ to 2 **do:**
8:          $H_i \leftarrow S_r$
9:          $S \leftarrow$ ACE(S)
10:      $H_3 \leftarrow S_r$
11:      **return** $H_0 || H_1 || H_2 || H_3$

Chapter 3

Security Claims

ACE is an all-in-one primitive and provides both authenticated encryption with associated data and hashing functionalities. The AEAD mode assumes a nonce respecting adversary and we do not claim any security in the event of nonce reuse. If the verification procedure fails, the decrypted ciphertext and the new tag should not be given as output. Moreover, we claim no security for reduced-round versions of ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256. In summary, the security claims of ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256 are given in Tables 3.1 and 3.2, respectively.

Note that the integrity security in Table 3.1 includes the integrity of nonce, associated data and plaintext.

Table 3.1: Security goals of ACE-$\mathcal{AE}$-128 (in bits)

Confidentiality	Integrity	Authenticity	Data limit
128	128	128	2^{124}

Table 3.2: Security goals of ACE-$\mathcal{H}$-256 (in bits)

Collision	Preimage	Second preimage
128	192	128

Chapter 4

Security Analysis

In this chapter, we first analyze the security of the ACE permutation by assessing its indistinguishability properties against various distinguishing attacks. We primarily focus on the diffusion behavior, expected upper bounds on the probabilities of differential and linear characteristics, algebraic properties and self-symmetry based distinguishers. Next, we present the security bounds of ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256, whose results directly follow the security proofs of sponge modes.

In our analysis, we denote the linear layer by π, i.e., π permutates the words of state. For example, if $\pi(0, 1, 2, 3, 4) = (3, 2, 0, 4, 1)$,then after applying π, the state $A||B||C||D||E$ is transformed to $D||C||A||E||B$. Moreover, by the component function f_j we refer to the Algebraic Normal Form (ANF) of the j-th bit.

4.1 Diffusion

To assess the diffusion behavior, we evaluate the minimum value of $u \times s$ such that each component function of the state after s steps depends on all the input state bits. We find that $u = 11$ gives full bit diffusion within a single Simeck sbox. Since ACE has five words that are updated in each step, we note that s has to be at least 5. Accordingly, we search for the following values of $(u, s) \in \{(i, 5)|1 \leq i \leq 11\}$. Note that for $u = 8$ and $s = 5$, the number of linear layers satisfying the full bit diffusion property are 13, and $\pi = (3, 2, 0, 4, 1)$ is one among them.

Given that $(u, s) = (8, 16)$ and $\pi = (3, 2, 0, 4, 1)$ for ACE, we claim that meet/miss-in-the-middle distinguishers cannot cover more than ten steps, because ten steps guarantees full bit diffusion in both forward and backward directions.

4.2 Differential and Linear Cryptanalysis

To analyze the security of ACE w.r.t differential and linear distinguishers [17, 28], we model ACE using Mixed Integer Linear Programming (MILP) and bound the minimum number of active Simeck sboxes (SB-64). We then provide expected bounds for the

maximum probabilities of differential (resp. linear) characteristics. Table 4.1 depicts the minimum number of active Simeck sboxes for all linear layers.

4.2.1 Expected bounds on the maximum probabilities of differential and linear characteristics

Let $n_s(\pi)$ be the minimum number of active Simeck sboxes in s steps for a linear layer π, and p denote the Maximum Differential Probability bound (MDP) for a u-round Simeck sbox in $\log_2(\cdot)$ scale. An in-depth analysis of values of p has been provided in [6] (cf. Section 4.2). We choose u, s and π such that

- the upper bound on the maximum differential characteristic probability is less than 2^{-320}, i.e., $|n_s(\pi)p| > 320$.

- $u \times s$ is minimum and s is at least three times the number of steps required for full bit diffusion. This implies $s \geq 15$ for ACE.

For $(u, s) = (8, 16)$ and $\pi = (3, 2, 0, 4, 1)$, $n_s(\pi) = 21$ and $p = -15.8$. Thus, $|21 \times (-15.8)| \approx 331.8 > 320$ and maximum differential characteristic probability bound is $2^{-331.8}$. The maximum squared correlation of a linear characteristic is computed analogously using $\gamma = -15.6$ and equals $2^{-327.6}$, where γ is the maximum square correlation of a 8-round Simeck sbox (cf. Section 4.2.2 [6]).

4.3 Algebraic Properties

In this section, we provide bounds for the algebraic degree of ACE and evaluate its security against integral distinguishers. We use the bit based division property [29, 9] to compute the algebraic degree. We find that the algebraic degree of a 8-round Simeck sbox is 36. Note that the algebraic degree (after 8 rounds) of all component functions from $f_0 - f_{31}$ is 36 while it is 27 for the component functions $f_{32} - f_{63}$. Thus, to evaluate the algebraic degree of ACE it is enough to find bounds for algebraic degree of the component functions $f_0, f_{32}, f_{64}, f_{96}, f_{128}, f_{160}, f_{192}, f_{224}, f_{256}$ and f_{288}. Table 4.2 provides bounds of the algebraic degree for the above component functions.

Note that since the number of words in ACE is odd, due to slow diffusion the algebraic degrees are 63 and 62 for the component functions f_{64} and f_{96} after 2 steps, respectively. A similar trend can be seen for the component functions f_{256} and f_{288}. This non-uniformity in degree continues till step five, after which the degree is stabilized to 304-313 due to full bit diffusion (Section 4.1). We expect that the degree reaches 319 in six steps.

Integral distinguishers [24]. To search for the longest length integral distinguisher, we set a single bit of the input state as constant (0) and the rest are set to active (1). We then evaluate the algebraic degree at the s-th step of each component function in terms

Table 4.1: Minimum number of active Simeck sboxes for s-step ACE

Linear layer	step s															
π	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
(1, 0, 3, 4, 2)	0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8
(1, 0, 4, 2, 3)	0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8
(1, 2, 0, 4, 3)	0	1	2	3	4	6	8	8	9	10	11	12	14	16	16	17
(1, 2, 3, 4, 0)	0	1	2	3	4	6	7	8	9	10	11	12	13	14	15	16
(1, 2, 4, 0, 3)	0	1	1	2	3	5	7	8	9	9	10	11	13	15	16	17
(1, 3, 0, 4, 2)	0	0	1	2	4	4	5	7	9	12	13	14	15	16	17	19
(1, 3, 4, 0, 2)	0	0	1	1	1	2	2	2	3	3	3	4	4	4	5	5
(1, 3, 4, 2, 0)	0	0	1	2	3	4	5	6	7	9	11	12	12	13	14	15
(1, 4, 0, 2, 3)	0	1	2	3	4	6	8	8	9	10	11	12	14	16	16	17
(1, 4, 3, 0, 2)	0	1	1	2	4	5	6	7	9	10	11	12	14	15	16	18
(1, 4, 3, 2, 0)	0	1	2	3	5	6	7	9	11	12	13	14	15	17	18	19
(2, 0, 1, 4, 3)	0	1	2	3	4	6	6	8	9	10	11	12	14	15	16	17
(2, 0, 3, 4, 1)	0	1	2	3	4	5	7	8	9	10	11	12	13	14	15	16
(2, 0, 4, 1, 3)	0	0	1	2	3	3	4	5	7	9	10	11	12	12	13	14
(2, 3, 0, 4, 1)	0	0	1	2	3	5	7	9	10	10	11	12	13	15	17	19
(2, 3, 1, 4, 0)	0	0	1	3	4	6	7	8	8	9	11	12	13	14	15	16
(2, 3, 4, 0, 1)	0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
(2, 3, 4, 1, 0)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
(2, 4, 0, 1, 3)	0	0	1	3	4	5	7	9	10	10	11	13	14	15	17	19
(2, 4, 1, 0, 3)	0	1	2	3	4	5	7	8	9	10	11	12	13	15	16	17
(2, 4, 3, 0, 1)	0	1	2	3	5	5	6	7	8	10	10	11	12	13	15	15
(2, 4, 3, 1, 0)	0	0	1	2	4	6	7	8	9	10	11	12	13	14	15	16
(3, 0, 1, 4, 2)	0	1	1	2	4	6	8	8	10	10	11	13	15	16	17	19
(3, 0, 4, 1, 2)	0	0	1	1	1	2	2	2	3	3	3	4	4	4	5	5
(3, 0, 4, 2, 1)	0	1	1	2	3	4	5	6	7	8	9	10	11	12	13	14
(3, 2, 0, 4, 1)	0	1	2	3	5	7	8	9	11	12	13	15	16	17	**19**	**21**
(3, 2, 1, 4, 0)	0	1	2	2	3	4	4	5	6	6	7	8	8	9	10	10
(3, 2, 4, 0, 1)	0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8
(3, 2, 4, 1, 0)	0	0	1	2	3	6	8	9	9	10	11	12	15	16	18	18
(3, 4, 0, 1, 2)	0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
(3, 4, 0, 2, 1)	0	1	2	3	4	4	5	6	7	8	8	9	10	11	12	12
(3, 4, 1, 0, 2)	0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8
(3, 4, 1, 2, 0)	0	1	2	3	5	7	8	9	11	12	13	15	16	17	19	21
(4, 0, 1, 2, 3)	0	1	2	3	4	5	7	8	10	12	13	13	14	15	17	19
(4, 0, 3, 1, 2)	0	0	1	2	3	3	4	5	7	9	10	11	12	12	13	14
(4, 0, 3, 2, 1)	0	1	2	3	4	5	6	8	10	11	12	13	14	15	16	17
(4, 2, 0, 1, 3)	0	0	1	2	4	6	7	9	10	11	12	13	14	15	17	19
(4, 2, 1, 0, 3)	0	1	2	2	3	4	4	5	6	6	7	8	8	9	10	10
(4, 2, 3, 0, 1)	0	1	2	3	5	6	8	9	10	11	12	14	16	17	18	19
(4, 2, 3, 1, 0)	0	0	1	1	2	3	4	4	4	5	5	6	7	8	8	8
(4, 3, 0, 1, 2)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
(4, 3, 0, 2, 1)	0	0	1	2	3	5	6	7	10	10	11	12	13	15	16	17
(4, 3, 1, 0, 2)	0	0	1	2	4	5	6	7	9	10	11	12	13	14	15	17
(4, 3, 1, 2, 0)	0	0	1	1	2	3	4	4	4	5	5	6	7	8	8	8

Table 4.2: Bounds on the algebraic degree of ACE

steps (s)	Component function									
	f_0	f_{32}	f_{64}	f_{96}	f_{128}	f_{160}	f_{192}	f_{224}	f_{256}	f_{288}
1	36	27	36	27	36	27	36	27	36	27
2	92	83	63	62	92	83	92	83	63	62
3	126	125	119	117-120	239-247	235-245	236-249	233-248	119	118-120
4	240-247	238-246	241-248	242-247	306-312	303-311	304-313	304-311	241-248	241-247

of the involved active bits. If the algebraic degree equals the number of active bits, then the bit is unknown (i.e., XOR sum of the component function is unpredictable). Otherwise, it is balanced in which case the XOR sum is always zero.

In Table 4.3, we list the integral distinguishers of ACE. Note that the positions of constant bits are chosen based on the degree of the Simeck sbox.

Table 4.3: Integral distinguishers of ACE

Steps s	Input division property	Balanced bits
8	$1^{32}||0||1^{287}$	64-127, 256-319
	$1^{96}||0||1^{223}$	None
	$1^{160}||0||1^{159}$	None
	$1^{224}||0||1^{95}$	64-127, 256-319
	$1^{288}||0||1^{31}$	None

4.4 Self Symmetry-based Distinguishers

A cryptographic permutation is vulnerable to attacks such as rotational distinguishers, slide distinguishers [18] and invariant subspace attack [26] which exploit the symmetric properties of a round function. For example, in ACE the nonlinear Simeck sbox is rotational invariant if constants are not added at each round. Thus, a proper choice of round constants is required to mitigate the above attacks.

ACE employs an 7-bit LFSR to generate round and step constants (see Section 5.6.2). Below we list properties of the constants which ensure that each step function of ACE is distinct.

