Entropy Sources Importance and testing

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Overview of the talk



Part I: Overview of NIST standards on random bit generation

Part II: Entropy estimation

Part III: Validation process

Part I: Overview of NIST Standards on Random Bit Generation

Cryptographic random number generation



Security of cryptographic primitives relies of the assumption that bits are generated uniformly at random and are unpredictable.

Designing random bit generators (RBGs) is challenging.

- Finding a robust randomness source and correctly extracting randomness
- Difficult to know how unpredictable the outputs are (i.e., estimating entropy)
- Difficult to statistically model the process
- Difficult to understand the effects of outside parameters and environmental conditions (e.g., humidity, temperature) on the source

Validating RBGs is challenging.

- Expert knowledge on the randomness sources
- Difficult to verify some of the claims
- Practical constraints (e.g., time)

NIST SP 800 90 Series



- Provides guidelines on how to construct RBGs that can be validated through FIPS 140.
- Aims to improve the quality of RBGs by specifying design principles, requirements.

The series consists of three parts:

- SP 800 90A Recommendation for Random Number Generation Using Deterministic Random Bit Generators (2015)
- SP 800 90B Recommendation for the Entropy Sources Used for Random Bit Generation (2018)
- SP 800 90C Recommendation for Random Bit Generator (RBG) Constructions (2022, 3rd draft)

SP 800 90A (2015)



Recommendation for random number generation using Deterministic Random Bit Generators

 Specifies mechanisms for the generation of random bits using deterministic methods based on hash functions and block ciphers.

Earlier versions: January 2012 and June 2006

Next steps: NIST is working on a new revision to align with the new revision of 90C.

NIST Special Publication 800-90A Revision 1

Recommendation for Random Number Generation Using Deterministic Random Bit Generators

Elaine Barker John Kelsey

This publication is available free of charge from: http://dx.doi.org/10.6028/NIST.SP.800-90Ar1

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SP 800 90B (2018)



Recommendation for the Entropy Sources Used for Random Bit Generation

- Provides an entropy source definition and a model.
- Specifies design principles and requirements for entropy source components.
- Includes entropy estimation techniques.

Earlier versions: August 2012 and January 2016

Next steps: NIST is planning to revise the standard based on the lessons learned during the validation testing.

NIST Special Publication 800-90B

Recommendation for the Entropy Sources Used for Random Bit Generation

Meltem Sönmez Turan Elaine Barker John Kelsey Kerry A. McKay Mary L. Baish Mike Boyle

This publication is available free of charge from: https://doi.org/10.6028/NIST.SP.800-90B

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SP 800 90C (2022)



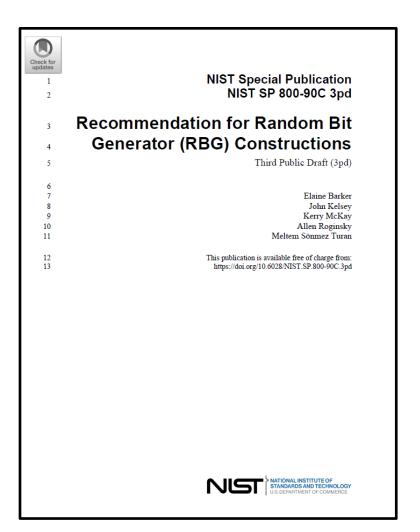
Recommendation for Random Bit Generator (RBG)
Constructions

Describes three RBGs constructions:

- RBG1 provides random bits from a device that is initialized from an external RBG.
- RBG2 includes an entropy source that is available on demand.
- RBG3 includes an entropy source that is continuously accessed to provide output with full entropy.

Earlier versions: August 2012 and April 2016.

Next steps: Third draft is published in September 2022. *Public comments due*: December 7, 2022



SP 800 22 (2010)



A Statistical Test Suite for Random and Pseudorandom Number Generators for Cryptographic Applications

• Specifies 15 statistical randomness tests and includes a software tool

Earlier version: August 2008 and October 2000.

Next steps:

Crypto publication review board recently completed the review of SP 800-22 and proposed to revise the standard to align with SP 800 90 series and to make technical improvements. NIST is working on Revision 2. National Institute of Standards and Technology Technology Administration

Special Publication 800-22

A Statistical Test Suite for Random and Pseudorandom Number Generators for Cryptographic Applications

Andrew Rukhin, Juan Soto, James Nechvatal, Miles Smid, Elaine Barker, Stefan Leigh, Mark Levenson, Mark Vangel, David Banks, Alan Heckert, James Dray, San Vo

Revised: April 2010 Lawrence E Bassham III

More info: https://csrc.nist.gov/projects/crypto-publication-review-project/completed-reviews

Aligning NIST and BSI standards



BSI (Germany) also has standards on random number generation:

- AIS 20: Functionality classes and evaluation methodology for deterministic random number generators
- AIS 31: Functionality classes and evaluation of physical random number generators

There are differences in the BSI's and NIST's validation process in terms of definitions, requirements, modeling and evaluation process.

NIST and BSI are jointly working to align the RBG standards, will publish a joint NIST-BSI report to explain the process.

Part II: Entropy Estimation

What do we mean by "entropy?"