- For $0 \leq i \leq 15$, $sc_0^i \neq sc_1^i \neq sc_2^i$

- For $0 \leq i \leq 15$, $(rc_0^i, rc_1^i, rc_2^i) \neq (sc_0^i, sc_1^i, sc_2^i)$

- For $0 \leq i, j \leq 15$ and $i \neq j$, $(rc_0^i, rc_1^i, rc_2^i) \neq (rc_0^j, rc_1^j, rc_2^j)$

- For $0 \leq i, j \leq 15$ and $i \neq j$, $(sc_0^i, sc_1^i, sc_2^i) \neq (sc_0^j, sc_1^j, sc_2^j)$.

4.5 Security of **ACE-$\mathcal{AE}$-128** and **ACE-$\mathcal{H}$-256**

The security proofs of modes based on the sponge construction rely on the indistinguishability of the underlying permutation from a random one [11, 15, 14, 22]. In previous sections, we have shown that there are no distinguishers for 16 steps of ACE. Thus, the security bounds of sponge modes are applicable to both ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256.

ACE-$\mathcal{AE}$-128 security. We assume a nonce-respecting adversary, i.e, for a fixed K, the nonce N is never repeated. Then considering a data limit of 2^d, k-bit security is achieved if $c \geq k + d + 1$ and $d \ll c/2$ [14]. The parameter set of ACE-$\mathcal{AE}$-128 (Table 2.1 in Section 2.2) with actual effective capacity 254 (2 bits are lost for domain separation) satisfies this condition, and hence ACE-$\mathcal{AE}$-128 provides 128-bit security for confidentiality, integrity and authenticity.

Note that we could use $r = 192$, $d = 64$ and obtain the same level of security [22]. However, this would require an additional 128 XORs and cannot meet our objective to achieve both AEAD and hash functionalities using the same hardware circuit. Nevertheless, this is another option for ACE with high throughput.

ACE-$\mathcal{H}$-256 security. For a sponge based hash with $b = r + c$ and h-bit message digest, the generic security bounds [13, 21] are given by:

- **Collision:** $\min(2^{h/2}, 2^{c/2})$
- **Preimage:** $\min(2^{\min(h,b)}, \max(2^{\min(h,b)-r}, 2^{c/2}))$
- **Second-preimage:** $\min(2^h, 2^{c/2})$

Accordingly, ACE-$\mathcal{H}$-256 provides 128, 192 and 128-bit securities for collision, preimage and second preimage, respectively.

Chapter 5

Design Rationale

In this chapter, we provide the rationale for our design choices and justify the design principles of each component of ACE, ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256.

5.1   Choice of the Mode: sLiSCP Sponge Mode

Our adopted mode is a variation of the sponge duplex construction. Sponge constructions are very diversified in terms of the offered security level. Particularly, it is proven that the sponge and its single pass duplex mode offer a $2^{c/2}$ bound against generic attacks [12, 15] which provides a lower bound on the width of the underlying permutation. However, for authenticated encryption (AE), a security level of 2^{c-d} is proven when the number of queries is upper bounded by 2^d [16]. When restricting the data complexity to the maximum of 2^d queries with $d \ll c/2$, one can reduce the capacity and increase the rate for a better throughput with the same security level. Jovanovic *et.al.* [22] have shown that sponge based AE achieve higher security bound, i.e., $\min\{2^{b/2}, 2^c, 2^k\}$ compared to [14]. However, we are concerned with the former bound, as shown in Section 4.5.

In sponge keyed encryption modes, nonce reuse enables the encryption of two different messages with the same key stream, which undermines the privacy of the primitive. More precisely, the sponge duplex authenticated encryption mode requires the uniqueness of a nonce when encrypting different messages with the same key because the ability of the attacker to acquire multiple combinations of input and output differences leaks information about the inner state bits, which may lead to the reconstruction of the full state [15, 10]. Nonce reuse in the duplex constructions reveals the XOR difference between the first two plaintexts by XORing their corresponding ciphertexts. On the other hand, a nonce reuse differential attack may be exploited if the attacker is able to inject a difference in the plaintext and cancel it out by another difference after the permutation application. However, such an attack depends on the probability of the best differential characteristic and the number of rounds of the underlying permutation. Accordingly, if such a permutation offers enough resistance to differential cryptanaly-

sis, the feasibility of nonce reuse differential attacks is minimal. The condition on the differential behavior of the underlying permutation is also important when considering resynchronization attacks, where related nonces are to be used. For that reason, even if nonce reuse is not permitted, the underlying permutation used in the initialization stage should be strong enough to mitigate differential attacks.

Given the above results, the sLiSCP sponge mode [5] realizes the following objectives:

- The flexibility to adapt the same circuitry to provide both authenticated encryption and hashing functionalities, as we adopt a unified round function for all functionalities.

- High key agility, which fits the lightweight requirements, because AE mode require no key scheduling.

- Simplicity, as there is no need to implement a decryption algorithm, because the same encryption algorithm is used for decryption.

- Both plaintext and ciphertext blocks are generated online without the need to process the whole input message and encrypted material first.

- Keyed initialization and finalization phases that make key recovery hard even if the internal state is recovered and also renders universal forgery with the knowledge of the internal state unattainable.

- Hardware efficient initialization and finalization stages where the state is initialized with the key which is again absorbed in the rate part afterward.

- Domain separators run for all rounds of all stages and offer uniformity across different stages. We change the domain separators with each new transition and not before because we found that it leads to a more efficient hardware implementations. Such mechanism has been shown to be secure in [22].

5.2   ACE State Size

Our main objective is to choose b (state size) that provides 128-bit security for both hash and AEAD, i.e., 256-bit hash output and 128-bit key and tag. For b-bit state with $b = r + c$, r-bit rate and c-bit hash output, generic attacks with $2^{c/2}$ permutation queries exist [12]. Thus, to satisfy the security requirements of hash, c should be 256 which implies $b \geq 257$. The immediate choices are $b = 288, 320$ and 384. In ACE, we choose $b = 320$ as it provides the best trade-off among hardware and software requirements, security and efficiency. With this choice of b, ACE can have implementations in a wide range of platforms. We discard the other state sizes for the following reasons.

- Considering the lightweight applications, 384-bit state is too heavy in hardware.

- 288 is not a multiple of 64, hence, we can not efficiently use inbuilt 64-bit CPU instructions for software implementation.

5.3 ACE Step Function

The step function of the ACE permutation can be seen as a generalized five 64-bit word sLiSCP-light [6] structure. Since we aim to build a 320-bit permutation, we could have used a 4-word sLiSCP-light with 80-bit Simeck sboxes. However, we found that it is not practical to evaluate most of the cryptographic properties for the resulting permutation using Simeck sboxes with sizes > 64, and that our 80-bit based software implementation is not efficient. Consequently, we decided to use a 5-word sLiSCP-light with 3 Simeck sboxes and wrap around the linear mixing between words A and E. We also decided to XOR SB-64(A) with SB-64(E) and not E to avoid the need for an extra temporary 64-bit register to store the initial value of E while intermediate results of the iterated SB-64 function are stored in E.

5.4 Nonlinear Layer: Simeck sbox (SB-64)

The Simeck sbox is an unkeyed independently parameterized variant of the round function of the Simon round function [8]. Moreover, it has set a new record in terms of hardware efficiency and performance on almost all platforms [30]. In what follows, we list the reasons that motivated our adoption of Simeck sboxes as the nonlinear function of ACE permutation.

- Simeck has a hardware friendly round function that consists of simple bitwise XOR, AND and cyclic shift operations. Moreover, the hardware cost grows linearly with input size.

- It is practical to evaluate the SB-64 maximum (expected) differential probability and maximum (expected) linear squared correlation which are $2^{-15.8}$ and $2^{-15.6}$, respectively. Accordingly, we can provide an expected bounds against differential and linear cryptanalysis.

- SB-64 has an algebraic degree of 36 and the output component functions $f_0 - f_{31}$ (resp. $f_{32} - f_{63}$) depend on 61 (resp. 55) input state bits, which enables us to provides guarantees gainst algebraic and diffusion-based attacks.

- Each Simeck sbox is independently parameterized by the associated set of round constants, which suggests that the actual security against differential and linear cryptanalysis is better than the reported bounds.

5.5   Linear Layer: $\pi = (3, 2, 0, 4, 1)$

The choice of a linear layer is crucial for the proper mixing among the blocks, which in turn affects the differential and algebraic properties. Out of 5! possible permutations of the words, 44 do not exhibit fixed points. Moreover, we found that iterating such permutations for multiple rounds achieves different differential and algebraic bounds. Accordingly, we searched their space to find the ones that offer the best diffusion and result in the minimum number of active Simeck sboxes in the smallest number of steps. We found that only two permutations, $\pi = (3, 2, 0, 4, 1)$, and $\pi' = (3, 4, 1, 2, 0)$ achieve these conditions. More precisely, using either π or π', ACE reaches full bit diffusion in 5 steps and has 21 active Simeck sboxes (see Table 4.1). Accordingly, we picked π as our linear layer.

5.6   Round and Step Constants

5.6.1   Rationale

We use the following set of constants to mitigate the self-symmetry distinguishers.

- **Three 8-bit unique step constants** (sc_0^i, sc_1^i, sc_2^i). The 3-tuple constant value is unique across all steps, hence it destroys any symmetry between the steps of the permutation. Accordingly, we mitigate slide distinguishers [18]. We also require that for any given step i, $sc_0^i \neq sc_1^i \neq sc_2^i$ in order to destroy any symmetry between word shuffles.

- **Three 8-bit unique round constants** (rc_0^i, rc_1^i, rc_2^i). One bit of each round constant is XORed with the state of the Simeck sbox in each round to destroy the preservation of any rotational properties. Moreover, we append 31 '1' bits to each one bit constant, which results many inversions, and accordingly breaks the propagation of the rotational property in one step.

Our choice of the LFSR polynomial to generate the constants ensures that each tuple of such constants does not repeat due to the periodicity of the 8-tuple sequence constructed from the decimated m-sequence of period 127 (for theory of m-sequences see [19]).

5.6.2   Generation of round and step constants

We use an LFSR of length 7 with the feedback polynomial $x^7 + x + 1$ to generate the round and step constants of ACE. To construct these constants, the same LFSR is run in a 3-way parallel configuration, as illustrated in Figure 5.1. Let $\underline{a}$ denote the sequence generated by the initial state $(a_0, a_1, \ldots, a_6)$ of the LFSR without parallelization. The parallel version of this LFSR outputs three sequences, all of them using decimation exponent 3. Instead of one XOR gate feedback for the non-parallel implementation, three XOR gates are needed to compute three feedback values.

Figure 5.1: LFSR for generating ACE constants.

Figure 5.2 shows the same LFSR as Figure 5.1, but annotated with sequence elements at the moment when the last three bits for the round constants are available. The round constants are produced by the sequence elements a_{24i+21}, a_{24i+22} and a_{24i+23} in every clock cycle as follows.

$$rc_0^i = a_{24i+21}\|a_{24i+18}\|a_{24i+15}\|a_{24i+12}\| \ a_{24i+9}\|a_{24i+6}\|a_{24i+3}\|a_{24i+0}$$
$$rc_1^i = a_{24i+22}\|a_{24i+19}\|a_{24i+16}\|a_{24i+13}\|a_{24i+10}\|a_{24i+7}\|a_{24i+4}\|a_{24i+1}$$
$$rc_2^i = a_{24i+23}\|a_{24i+20}\|a_{24i+17}\|a_{24i+14}\|a_{24i+11}\|a_{24i+8}\|a_{24i+5}\|a_{24i+2}$$

where

- rc_0^i corresponds to the sequence $\underline{a}$ with decimation 3

- rc_1^i corresponds to the sequence $\underline{a}$ shifted by 1, then decimated by 3

- rc_2^i corresponds to the sequence $\underline{a}$ shifted by 2, then decimated by 3

Figure 5.2: Schematic of the 3-way parallel LFSR for generation of the constants

In every 8-th clock cycle, the step constants are needed in addition to round constants. The computation of step constants does not need any extra circuitry, but rather uses the three feedback values a_{24i+28}, a_{24i+29} and a_{24i+30} together with all 7 state bits,

$$a_{24i+30}, a_{24i+29}, \underbrace{a_{24i+28}, a_{24i+27}, a_{24i+26}, a_{24i+25}, a_{24i+24}, a_{24i+23}, a_{24i+22}, a_{24i+21}}_{sc_0^i}$$

Figure 5.3: Three 8-bit step constants, generated from 10 consecutive sequence elements

annotated in Figure 5.2. Figure 5.3 shows how the 10 consecutive sequence elements are used to generate step constants. The step constants are given by:

$$sc_0^i = a_{24i+28}\|a_{24i+27}\|a_{24i+26}\|a_{24i+25}\|a_{24i+24}\|a_{24i+23}\|a_{24i+22}\|a_{24i+21}$$
$$sc_1^i = a_{24i+29}\|a_{24i+28}\|a_{24i+27}\|a_{24i+26}\|a_{24i+25}\|a_{24i+24}\|a_{24i+23}\|a_{24i+22}$$
$$sc_2^i = a_{24i+30}\|a_{24i+29}\|a_{24i+28}\|a_{24i+27}\|a_{24i+26}\|a_{24i+25}\|a_{24i+24}\|a_{24i+23}$$

We provide an example of how to obtain hex values of constants from the m-sequence in Appendix C.

5.7 Number of Rounds and Steps

Our rationale for choosing the number of rounds u and number of steps s of ACE is based on achieving the best trade-off between security and efficiency. By security and efficiency, we mean the value of (u, s) for which ACE is indistiguishable from a random permutation and $u \times s$ is minimum. We now justify the choice of $(u, s) = (8, 16)$ for ACE.

Diffusion. Our first criteria is that s should be at least $3 \times m$ where m is the number of #steps needed to achieve full bit diffusion in the state. This choice is inspired from [20] and directly adds a 33% security margin against meet/miss-in-the-middle distinguishers, as in $2m$ steps full bit diffusion is achieved in both forward and backward directions. Hence, $m = 5 \implies u \geq 4$ and $s \geq 15$ (c.f. Section 4.1). However, we found that we cannot choose $u = 4, \ldots, 7$, because we also aim to achieve good resistance against differential and linear cryptanalysis. Note that having a smaller number of rounds results in a weaker Simeck sbox.

Maximum expected differential characteristic probability (MEDCP). Our second criteria is to push the MEDCP value of ACE to below 2^{-320}. This value depends on the MEDCP of a u-round Simeck sbox and the number of such active sboxes in s steps (denote by n_s). We have $n_{15} = 19$ and $n_{16} = 21$ (see Table 4.1).

Table 5.1 depicts that $(u, s) \in \{(8, 15), (8, 16), (9, 15), (9, 16)\}$. However, if we consider the differential effect, then the differential probability is $2^{-15.8}$ when $u = 8$. An indepth analysis of such effect has been provided in [6] where the CryptoSMT tool [25] is used to obtain the optimal differential characteristics and corresponding probabilities.

Table 5.1: Optimal differential characteristic probability p for u-round Simeck sbox and the corresponding MEDCP of ACE for $s = 15, 16$.

u	4	5	6	7	8	9
$\log_2(p)$	-6	-8	-12	-14	-18	-20
$n_{15} \times \log_2(p)$	-114	-152	-228	-266	-342	-380
$n_{16} \times \log_2(p)$	-126	-168	-252	-294	-378	-420

Accordingly, we have:

$$n_{15} \times -15.8 = 19 \times -15.8 = -300.2 > -320$$

$$n_{16} \times -15.8 = 21 \times -15.8 = -331.8 < -320.$$

Thus, we ignore $(u, s) = (8, 15)$ and choose $(u, s) = (8, 16)$. The other two choices are discarded from the efficiency perspective as $u \times s = 135$ (resp. 144) when $(u, s) = (9, 15)$ (resp. (9,16)) compared to 128 iterations when $(u, s) = (8, 16)$.

5.8 Choice of Rate Positions

We have followed a similar strategy in choosing the rate position as the one that has been used in sLiSCP [5, 7]. More precisely, we absorb message blocks in words A and C. Such rate positions allow the input bits to be processed by the Simeck sboxes as soon as possible so we achieve faster diffusion. Also, our choice forces any injected differences to activate Simeck sboxes in the first step which also enhances ACE's resistance to differential and linear cryptanalysis. This observation has also been confirmed by a third party cryptanalysis of sLiSCP [27].

5.9 Statement

The authors declare that there are no hidden weaknesses in the ACE permutation, ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256.

Chapter 6

Hardware Design and Analysis

In this chapter, we describe the hardware implementation of ACE_module, which is a single module that supports all three functionalities: authenticated encryption, verified decryption, and hashing using the same hardware circuit. Section 6.1 outlines some of the principles underlying our hardware design. Section 6.2 describes the interface and top-level ACE_module module. Section 6.3 goes into the details of the state machine and datapath implementation. And, finally, Section 6.4 presents the implementation results for four ASIC libraries and two FPGAs.

6.1   Hardware Design Principles

The design principles and assumptions followed by the hardware implementations:

1. **Multi-functionality module.** The system should support all three operations, namely authenticated encryption, authenticated decryption, and hashing, in a single module (Figure 6.1), because lightweight applications generally cannot afford the extra area for separate modules. As a result, the area for the system will be greater compared to a single-function module.

2. **Single input/output ports.** In small devices, ports can be expensive, and optimizing the number of ports may require additional multiplexers and control circuitry. To ensure that we are not biasing our design in favour of the system and at the expense of the environment, the key, nonce, associated data, and message all use a single data-input port (Table 6.1). Similarly, the output ciphertext, tag, and hash all use a single output port (Table 6.1). That being said, the authors agree with the proposed lightweight cryptography hardware API's [23] use of separate public and private data ports and will update implementations accordingly.

3. **Valid-bit protocol and stalling capability.** The environment may take an arbitrarily long time to produce any piece of data. For example, a small microprocessor could require multiple clock cycles to read data from memory and write

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it to the systems input port. We use a single-phase valid bit protocol, where each input or output data signal is paired with a valid bit to denote when the data is valid. The receiving entity must capture the data in a single clock cycle (Figure 6.4), which is a simple and widely applicable protocol. The system shall wait in an idle state, while signalling the environment that it is ready to receive. In reality, the environment can stall as well. In the future, ACE hardware implementations will be updated to match the proposed lighweight crypto hardware API's use of a valid/ready protocol for both input and output ports.

4. **Use a "pure register-transfer-level" implementation style.** In particular, use only registers, not latches; multiplexers, not tri-state buffers; synchronous, not asynchronous reset; no scan-cell flip-flops; clock-gating is used for power and area optimization.

6.2 Interface and Top-level Module

In Figure 6.1, we depict the block diagram of the top-level ACE_module and the description of each interface signal is given in Table 6.1.

Table 6.1: Interface signals

Input signal	Meaning
reset	resets the state machine
i_mode	mode of operation
i_dom_sep	domain separator
i_padding	the last block is padded
i_data	input data
i_valid	valid data on i_data

Output signal	Meaning
o_ready	hardware is ready
o_data	output data
o_valid	valid data on o_data

Table 6.2: Modes of operation

i_mode			
(1)	(0)	Mode	Operation or phase
0	0	ACE-$\mathcal{E}$	Encryption
0	1	ACE-$\mathcal{D}$	Decryption
1	0	ACE-$\mathcal{H}$-256	Absorb
1	1	ACE-$\mathcal{H}$-256	Squeeze

The ACE-$\mathcal{AE}$-128 mode can perform two operations: authenticated encryption (ACE-$\mathcal{E}$) and verified decryption (ACE-$\mathcal{D}$). The ACE-$\mathcal{H}$-256 mode has two phases: absorbing and squeezing, both of which have the same domain separator. We use the i_mode input signal (see Table 6.2) to distinguish between the operations or phases.

The environment separates the associated data and the message/ciphertext, and performs their padding if necessary, as specified in Sections 2.4 and 2.5. The control input i_pad is used to indicate that the last i_data block is padded. The hardware is unaware of the lengths of individual phases, hence no internal counters for the number of processed blocks are needed. The domain separators are provided by the environment and serve as an indication of the phase change for AEAD functionality, i.e., whether the input data for ACE-$\mathcal{AE}$-128 is the key, associated data or plaintext/ciphertext. For

Figure 6.1: Top-level ACE_module and the interface with the environment

ACE-$\mathcal{H}$-256, the phase change is indicated by the change of the i_mode(0) signal, as shown in Table 6.2.

6.2.1 Interface protocol

The top-level ACE_module is in constant interaction with the environment application. We show this interaction in a form of protocol in Figures 6.2a-6.2d for the ACE-$\mathcal{AE}$-128 encryption example, using the signal names from Figure 6.1. The environment is only allowed to send data to the ACE hardware when it is in the idle mode, which is indicated by the hardware using the o_ready signal. The only exception from this behaviour is the reset signal, which will force the hardware module to reset its state machine and return to the idle state and set the o_ready signal. Figure 6.2a shows the environment (one the left) resetting the ACE_module (on the right), waiting for the o_ready to be asserted, then sending the key and the nonce, as specified in load-$\mathcal{AE}(N, K)$ in Section 2.4. Upon receiving all four key and nonce blocks, the ACE_module starts with the initial ACE permutation, as indicated on the right. After completing the permutation, ACE_module enters idle state and asserts the o_ready to signal to the environment that it can accept new data. The environment proceeds with K_0, accompanied by the proper values for i_mode and i_dom_sep. Loading and initialization is the same for both ACE-$\mathcal{E}$ and ACE-$\mathcal{D}$, which is why Figure 6.2a shows i_mode=0− (see Table 6.2). The ACE_module performs the ACE permutation and asserts o_ready, and the environment responds with the second key block K_1.

Figure 6.2b shows the communication between the environment and the ACE_module for the first two blocks of associated data AD_0 and AD_1. The environment sets i_dom_sep to value 1 and signals the arrival of new AD block with i_valid. After completing the ACE permutation, ACE_module asserts the o_ready. Figure 6.2c shows the handshake signals for encryption of message blocks M_5 and M_6. The environment sends the plaintexts along with i_dom_sep=2 and i_mode=00. The ACE_module receives M_5, encrypts it and immediately returns C_5 together with asserted o_valid, then starts the ACE permutation and asserts o_ready upon its completion. With exception of the tag generation, encryption (decryption) is the only phase during ACE-

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(a) Loading and initialization

(b) Processing associated data

(c) Encryption

(d) Finalization and tag generation

Figure 6.2: Interface protocol

$\mathcal{AE}$-128 when the ACE_module sends data to the environment.

Each time a data block is transmitted between the environment and the ACE_module the valid bit protocol is used: the environment asserts the i_valid, and the ACE_module the o_valid signal. This naming convention is centred around the hardware module. Another important part of the handshake between the environment and ACE_module is the o_ready signal: ACE_module sets this signal to 1 when it is ready to receive new data from the environment, and to 0 when it is busy and wants the environment to wait.

When all message blocks are encrypted, the finalization and tag generation begins (Figure 6.2d). The environment changes i_dom_sep to value 0 and starts sending the key blocks. After receiving K_0, ACE_module performs an ACE permutation and sets o_ready. After receiving K_1, ACE_module again performs an ACE permutation, but this time replies to the environment with two tag blocks T_0, T_1 , each accompanied by the o_valid signal. Afterwards, the ACE_module returns to idle and asserts the o_ready signal.

As was mentioned before, the ACE_module is unaware of the number of AD and M blocks, and relies on the environment to set proper values for i_dom_sep. However, the ACE state machine is not completely free of counters: a small internal counter is needed to keep track of the number of blocks received and transmitted during the loading and initialization phase and the tag extraction. Another counter is needed to keep track of the ACE permutation, which requires 128 clock cycles to complete. More details follow in Subsection 6.2.3.

In streaming applications, the total length of the data might not be known at the time that the message begins streaming. Hence, each time data is sent to the cipher, the environment informs the cipher what type of data is being sent. This information is easily encoded using a two-bit mode signal to denote which operation is to be performed (Encryption, Decryption, Hashing) and the two-bit domain separator to denote the type of data being processed (associated data, message, ciphertext). The hardware uses o_ready to signal that it is ready to receive new data, and the environment uses i_valid to signal that it is sending data to the hardware.

6.2.2 Protocol timing

More detailed representation of the events between the environment and the ACE_module is possible with the use of timing diagrams in Figures 6.3-6.5. In each diagram, the top few lines show the interface signals (Table 6.1), which were already discussed as a part of the communication protocol between the environment and the hardware module. Signals i_mode and i_dom_sep are omitted from the timing diagrams: their current value is the same as shown in the corresponding protocol figure. The vertical ticks on the horizontal lines represent the time: a single column shows the signal values within the same clock period.

Loading and initialization during ACE-$\mathcal{AE}$-128. Figure 6.3 shows the loading and

initialization up to the beginning of the second ACE permutation; it corresponds to the upper half of the protocol Figure 6.2a. At the top, we can see the interface signals reset, o_ready, i_valid and i_data, followed by the internal signals count, pcount and phase, which are a part of the ACE state machine. Counter count is needed to keep track of the number of loaded key and nonce blocks. It is then reused to count the number of key blocks processed during the rest of initialization and during finalization, and for counting the number of produced tag and hash blocks. Counter pcount keeps track of the 128 clock cycles needed for one ACE permutation. After the environment deasserts the reset signal, the ACE_module clears the internal state machine signals, enters the Load phase and sets the o_ready signal. The environment responds with the first key block K_0, accompanied with asserted i_valid. The ACE_module stores the new data into its internal state and increments count. Figure 6.3 shows an example when the response of the environment varies, e.g., the delay between K_0 and K_1 is bigger than delay between K_1 and N_0. After receiving N_1, the ACE_module performs the first ACE permutation, denoted LoadPerm: the o_ready signal is dropped and the pcount increments every clock cycle. After LoadPerm is finished, the state machine enters the Init phase and the o_ready signal is set to 1 while waiting for the first key block. Arrival of the next i_valid and K_0 triggers the second ACE permutation.

Figure 6.3: Timing diagram: Loading and initialization during ACE-$\mathcal{AE}$-128

Encryption during ACE-$\mathcal{AE}$-128. Figure 6.4 shows the timing diagram during the encryption of message blocks M_5 and M_6, corresponding to protocol in Figure 6.2c. It clearly shows both sides of the valid-bit protocol. The first five lines show the top-level interface signals and line six shows the value of the permutation counter pcount: $8 \cdot 16 = 128$ clock cycles are needed to complete 16 steps, 8 rounds per step, for one ACE permutation. The values round and step, shown in the last two lines in Figure 6.4 are not two actual counters, but the lower and upper bits of counter pcount.

After completing the previous permutation, ACE_module asserts o_ready. The environment replies with a new message block M_5 accompanied by an i_valid signal. The hardware immediately encrypts, returns C_5 and asserts o_valid. This clock cycle is also the first round of a new ACE permutation and the o_ready is deasserted, indicating that the hardware is busy. Figure 6.4 also shows the ACE_module remaining
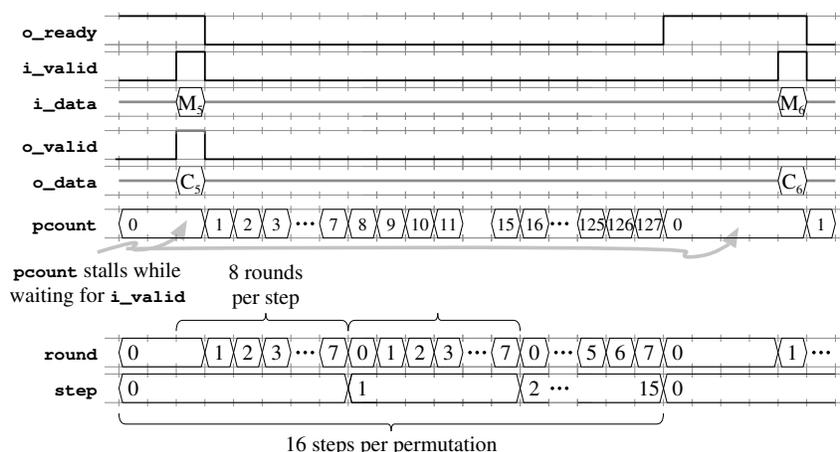
Figure 6.4: Timing diagram: Encryption during ACE-$\mathcal{AE}$-128

busy (o_ready = 0) for the duration of one ACE permutation. When pcount wraps around from 127 to 0, the hardware is again idle and ready to receive new input, in this case M_6. The counter count is not being used. Since processing of associated data is very similar to encryption, with exception of AD blocks instead of M blocks and no output for o_data, we do not show a separate timing diagram.

Tag phase during ACE-$\mathcal{AE}$-128. Figure 6.5 shows a part of the finalization, tag extract and the return of the state machine into the loading phase, corresponding to the lower part of the protocol in Figure 6.2d. The timing diagram starts with the completion of the ACE permutation after block K_0 was received, followed by K_1 immediately, which triggers the second ACE permutation during finalization, which is also the last ACE permutation of ACE-$\mathcal{AE}$-128. After the permutation, ACE_module sends two tag blocks to the environment. The counter count is used to return the ACE_module to the Load phase, where it sets the o_ready signal and awaits the new key and nonce in case of ACE-$\mathcal{AE}$-128, or fixed IV in case of ACE-$\mathcal{H}$-256.
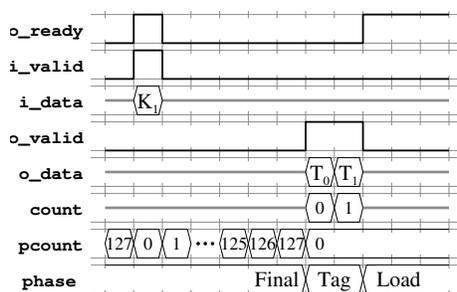

Figure 6.5: Timing of tag phase during ACE-$\mathcal{AE}$-128

6.2.3 Control phases

In the previous section (6.2.2) we touched on the different phases of the control circuitry. The phases are categorizations of the active connections between the ACE permutation on the interface signals. The seven categories, i.e., phases, are shown in Figure 6.6 and described below:

- The first column shows `Load` (Figure 6.6(I.)) and `Permutation` (Figure 6.6(II.)). The domain separator is not used.
  - `Load` phase: `i_data` is loaded (Figure 6.6(I.)) into A, B, C and E words of the internal state S during ACE-$\mathcal{AE}$-128, and into word B of the internal state S during ACE-$\mathcal{H}$-256, while the other words of S are set to 0. During each `Load`, a portion of the internal state S is *replaced* with new data.
  - `Permutation` phase: one iteration of the ACE permutation, without any interactions with the environment. This happens $128\times$ during the `LoadPerm`, and $127\times$ for all other ACE permutations.

- The second column shows `Init/ProcAD/Final/Absorb` (Figure 6.6(III.)) and `Squeeze` (Figure 6.6(IV.)). The domain separator is set to 1 for `ProcAD` and to 0 for all other phases in this column.
  - `Init/ProcAD/Final/Absorb` phase: the `i_data` is *added* (XORed) to the S_r portion of the internal state S before entering the ACE permutation, i.e., between two consecutive ACE permutations. This phase is treated as one phase from the hardware perspective, i.e., the state machine drives same control signals, but from the algorithm perspective it captures the behaviour during initialization, processing associated data and finalization for ACE-$\mathcal{AE}$-128, and during absorbing for ACE-$\mathcal{H}$-256.
  - `Squeeze` phase: during ACE-$\mathcal{H}$-256 squeezing, `o_data` is extracted from the A and C words of the internal state S, then ACE permutation is triggered (except for the last block H_3). There is no adding or replacing of any portion of the internal state S.

- The third column shows `Encrypt` (Figure 6.6(V.)) and `Decrypt` (Figure 6.6(VI.)) phase during ACE-$\mathcal{AE}$-128. For both phases, the domain separator is set to 2.
  - `Encrypt` phase: received `i_data` (plaintext) is *added* to the S_r portion of the internal state S and the result of this operation (ciphertext) is passed to the `o_data` output. The resulting ciphertext is a part of the internal state S when the next ACE permutation begins.
  - `Decrypt` phase: received `i_data` (ciphertext) is XORed with the S_r portion of the internal state S and the result of this operation (plaintext) is passed to the `o_data` output. The resulting plaintext does *not* enter the next ACE permutation. Instead, the ciphertext from `i_data` is used to *replace* the S_r portion of the internal state before the next ACE permutation begins.

- The last column shows the Tag phase (Figure 6.6(VII.)). The domain separator is not used.

  - Tag phase: during tag extract, the o_data is extracted from the A and C words of the internal state S.

Figure 6.6: Phases and datapath operations

Note that the phases in Figure 6.6, that are showing ACE permutation, only show one round: in Figures 6.6(III.-VI.) the first round of ACE permutation, where interaction with the environment is required, and in Figure 6.6(II.) any round of ACE permutation, where no interaction with the environment takes place. For example, the encryption of M_5 block from timing diagram in Figure 6.4, consists one phase Encrypt (V.), followed by 127× Permutation (II.) - all together 128 rounds of ACE permutation. Table 6.3 summarizes the phases shown in Figure 6.6, including datapath operation taken (column dp. op.), and specifies the exact S_r input to the ACE permutation and the output of ACE_module for the environment, i.e., the o_data value.

Table 6.3: Control table for datapath based on phases from Figure 6.6

Function	i_mode	i_dom_sep	Phase	Dp. op	Input to permutation	Output to environment
–	– –	– –	Load	I.	×	×
–	– –	– –	Permutation	II.	S_r	×
En/De-crypt	0–	00	Init	III.	$S_r \oplus$ i_data	×
En/De-crypt	0–	01	ProcAD			
En/De-crypt	0–	00	Final			
Hash	10	00	Absorb			
Hash	11	00	Squeeze	IV.	S_r	S_r
Encrypt	00	10	Encrypt	V.	$S_r \oplus$ i_data	$S_r \oplus$ i_data
Decrypt	01	10	Decrypt	VI.	i_data	$S_r \oplus$ i_data
En/De-crypt	0–	– –	Tag	VII.	×	A, C of S

– stands for "don't care"   × stands for "not used"

6.3 Hardware Implementation Details

In this section, we describe the implementation details of ACE_module. Section 6.3.1 describes how the state machine is derived from the interface protocols (Figures 6.2a–6.2d) and datapath phases (Figure 6.6). Section 6.3.2 describes the datapath.

6.3.1 State machine

Control flow between phases. Figure 6.7 shows all possible transitions between the state machine phases from Figure 6.6. After reset signal, we first enter Load, followed by a single ACE permutation LoadPerm. Although load-$\mathcal{AE}(N, K)$ and load-$\mathcal{H}(IV)$ are different, they are considered as a unified Load phase for the high-level description of the state machine in Figure 6.7. After LoadPerm, the transition depends on the operation, i.e., mode: the left branch is taken during ACE-$\mathcal{AE}$-128, and the right branch during ACE-$\mathcal{H}$-256.

The first phase on the ACE-$\mathcal{AE}$-128 branch is Init. The transition from Init depends on the value of i_dom_sep signal. When i_dom_sep=1, we enter the ProcAD phase, and remain there for as long as i_dom_sep=1. Regardless if current state is Init or ProcAD, the i_dom_sep=2 will trigger transition to either Encrypt or Decrypt, depending on the i_mode value. Note that because of our padding rule, there will always be at least one block with i_dom_sep=2. The FSM will enter the Final phase only when the domain separator changes to 0. The phase Final is followed by the Tag phase and the return to the reset state unconditionally.

For ACE-$\mathcal{H}$-256, the state machine always transitions to Absorb phase, because the padding rule implies at least one message block. The domain separator is always 0, but we use the 2-bit i_mode signal to trigger the transition from Absorb to Squeeze phase, as shown in Figure 6.7.
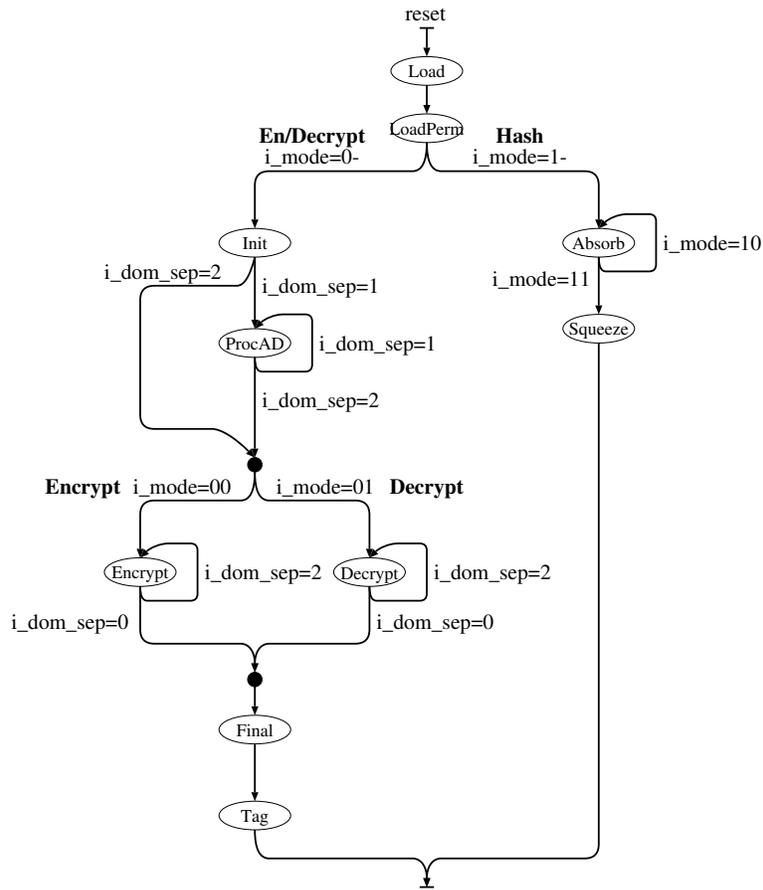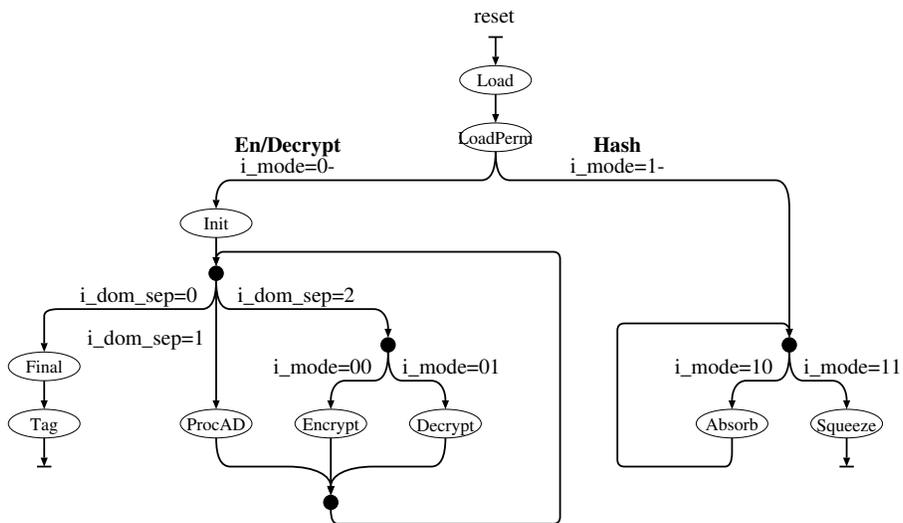
Figure 6.7: Control flow between phases

Figure 6.8: Optimized control flow between phases

Optimized control flow between phases. Figure 6.8 shows the optimized control flow from Figure 6.7, with ACE-$\mathcal{AE}$-128 on the left and ACE-$\mathcal{H}$-256 on the right branch. The optimized figure is annotated with transient states in which the paths split or join. The values of the interface signals are checked in the splitting transient states. Note that transient states do not indicate a clock cycle boundary, while all other states do.

Summary of control flow. The high-level algorithms for ACE (Figures 2.3 and 2.4) were designed to simplify the state machine. Functionally, it is equivalent for the boundary between phases to occur either before or after the permutation. The boundary was placed *after* the permutation updates the state register. As will be demonstrated in Section 6.3.2, with this structure the two-bit domain separator is sufficient to determine the value of many of the multiplexer select lines and other control signals. All phases that have a domain separator of "00" have the same multiplexer select values. The same also holds true for "01". Unfortunately, this cannot be achieved for "10", because encryption and decryption require different control signal values, but the same domain separator. Using the domain separator to signal the transition between phases for encryption and decryption also simplified the control circuit. For hashing, the transition from absorbing to squeezing is controlled by the i_mode signal.

A final note about the control flow diagrams in this section: only when the number of iterations in a certain phase depends on the length of the data, i.e., ℓ_X, $X \in \{AD, M, C\}$, which is indicated by the value change of interface signal i_mode or i_dom_sep, we show the transition to itself. While the phases Load, Init, Final, Tag and Squeeze also take more than one iteration, the number of iterations is fixed by the ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256 algorithms specified in Chapter 2 and hence not shown in the control flow diagrams in Figures 6.7 and 6.8. However, this level of detail is included in the state machine Figures 6.9-6.11.

Derivation of state machine from control flow. The implementation details for the control flow from Figure 6.8 are shown as state machines, spread out through Figures 6.9-6.11. All the phases are split into at least two parts, following the convention iStateName and pStateName, where the prefix "i" stands for "idle" and "p" for "permutation", and the state name corresponds to the phase name. In the "idle" states, the ACE_module is waiting for new input from the environment, i.e., for i_valid=1. In the "permutation" states the ACE permutation is running and the ACE_module is busy, i.e., o_ready=0. The normal structure can be seen in the iInit and pInit states in Figure 6.11. There are a few exceptions to the normal structure:

- The phase Load (Figure 6.9) can receive multiple blocks consecutively without running a permutation. Hence, there is a third state Load without a prefix in addition to iLoad and pLoad.

- The phase Tag (Figure 6.11) can transmits multiple blocks consecutively without running a permutation. Hence, there is no need for a p-state.

- The states pAbsorb and pSqueeze (Figure 6.10) have the same behaviour for

idling, and so their idle states are merged into `iHash`.

- Similarly, states `pProcAD`, `pEncrypt` and `pDecrypt` all use the same merged idle state `iAED`.

Each state is annotated with four circles to denote the four bits encoding the current values on the interface signals `i_mode` and `i_dom_sep`. An empty circle denotes 0, a filled circle denotes 1, and a circle with a dash is a "don't care" value, meaning the behaviour is independent of this bit. Each transition between a pair of states is annotated with a roman numeral from Figure 6.6 denoting the datapath operation to be performed.

State machine: Loading. The loading part of the state machine is shown in Figure 6.9. The `reset` control signal places the state machine into the `iLoad` idle state, where it awaits the first key block in the case of ACE-$\mathcal{AE}$-128 or a single IV block in the case of ACE-$\mathcal{H}$-256. In case of ACE-$\mathcal{AE}$-128, the environment sends $4(2 + 2)$ key and nonce blocks, and the state machine uses an internal counter `count` to keep track of the loading,i.e., to keep track of iterations back to state `Load`. This behaviour was explained in timing diagram in Figure 6.3. After the loading blocks are received, the state machine enters the permutations state `pLoad`, which is controlled by the counter `pcount` counting steps and rounds as was shown in Figure 6.4. The transition to the left branch is made in the case of `i_mode=0-`, i.e., for ACE-$\mathcal{AE}$-128, in which case the state machine continues in Figure 6.11, and to the right branch in the case of `i_mode=1-`, i.e., in the case of ACE-$\mathcal{H}$-256 in which case the state machine continues in Figure 6.10. In both cases, the next state is an idle state.

State machine: Hashing. The hashing states continue in Figure 6.10, corresponding to the `Absorb` and `Squeeze` phase in the right branch of the control flow in Figure 6.8. The first state entered is the merged idle state `iHash`. Upon the next `i_valid`, we can continue to one of the permutation states based on the value of the `i_mode(0)` signal, which is set by the environment. The left loop in Figure 6.10 shows the state machine entering `pAbsorb` when `i_mode=10`, followed by the `iHash` idle state. The end of the message for ACE-$\mathcal{H}$-256 is indicated by the mode chage to `i_mode=11`, which causes the transition from `iHash` to `pSqueeze`. Note that since the number of hash blocks is fixed and does not require any input from the environment, we do not need a return loop from `pSqueeze` to `iHash`. The state machine uses the counter `count` to keep track of the hash blocks produced so far. No ACE permutation is needed after H_3.

State machine: Encryption and decryption. The left branch in Figure 6.9, taken in the case of ACE-$\mathcal{AE}$-128, is shown in Figure 6.11. Similarly, we first enter the `iInit` state and transition to `pInit` at the arrival of the next `i_valid`. The counter `pcount` is, as usual, used to keep track of the ACE permutation, and the counter `count` of the number of iterations in `Init` phase. After the second ACE permutation in the `Init` phase is completed, we proceed to `iAED`, a merged idle state for `iProcAD`, `iEncrypt` and `iDecrypt`. The next `i_valid` triggers the transition

Figure 6.9: State machine: Loading

Figure 6.10: State machine: Hashing

to pProcAD if i_dom_sep=01 or to transient state on the right if i_dom_sep=10, for either pEncrypt or pDecrypt, depending on the i_mode. Either way, an ACE permutation starts, and the pcount runs for 128 cycles. After completing an ACE permutation, the state machine returns to the idle state iAED. When we observe i_dom_sep=00, the state machine will transition into pFinal state and run the first ACE permutation in Final phase. Again, counter count is used to keep track of the two iterations. The idle state iFinal is entered only once. Finally, the state machine enters the Tag state, and ACE_module transmits two tag blocks to the environment. Again, counter count is used, but this time, no ACE permutation is required.

Summary of state machine. The state machine is responsible for the o_valid and o_ready interface signals. It is also tasked with control signals for the multiplexers in ACE datapath, which accommodate different interactions between ACE_module and the environment, i.e., different phases from Figure 6.6. This will be discussed in more detail in Section 6.3.2.

Figure 6.11: State machine: Encryption and decryption

The state machine and encodings for control signals were designed to take advantage of similarities in structure to enable optimizations in the control circuitry. The only control-flow decision made within an idle state is to exit when i_valid='1'. This reduces the number of idle states and facilitates combinational logic optimizations due to the uniform structure of the control flow. Loading, squeezing, and finalization all use the same one-hot counter to count their iterations. Also, all seven of the states that perform the permutation have the same control structure, which provides opportunities for logic synthesis optimizations, such as common subexpression elimination.

6.3.2 ACE datapath

Figure 6.12 shows the schematic for the ACE datapath. The top of the figure depicts the five 64-bit signals A, B, C, D and E, with the A and C registers split into half. The triangular shapes on signal lines denote splitting or joining of signals, e.g., the 64-bit data input i_data is split into two halves, one for each 32-bit part of the S_r. Similarly, the output of the 32-bit 3-to-1 multiplexer is joined with the unmodified A_0

(half of signal A) before entering the SB-64$_1$. Next the hardware components required for absorbing, replacing and driving the outputs, annotated with "i_data and o_data muxes", are shown. The rest of the Figure 6.12 shows one step of the ACE permutation, annotated on the left.

Module SB-64$_1$ in Figure 6.12 implements one out of eight rounds required for SB-64. The three parallel SB-64$_1$ modules are shown in Figure 6.12. There is an important difference between Figures 2.1 and 6.12:

- Figure 2.1 shows the ACE-step, containing three parallel Simeck boxes SB-64
- Figure 6.12 shows the ACE-datapath, the actual hardware implementation, where we implement one round SB-64$_1$ and reuse it 8 times to complete one SB-64.

Figure 6.12: The ACE-datapath

The repeated use of SB-64$_1$ is functionally equivalent to SB-64. However, implementing SB-64$_1$ has multiple advantages. The SB-64$_1$ module is one-eighth the size of a full SB-64 module. Also using SB-64$_1$ enables the step and round to use same hardware circuitry. The rounds and steps always use the same hardware, but in different clock cycles, which forces the use of multiplexers inside the ACE permutation. Additions with round and step constants, SB-64$_1$, linear permutation layer and the multiplexers to choose between round and step constants are annotated as well. The step/round

multiplexers are the last layer of multiplexers to choose between loading and permutation outputs before updating the 64-bit registers A, B, C, D and E.

Hardware circuitory for en/de-cryption and hash. Figure 6.12 depicts the ACE permutation, but also shows the circuitry needed to utilize the ACE permutation to have a specific mode. The absorbing hardware part is also shown in Figure 6.12. Apart from the output generation, this behaviour is the same for ACE-$\mathcal{AE}$-128 initialization, processing associated data, encryption, finalization, and for the ACE-$\mathcal{H}$-256 absorbing and squeezing phase. For ACE-$\mathcal{AE}$-128 decryption, extra multiplexers are required on the inputs to the ACE permutation, hence the 3:1 multiplexers before the start of the ACE permutation.

The FSM phases and "i_data and o_data muxes". The state machine is responsible to drive the control signals for all the multiplexers shown in Figure 6.12 based on the current state and values of counters count and pcount. The "round/step muxes" choose the step output (left mux input), when the pcount changes in its step part, and the round input (right mux input), when only the lower round bits of the counter pcount change, as explained in timing diagram in Figure 6.4. For most of the time, the "load/perm muxes" are passing the permutation signals (left mux inputs), with the exception of the Load stages before LoadPerm, as shown in control diagrams and state machines in Figures 6.7-6.9. The "i_data and o_data muxes" consist of six 32-bit multiplexers: two 3-to-1 "i_data multiplexers" and two pairs of 4-to-1 and 2-to-1 "o_data multiplxers".

Tables 6.4-6.6 below show different scenarios for the "i_data and o_data muxes". There are three sets of these multiplexers: 3:1 i_data multiplexers (Table 6.4), 4:1 o_data multiplexers (Table 6.5), and 2:1 o_data multiplexers (Table 6.6). Each set of multiplexers has one instance in the A_1 column of the datapath and one instance in the C_1 column (Figure 6.12). All three tables are formatted in the same way. Column 2 corresponds to the multiplexer for A_1 and column 3 to the multiplexer for C_1. The multiplexer inputs are linked to ACE hardware phases in Figure 6.6 in column 4. Recall that phases **III-VI** include only the first iteration of the ACE permutation, which is the iteration in which all the i_data and o_data interaction with the environment takes place. Every one of these phases is then followed by the remaining 127 iterations of the ACE permutation, i.e., 127× phase **II**. In phase **II**, the i_data and o_data are disconnected from the ACE permutation circuit in the lower part of Figure 6.12. For the "i_data multiplexers" in Table 6.4 there are two exceptions, which have the same multiplexer inputs for all 128 iterations of ACE permutation: the hash sqeeuzing (**IV** followed by 127× **II**) and the loading permutation LoadPerm (128× **II**). Table 6.6 has two exceptions, where no output is generated during any part of the phase, including all 128 iterations of the ACE permutation: Init, ProcAD, Final, Absorb (Figure 6.6(**III**)), and the all Load and LoadPerm phases (Figure 6.6(**I, II**)).

Table 6.4: 3-to-1 "i_data multiplexers"

mux input position *	S_r input for permutation		Fig.6.6 subfigure	description
	A_1 part	C_1 part		
0	i_data$_0$	i_data$_1$	**VI**	*replace* S_r with new data
1	$A_1 \oplus$ i_data$_0$	$C_1 \oplus$ i_data$_1$	**III, V**	*add* new data into S_r
2	A_1	C_1	**IV, II**	hash squeezing and during ACE permutation iter. **II**

∗ mux input positions are numbered from the left

Table 6.5: 4-to-1 "o_data multiplexers"

mux input position *	4-to-1 mux output for 2-to-1 mux		Fig.6.6 subfigure	description
	o_data$_0$ part	o_data$_1$ part		
0	$A_1 \oplus$ i_data$_0$	$C_1 \oplus$ i_data$_1$	**V, VI**	data block C_i or M_i
1	A_1	C_1	**IV**	hash block H_i
2	A_1	A_0	**VII**	tag block T_0
3	C_1	C_0	**VII**	tag block T_1

∗ mux input positions are numbered from the left

Table 6.6: 2-to-1 "o_data multiplexers"

mux input position *	2-to-1 mux output for		Fig.6.6 subfigure	description
	o_data$_0$ part	o_data$_1$ part		
0	4-to-1 o_data$_0$ mux output	4-to-1 o_data$_1$ mux output	**IV, V VI, VII**	output data block M_i, C_i, T_i or H_i
1	all 0 block	all 0 block	**I, II, III** and	no output

∗ mux input positions are numbered from the left

Estimated and synthesized cost of ACE permutation. In Table 6.7, we provide both the estimate based on the CMOS 65 nm ASIC library and actual hardware area of the ACE permutation. For the CMOS 65 nm we use an estimate of 3.75 GE for a 1-bit register and 2.00 GE for a 2-input XOR gate. The row "other XOR" contains the XOR gates needed for masking B, D and E with outputs of the three SB-64$_1$ modules, and for the addition of step constants.

First we provide the estimate for the ACE permutation without multiplexers. Then we add the round/step multiplexers and a minimum number of load multiplexers, in this case for word B which is loaded during ACE-$\mathcal{H}$-256, and the synthesized area of the LFSR for the constant generation, to obtain the estimate (and synthesized results) for the ACE permutation with minimal amount of multiplexers added.

Finally, we add the estimates for the hardware needed to support the mode. We estimate the "i_data and o_data muxes" as 2-to-1 muxes, e.g., a 4-to-1 mux is estimated as 3 2-to-1 muxes, yielding in total 6 2-to-1 muxes per bit. The XORs for mode are the ones required for the encryption/decryption. Additional load multiplexers are needed to load the entire state. These components, listed in the second part of Table 6.7, amount to 1408 GE (estimated), but the synthesis reports show, the tools were able

to do some optimizations, e.g., using actual (and smaller) 3-to-1 muxes. Finally, we list the estimate and the synthesized result for the complete datapath, followed by the synthesized state machine and the results for ACE_module. The complete cipher results reported here are for logic synthesis (i.e., before place-and-route) with a sufficiently long clock period to get a minimum area. This differs from the results in Table 6.9, where the results are for physical synthesis (after place and route) and the selected result is the one with the maximum performance over area-squared ratio (Section 6.4.2).

Table 6.7: ACE permutation hardware area estimate and implementation results

Component	Estimate per unit [GE]	Count	Estimate per component [GE]
State registers	3.75	320	1200
SB-64$_1$	154†	3	462
Other XORs	2.00	$3 \times (64 + 8)$	432
Permutation without muxes (estimate)			2094
round/step muxes	2.00	320	640
min load muxes	2.00	64	128
LFSR for constants	49†		49
Permutation with muxes (estimate)			2911
Synthesized result†			2870
`i_data/ o_data` muxes	2.00	$6 \times 32 \times 2 = 384$	768
XORs for mode	2.00	$32 \times 2 = 64$	128
Additional load muxes	2.0	$64\times = 256$	512
Hardware for the mode (estimate)			1408
Synthesized result†			1128
Complete datapath (estimate)			4319
Synthesized result†			3998
State machine (synthesized result†)			318
ACE_module (estimate)			4637
Synthesized result†			4317

† pre-PAR implementation results

6.4   Hardware Implementation Results

In this section, we provide the ASIC and FPGA implementation results of ACE and its modes. We first give the details of the synthesis and simulation tools and then present the implementation results.

Table 6.8: Tools and implementation technologies

Tools and libraries for ASICs

Logic synthesis	Synopsys Design Compiler vN-2017.09
Physical synthesis	Cadence Encounter 2014.13-s036_1
Simulation	Mentor Graphics QuestaSim 10.5c
ASIC cell libraries	65 nm STMicroelectronics CORE65LPLVT, 1.25V
	TSMC 65 nm tpfn65gpgv2od3 200c and tcbn65gplus 200a at 1.0V
	ST Microelectronics 90 nm CORE90GPLVT and CORX90GPLVT at 1.0V
	IBM 130nm CMRF8SF LPVT with SAGE-X v2.0 standard cells at 1.2V

Synthesis tools for FPGAs

Logic synthesis	Mentor Graphics Precision 64-bit 2016.1.1.28 (for Intel/Altera)
	ISE (for Xilinx)
Physical synthesis	Altera Quartus Prime 15.1.0 SJ (for Intel/Altera)
	ISE (for Xilinx)

6.4.1 Tool configuration and implementation technologies

Table 6.8 lists the configuration details of synthesis and simulation tools and libraries for both ASIC and FPGA implementations. All area results are post place-and-route. Energy results are computed through timing simulation of the post place-and-route design at a clock speed of 10 MHz.

For ASICs, logic synthesis was done using the `compile_ultra` command and clock gating; and physical synthesis (place-and-route) was done with a density of 95%. By selecting a target clock speed, synthesis for ASICs can exhibit a significant range in tradeoffs between speed and area for the same RTL code. The results reported here reflect the clock speed and area that obtained the highest ratio of performance over area-squared. We used area squared, because area is a reasonable approximation of power and is much less sensitive to the choice of the ASIC library than is power itself.

6.4.2 Implementation results

Figure 6.13, Table 6.9, and Table 6.10 present the hardware implementation results. Note that ACE_module performs all three functionalities (authenticated encryption, verified decryption and hashing) in a single module.

Figure 6.13 shows area^2 vs. throughput for ASICs with different degrees of parallelization, denoted by A-p ($p = 1, 2, 3, 4, 8$). The throughput axis is scaled as log(Tput) and the area axis is scaled as log(area^2). The grey contour lines denote the relative optimality of the circuits using Tput/area^2. Throughput is increased by increasing the degree of parallelization (unrolling), which reduces the number of clock cycles per permutation round. Going from $p = 1$ to $p = 8$ results in a 1.72$\times$ area increase, and

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optimality increases as parallelism increases from 1 to 8.

As can be seen by the relative constant size of the shaded rectangles enclosing the data points, the relative area increase with parallelization is relatively independent of implementation technology.

Throughput is measured in bits per clock cycle (bpc), and plotted on a log scale axis.
The area axis is scaled as $\log(\text{Area}^2)$.

Figure 6.13: Area^2 vs Throughput

Table 6.9: ASIC implementation results

Label	Tput	ST Micro 65 nm			TSMC 65 nm			ST Micro 90 nm			IBM 130 nm		
		A	f	E	A	f	E	A	f	E	A	f	E
	[bpc]	[GE]	[MHz]	[nJ]	[GE]	[MHz]	[nJ]	[GE]	[MHz]	[nJ]	[GE]	[MHz]	[nJ]
A-1	0.5	4250	720	27.9	4600	705	20.1	3660	657	62.2	4350	128	46.8
A-2	1	4780	618	18.4	5290	645	12.4	4130	628	35.8	4980	88.9	29.4
A-4	2	5760	394	15.1	6260	588	8.51	4940	484	25.4	5910	90.5	21.1
A-8	4	7240	246	11.4	8090	493	6.40	6170	336	19.4	7550	63.2	18.4

Table 6.9 represents the same data points as Figure 6.13 with the addition of maximum frequency (f, MHz) and energy per bit (E, nJ). Energy is measured as the average

value while performing all cryptographic operations over 8192 bits of data at 10 MHz. As throughput increases, energy per bit decreases consistently, despite higher circuit area and, therefore, power consumption. Connecting modules in a combinational chain can result in an exponential increase of the number of glitches, which drastically increases power consumption. However, because of the small size of the ACE permutation, the actual increase in power is not that significant for parallelism up to degree 8.

Table 6.10: FPGA implementation results

Module	Frequency [MHz]	# of slices	# of FFs	# of LUTs
Xilinx Spartan 3 (xc3s200-5ft256)				
ACE permutation	181	215	327	381
ACE_module	68	727	353	1410
Xilinx Spartan 6 (xc6slx9-3ftg256)				
ACE permutation	306	127	327	378
ACE_module	123	429	365	1272

Module	Frequency [MHz]	# of LC	# of FFs	# of LUTs
Intel/Altera Stratix IV (EP4SGX70HF35M3)				
ACE permutation	128	327	327	296
ACE_module	51	781†	354	781

† ACE_module includes ALTSYNCRAM block memory with 35 bits.

Chapter 7

Efficiency Analysis in Software

The ACE permutation is designed to be efficient on a wide range of resource constrianed devices, which requires the primitive to be efficient in hardware as well as software. Even for lightweight applications, a server communicating with such devices needs to perform the encryption/decryption, and hashing operations at a high speed. We assess the efficiency of the ACE permutation and its modes on two different software platforms: high-performance CPUs and microcontrollers. For the high-performance CPU implementation, we consider a bit-sliced implementation of ACE using SIMD instruction sets.

7.1 Software: High-performance CPU

We implement ACE in the bit-slice fashion using SIMD instruction sets which provides resistance against cache-timing attacks and allows to execute multiple independent ACE instances in parallel. We consider SSE and AVX instruction sets in Intel processors where the SSE and AVX instruction sets, support 128-bit and 256-bit SIMD registers, known as XMM and YMM, respectively. Algorithm 4 depicts the detailed steps of our implementation. In our implementation, packing and unpacking of data are two important tasks, which are performed at the beginning and at the end of the execution of the permutation and also during the execution of the permutation.

Basic idea. The key idea for our software implementation of the ACE permutation is to split the state of the permutation among different registers for performing similar types of operations (e.g., SB-64). For instance, when eight parallel instances of ACE are evaluated using YMM registers, we pack data for SB-64 operation into six YMM registers and other blocks are stored in four other YMM registers. This allows us to perform the same operations in different registers to achieve efficiency in the implementation. Below we explain the bit-slice implementation details of ACE for YMM registers. The details for the SSE implementation using XMM registers are similar, and so are omitted.

Packing and unpacking for ACE. There are two different types of packing and unpacking operations in our implementation: 1) one pair is performed at the beginning and end of the permutation execution; and 2) the other one is performed at the beginning and end of the SB-64 layer in each step. We start by describing the first one. For the software implementation, we denote an ACE state by $S_i = s_0^i s_1^i s_2^i s_3^i s_4^i s_5^i s_6^i s_7^i s_8^i s_9^i$ where each s_j^i is a 32-bit word, $0 \leq i \leq 7$ and $0 \leq j \leq 9$. First, the eight independent states $S_0, S_1, S_2, S_3, S_4, S_5, S_6, S_7$ of ACE are loaded into ten 256-bit registers as follows.

$$R_0 \leftarrow s_7^0 s_6^0 s_5^0 s_4^0 s_3^0 s_2^0 s_1^0 s_0^0; \quad R_4 \leftarrow s_7^1 s_6^1 s_5^1 s_4^1 s_3^1 s_2^1 s_1^1 s_0^1;$$
$$R_1 \leftarrow s_7^2 s_6^2 s_5^2 s_4^2 s_3^2 s_2^2 s_1^2 s_0^2; \quad R_5 \leftarrow s_7^3 s_6^3 s_5^3 s_4^3 s_3^3 s_2^3 s_1^3 s_0^3;$$
$$R_2 \leftarrow s_7^4 s_6^4 s_5^4 s_4^4 s_3^4 s_2^4 s_1^4 s_0^4; \quad R_6 \leftarrow s_7^5 s_6^5 s_5^5 s_4^5 s_3^5 s_2^5 s_1^5 s_0^5;$$
$$R_3 \leftarrow s_7^6 s_6^6 s_5^6 s_4^6 s_3^6 s_2^6 s_1^6 s_0^6; \quad R_7 \leftarrow s_7^7 s_6^7 s_5^7 s_4^7 s_3^7 s_2^7 s_1^7 s_0^7;$$
$$R_8 \leftarrow s_9^3 s_8^3 s_9^2 s_8^2 s_9^1 s_8^1 s_9^0 s_8^0; \quad R_9 \leftarrow s_9^7 s_8^7 s_9^6 s_8^6 s_9^5 s_8^5 s_9^4 s_8^4;$$

Then the packing operation is defined as

$$\mathsf{PACK}(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9):$$
$$R_0 \leftarrow s_5^1 s_4^1 s_1^1 s_0^1 s_5^0 s_4^0 s_1^0 s_0^0; \quad R_4 \leftarrow s_7^1 s_6^1 s_3^1 s_2^1 s_7^0 s_6^0 s_3^0 s_2^0;$$
$$R_1 \leftarrow s_5^3 s_4^3 s_1^3 s_0^3 s_5^2 s_4^2 s_1^2 s_0^2; \quad R_5 \leftarrow s_7^3 s_6^3 s_3^3 s_2^3 s_7^2 s_6^2 s_3^2 s_2^2;$$
$$R_2 \leftarrow s_5^5 s_4^5 s_1^5 s_0^5 s_5^4 s_4^4 s_1^4 s_0^4; \quad R_6 \leftarrow s_7^5 s_6^5 s_3^5 s_2^5 s_7^4 s_6^4 s_3^4 s_2^4;$$
$$R_3 \leftarrow s_5^7 s_4^7 s_1^7 s_0^7 s_5^6 s_4^6 s_1^6 s_0^6; \quad R_7 \leftarrow s_7^7 s_6^7 s_3^7 s_2^7 s_7^6 s_6^6 s_3^6 s_2^6;$$
$$R_8 \leftarrow s_9^3 s_8^3 s_9^2 s_8^2 s_9^1 s_8^1 s_9^0 s_8^0; \quad R_9 \leftarrow s_9^7 s_8^7 s_9^6 s_8^6 s_9^5 s_8^5 s_9^4 s_8^4;$$

where the SB-64 operation is performed on $R_0, R_1, R_2, R_3, R_8,$ and R_9.

The unpacking operation, denoted by $\mathsf{UNPACK}()$, is the inverse of the packing operation, which we omit here. Both operations are implemented using `vpermd` and `vperm2i128`, `vpunpcklqdq` and `vpunpckhqdq` instructions. Assume that we wish to apply the SB-64 operation on disjoint 64 bits (i.e., $a_{2i+1}a_{2i}$ or $b_{2i+1}b_{2i}$) in the registers $A = a_7 a_6 a_5 a_4 a_3 a_2 a_1 a_0$ and $B = b_7 b_6 b_5 b_4 b_3 b_2 b_1 b_0$. As SB-64 adopts the Feistel structure, the data in A and B are regrouped for the homogeneity of operations in SB-64. For this, we need the second pair of packing and unpacking operations for the SB-64 layer, which is given by

$$\mathsf{PACK\_SB\text{-}64}(A, B): \qquad\qquad \mathsf{UNPACK\_SB\text{-}64}(A, B):$$
$$A \leftarrow b_6 b_4 b_2 b_0 a_6 a_4 a_2 a_0; \qquad A \leftarrow b_3 a_3 b_2 a_2 b_1 a_1 b_0 a_0;$$
$$B \leftarrow b_7 b_5 b_3 b_1 a_7 a_5 a_3 a_3 \qquad B \leftarrow b_7 a_7 b_6 a_6 b_5 a_5 b_4 a_4;$$

ROAX operation. We create an instruction for one round of execution of SB-64, denoted by ROAX, which is given by

$$\mathsf{ROAX}(A, B, q_1, q_2):$$
$$\mathsf{tmp} \leftarrow A; \quad C \leftarrow \texttt{0xfffffffe};$$
$$A \leftarrow (\mathsf{L}^5(A) \odot A) \oplus \mathsf{L}^1(A);$$
$$A \leftarrow A \oplus B \oplus (C \oplus q_1, C \oplus q_2, \cdots, C \oplus q_1, C \oplus q_2);$$
$$B \leftarrow \mathsf{tmp};$$

where A and B are either a XMM or YMM register, $\mathsf{L}^5(A)$ (resp. $\mathsf{L}^1(A)$) denotes the left cyclic shift by 5 (resp. 1) on every a_i in A, which is implemented using vpslld and vpsrld instructions.

Swapblock operation. With $R_0, R_1, \cdots, R_9$ as input, the swap block operation, denoted as SWAPBLKS, corresponding to $\pi = (3, 2, 0, 4, 1)$ is given by

$$\text{SWAPBLKS}(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9) :$$
$$R_0 \leftarrow s_1^1 s_0^1 s_7^1 s_6^1 s_1^0 s_0^0 s_7^0 s_6^0; \quad R_4 \leftarrow s_9^1 s_8^1 s_5^1 s_4^1 s_9^0 s_8^0 s_5^0 s_4^0$$
$$R_1 \leftarrow s_1^3 s_0^3 s_7^3 s_6^3 s_1^2 s_0^2 s_7^2 s_6^2; \quad R_5 \leftarrow s_9^3 s_8^3 s_5^3 s_4^3 s_9^2 s_8^2 s_5^2 s_4^2$$
$$R_2 \leftarrow s_1^5 s_0^5 s_7^5 s_6^5 s_1^4 s_0^4 s_7^4 s_6^4; \quad R_6 \leftarrow s_9^5 s_8^5 s_5^5 s_4^5 s_9^4 s_8^4 s_5^4 s_4^4$$
$$R_3 \leftarrow s_1^7 s_0^7 s_7^7 s_6^7 s_1^6 s_0^6 s_7^6 s_6^6; \quad R_7 \leftarrow s_9^7 s_8^7 s_5^7 s_4^7 s_9^6 s_8^6 s_5^6 s_4^6$$
$$R_8 \leftarrow s_3^3 s_2^3 s_3^2 s_2^2 s_3^1 s_2^1 s_3^0 s_2^0; \quad R_9 \leftarrow s_3^7 s_2^7 s_3^6 s_2^6 s_3^5 s_2^5 s_3^4 s_2^4;$$

The execution of the eight parallel instances of the ACE permutation is summarized in Algorithm 4.

Algorithm 4 Eight parallel instances of the ACE permutation

1: Input: $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$
2: Output: $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$

3: $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9) \leftarrow \text{PACK}(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$;
4: **for** $i = 0$ to 15 **do**:
5:      $R_0, R_1 \leftarrow \text{PACK\_SB-64}(R_0, R_1)$;
6:      $R_2, R_3 \leftarrow \text{PACK\_SB-64}(R_2, R_3)$;
7:      $R_8, R_9 \leftarrow \text{PACK\_SB-64}(R_8, R_9)$;

8:      **for** $j = 0$ to 7 **do**:
9:          $R_0, R_1 \leftarrow \text{ROAX}(R_0, R_1, rc_0^i[j], rc_1^i[j])$; $\triangleright rc_0^i[j] : j$-th lsb of rc_0^i
10:          $R_2, R_3 \leftarrow \text{ROAX}(R_2, R_3, rc_0^i[j], rc_1^i[j])$;
11:          $R_8, R_9 \leftarrow \text{ROAX}(R_8, R_9, rc_2^i[j], rc_2^i[j])$;
12:      **end for**
13:      $R_0, R_1 \leftarrow \text{UNPACK\_SB-64}(R_0, R_1)$;
14:      $R_2, R_3 \leftarrow \text{UNPACK\_SB-64}(R_2, R_3)$;
15:      $R_8, R_9 \leftarrow \text{UNPACK\_SB-64}(R_8, R_9)$;
16:      $C \leftarrow \text{0xffffff00}; D \leftarrow \text{0xffffffff}$;
17:      $\text{tmp0} \leftarrow (D, C \oplus sc_0^i, D, C \oplus sc_1^i, D, C \oplus sc_0^i, D, C \oplus sc_1^i)$
18:      $\text{tmp1} \leftarrow (D, C \oplus sc_2^i, D, C \oplus sc_2^i, D, C \oplus sc_2^i, D, C \oplus sc_2^i)$
19:      $R_4 \leftarrow R_4 \oplus \text{tmp0}; R_5 \leftarrow R_5 \oplus \text{tmp0}$;
20:      $R_6 \leftarrow R_6 \oplus \text{tmp0}; R_7 \leftarrow R_7 \oplus \text{tmp0}$;
21:      $R_8 \leftarrow R_8 \oplus \text{tmp1}; R_9 \leftarrow R_9 \oplus \text{tmp1}$;
22:      $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9) \leftarrow \text{SWAPBLKS}(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$;
23: **end for**
24: $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9) \leftarrow \text{UNPACK}(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$;
25: **return** $(R_0, R_1, R_2, R_3, R_4, R_5, R_6, R_7, R_8, R_9)$;

Benchmarking. We implement the ACE permutation and ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256 modes in C using SSE2 and AVX2 instruction sets and measure their performances on two different Intel processors: Skylake and Haswell. The codes were compiled using gcc 5.4.0 on 64-bit machines with the compiler flags -O2 -funroll-all-loops -march=native. For both implementations, we evaluate eight parallel instances and compute the throughput of the permutation and its modes. Table 7.1 presents the performance results in cycles per byte for both implementations where the message digest is computed for 1024 bits and encryption is also done for 1024 bits and the associated data length is set to 128 bits. In our implementation, we include the costs for all packing and unpacking operations. The best speed achieved is 9.97 cycles/byte for ACE, using the AVX2 implementation on Skylake.

Table 7.1: Benchmarking the results for the ACE permutation and its AE and Hash modes.

Primitive	Speed [cpb]	Instruction Set	CPU Name Spec.
ACE	15.66	SSE2	Skylake
	9.97	AVX2	Intel i7-6700
	16.96	SSE2	Haswell
	10.56	AVX2	Intel i7-4790
ACE-$\mathcal{AE}$-128	110.29	SSE2	Skylake
	68.53	AVX2	Intel i7-6700
	128.66	SSE2	Haswell
	89.10	AVX2	Intel i7-4790
ACE-$\mathcal{H}$-256	95.65	SSE2	Skylake
	58.81	AVX2	Intel i7-6700
	108.15	SSE2	Haswell
	66.12	AVX2	Intel i7-4790

7.2   Software: Microcontroller

We implement the ACE permutation and ACE-$\mathcal{AE}$-128 on two distinct microcontroller platforms. For ACE-$\mathcal{AE}$-128, we implement only encryption, as decryption is the same as encryption, except updating the rate with ciphertext. Our codes are written in assembly language to achieve optimal performance. We choose: 1) MSP430F2370, a 16-bit microcontroller from Texas Instruments with 2.3 Kbytes of programmable flash memory, 128 Bytes of RAM, and 12 general purpose registers of 16 bits, and 2) ARM Cortex M3 LM3S9D96, a 32-bit microcontroller with 524.3 Kbytes of programmable flash memory, 131 Kbytes of RAM, and 13 general purpose registers of 32 bits. We focus on four key performance measures, namely throughput (Kbps), code size (Kbytes), energy (nJ), and RAM (Kbytes) consumptions.

For ACE-$\mathcal{AE}$-128, the scheme is instantiated with a random 128-bit key and 128-bit nonce. Note that the throughput of the modes decreases compared to the permutation as the messages are processed on 64-bit blocks and $(5 + \ell)$(resp. $(4 + \ell)$) executions of the permutation are needed to evaluate the AE (resp. hash) mode where ℓ is the number of the processed data in blocks including padding if needed. Table 7.2 presents the performance of the ACE permutation and its modes.

Table 7.2: Performance of ACE on microcontrollers at a clock frequency of 16 MHz

Platform	Primitive	#AD blocks	#M blocks	Memory (bytes)		#cycles	Throughput	Energy/bit
				SRAM	Flash		[Kbps]	[nJ]
	ACE permutation	-	-	304	1456	69440	73.73	225
	ACE-$\mathcal{AE}$-128	0	16	330	1740	1445059	11.34	1461
16-bit MSP430F2370	ACE-$\mathcal{AE}$-128	2	16	330	1786	1582892	10.35	1600
	ACE-$\mathcal{H}$-256	-	2	330	1682	413056	4.96	3340
	ACE-$\mathcal{H}$-256	-	16	330	1684	1375672	11.91	1390
	ACE permutation	-	-	523	1598	13003	393.76	846
	ACE-$\mathcal{AE}$-128	0	16	559	1790	269341	60.83	5479
32-bit Cortex M3 LM3S9D96	ACE-$\mathcal{AE}$-128	2	16	559	1858	294988	55.54	6001
	ACE-$\mathcal{H}$-256	-	2	559	1822	77114	26.56	12550
	ACE-$\mathcal{H}$-256	-	16	559	1822	256524	63.87	5218

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Appendix A

Other NIST-LWC Submissions

In Table A.1, we list our other NIST-LWC submissions whose underlying permutation adopts a similar design as sLiSCP-light [6] family of permutations. ACE is an all in one primitive that utilizes a generalized version of sLiSCP-light with state size 320-bit and a different linear layer to offer both hashing and authenticated encryption functionalities. SPIX adopts sLiSCP-light-256 in a monkey duplex to offer higher throughput than generic Sponge-based AE schemes. SPOC is an authenticated cipher that enables higher bound on the underlying state size to offer same security as other generic AE schemes, thus allowing larger rate size. SPOC adopts sLiSCP-light-192 and sLiSCP-light-256 to enable different performance and hence different target applications. In Table A.1, the submissions are classified based on their functionalities, mode of operation parameters and hardware area in 65 nm ASIC.

Table A.1: Submissions with sLiSCP-light like permutations

Algorithm	Permutation	Functionality	Parameters (in bits)			Mode of operation	Area
			State	Rate	Security		[GE]
ACE-$\mathcal{AE}$-128 and ACE-$\mathcal{H}$-256	ACE	AEAD & Hash	320	64	128	Unified sLiSCP sponge	4250
SPIX [4]	sLiSCP-light-256	AEAD	256	64	128	Monkey Duplex	2611
SPOC-64 [3]	sLiSCP-light-192	AEAD	192	64	128	SPOC	2329
SPOC-128 [3]	sLiSCP-light-256	AEAD	256	128	128	SPOC	3054

Appendix B

Test Vectors

B.1   Simeck sbox

Test vector for Simeck sbox with input = 0000000000000000 and $rc = 0x07$.

Round	State
0	0000000000000000
1	FFFFFFFF00000000
2	FFFFFFFFFFFFFFFF
3	00000000FFFFFFFF
4	0000000100000000
5	FFFFFFFC00000001
6	FFFFFF9AFFFFFFFC
7	00000C2DFFFFFF9A
8	00001C1E00000C2D

B.2   ACE Permutation

Test vector for ACE with all zero state.

Table B.1: Test vector for ACE permutation

Step	State
0	0000000000000000 0000000000000000 0000000000000000 0000000000000000 0000000000000000
1	FFFFC7CAFFFFE776 00003C9E00001C3A 00001C1E00000C2D FFFFDBD4FFFFEB67 FFFFC361FFFFE36A
2	A008C151D9C4D9F0 25ACD9A124884ECC 86A59002FBFA4BCD D9528A87DDC179A3 DA531AC0DB77ADAA
3	446BFB17FEAC5A5F 683F3428F9654513 68637D8AD2D9A691 F55A0C1AF1B48501 B26C12762212F44E
4	5453CAE4EC2F4442 1229976DFAB4E931 62A32D3D4BF8A3A4 C3AAEBC356636242 85E95CBAFC2E53AF
5	598621C1B175FD21 2D4271827840D029 7067E7DBE7730CF1 EA4B2DD90065936F C09419107D0BC64B
6	F082FCB61529AA71 7BCFD42DFA4C3E52 2D5F0057B73ACCE3 3796D138A276F5D5 A9725A507DF3111B
7	FEFB14A90FFC6647 9F5776716E158260 8E92C0A5D6800B6F 47FF05347B0A9853 1B675DA36BA6435A
8	89F30BAF3692897B C4FDA6EBEC5A67C9 14F005716C4AFC2A DAFC0BEA21D2ED4A A4552F657DB01A48
9	4C23136992E442A3 011A48EC0CB5FB43 66FE8CDB3B4199E5 F0219458887736CA 3A1811F81F10637C
10	2610F06C195D5056 17AE4FD7BD09471B FFBDD5A7EAB46BCE 298CB1937B9E0DFB E94BF8C44E4343C5
11	C0DC927D4DB070E3 CF7763937E89CB5C 15839159A987CDA1 FCD3B2B79FA9B089 2726D3BB3C7F7307
12	EB0021C196A1BD2A 0430040EFF58D77D BC9CEE20225F9C0F AB4F7D562B579198 34B898627E2EE36E
13	6665A40D97687B80 5930C806DDEBC73A 61B46748C3F87266 AC9EBE137FC7980E A2FF33F7DD4CEFF9
14	AB3B18A05461271D 8E535FE0229BC4A8 3A17D3E8D0C0DEBE 3DB2755BFB6661D6 289C6819008FFCC9
15	9FE7E5EA42C1167A 637EA3CF659E1667 A7C2AFF4D71079A3 05973F456EB70EC1 12D203D0B8FA2D26
16	5C93691AD5060935 DC19CE947EAD550D AC12BEE1A64B670E F516E8BE1DFA60DA 409892A4E4CCBC15

B.3   ACE-$\mathcal{AE}$-128

Key	00111122335588DD 00111122335588DD
Nonce	111122335588DD00 111122335588DD00
Associated data	1122335588DD0011 1122335588DD00
Plaintext	335588DD00111122 335588DD001111
Ciphertext	F9362385DC213A07 CEFEF38C34CEFF
Tag	AE85154F0242F0E4 0F9ECA3FE696D7C6

B.4   ACE-$\mathcal{H}$-256

Message 335588DD00111122 335588DD001111

Hash   1676336AB5C04A1D 9225FB283172A757 A0637A6523127B83 EFC3E990BABBD2E6

Appendix C

Constants: Sequence to Hex Conversion

In this section, we show how to obtain hex values of the constants for $i = 0$. Note that the LFSR is reset to initial all-one state $(1, \ldots, 1)$ at the beginning of each ACE permutation. The example is captured in Table C.1. First column in the table represents the clock cycle, which corresponds to the round within the step. The next column is showing the current LFSR state in this clock cycle. The bits are written in the same pattern as states in Figure 5.2, without showing the three feedback bits. The third column is showing 10 sequence bits, composed of the three feedback bits, followed by the state bits: the top row shows the subsequence with correct indices and the bottom row their respective values. The last three bits in every row are used directly as round constant in every clock cycle. The 10-bit subsequence from clock cycle 7 is used directly as the step constant and interpreted as shown in Figure 5.3.

The HEX values for step $i = 0$, listed in Table 2.2 are obtained as follows:

- from the last three columns of Table C.1 for the round constants

- from the last row of Table C.1 for the step constants

as follows:

$$
\begin{array}{llllllll}
rc_0^0 & = & 00000111 & = & 0x07 & \qquad sc_0^0 & = & 01010000 & = & 0x50 \\
rc_1^0 & = & 01010011 & = & 0x53 & \qquad sc_1^0 & = & 00101000 & = & 0x28 \\
rc_2^i & = & 01000011 & = & 0x43 & \qquad sc_2^i & = & 00010100 & = & 0x14
\end{array}
$$

Table C.1: Generation of round and step constants for $i = 0$

clk. cycle	(current) LFSR state			(current) subsequence bits									
	1	1	1	a_9	a_8	a_7	a_6	a_5	a_4	a_3	a_2	a_1	a_0
0		1	1										
		1	1	0	0	0	1	1	1	1	1	1	1
	0	1	1	a_{12}	a_{11}	a_{10}	a_9	a_8	a_7	a_6	a_5	a_4	a_3
1		0	1										
		0	1	0	0	0	0	0	0	1	1	1	1
	0	0	1	a_{15}	a_{14}	a_{13}	a_{12}	a_{11}	a_{10}	a_9	a_8	a_7	a_6
2		0	0										
		0	0	0	0	1	0	0	0	0	0	0	1
	0	0	0	a_{18}	a_{17}	a_{16}	a_{15}	a_{14}	a_{13}	a_{12}	a_{11}	a_{10}	a_9
3		1	0										
		0	0	0	0	0	0	0	1	0	0	0	0
	0	0	0	a_{21}	a_{20}	a_{19}	a_{18}	a_{17}	a_{16}	a_{15}	a_{14}	a_{13}	a_{12}
4		0	1										
		0	0	0	1	1	0	0	0	0	0	1	0
	0	0	0	a_{24}	a_{23}	a_{22}	a_{21}	a_{20}	a_{19}	a_{18}	a_{17}	a_{16}	a_{15}
5		1	0										
		1	0	0	0	0	0	1	1	0	0	0	0
	0	0	0	a_{27}	a_{26}	a_{25}	a_{24}	a_{23}	a_{22}	a_{21}	a_{20}	a_{19}	a_{18}
6		0	1										
		0	1	1	0	1	0	0	0	0	1	1	0
	1	0	0	a_{30}	a_{29}	a_{28}	a_{27}	a_{26}	a_{25}	a_{24}	a_{23}	a_{22}	a_{21}
7		1	0										
		0	0	0	0	0	1	0	1	0	0	0	0

$\leftarrow sc_2^0, sc_1^0, sc_0^0$

$\uparrow \quad \uparrow \quad \uparrow$
$rc_2^0 \quad rc_1^0 \quad rc_0^0$