We commonly use "entropy" to mean two things:

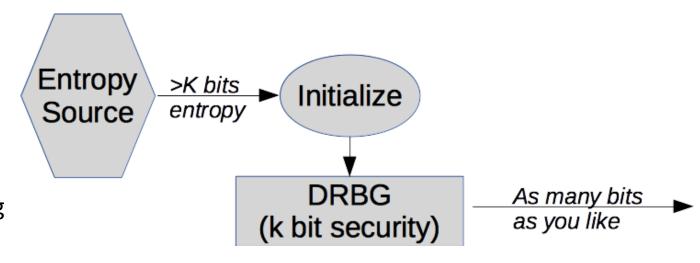
- A string of unpredictable bits
- A measure of how unpredictable the bits are
- We measure unpredictability by min-entropy
 - Consider the most powerful possible attacker trying to predict this string
 - P_{MAX} is prob of most likely output *given all possible attacker knowledge*

$$h_{min} = -lg(P_{MAX})$$

• In 90B, we get entropy from an entropy source

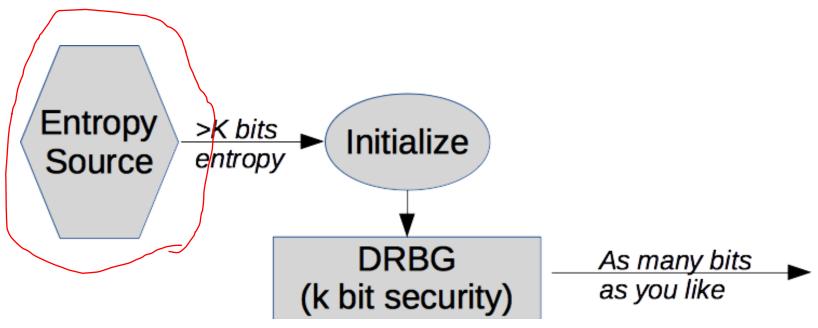
Big Picture: Entropy and SP 800-90

- We know how to build DRBGs
 - Deterministic algorithm
 - Published—attacker knows everything
 - Based on a cryptographic primitive



- The magic of a DRBG:
 - Takes an *unguessable* string.
 - Produces a string of indistinguishible-from-random output bits.
- What we need from Entropy Source:
 - String of bits
 - Known amount of entropy
 - Internal tests to make sure it's working

How Do We Build an Entropy Source?



- EVERYTHING in this picture is deterministic...
 - ...EXCEPT the **Entropy Source**
- Entropy Source:
 - Provides bitstrings with known amount of entropy
 - ...so we can initialize DRBG securely

SP 800-90B is all about building entropy sources.

How to Build an Entropy Source The SP 800-90B View

Noise Source

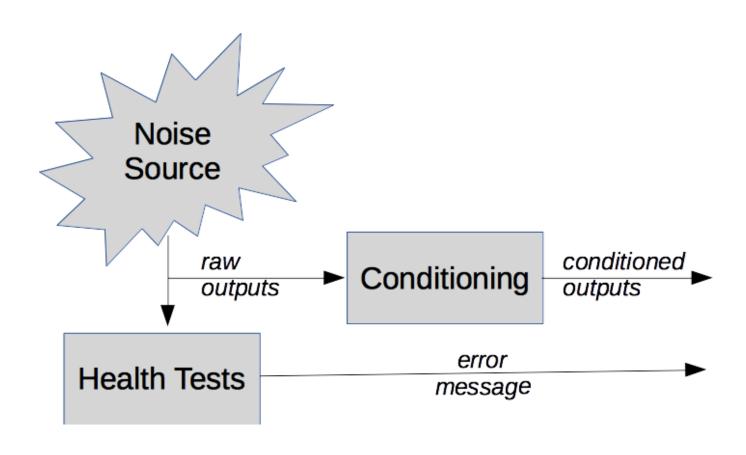
Where entropy comes from.

Health tests

Verify noise source still working correctly.

Conditioning

Optional processing of noise source outputs to improve statistics.



Reminder: An entropy source provides bitstrings with known entropy/sample

Two types of noise source

- Physical source
 - Purpose-built source of entropy
 - Unpredictibility based on some physical phenomenon
 - Should be simple enough to be modeled well
 - Examples:

Ring oscillators, metastable latches, noisy diodes, single-photon sources

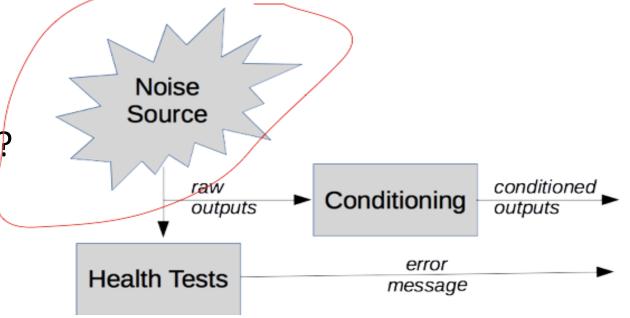
- Nonphysical source
 - "Found" source of entropy
 - Typically measured on a computer in software
 - Examples:

Interrupt timings, memory access timings, hard-drive access timing*

Estimating Entropy

How unpredictable is noise source?

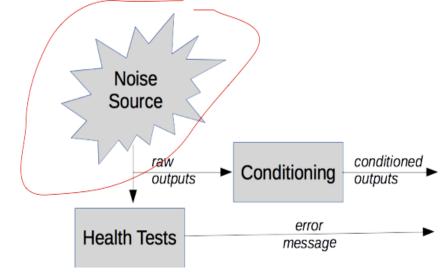
 We need a lower bound on: entropy per raw output



- Two ways to estimate this:
 - Modeling
 - Statistical testing / black box estimators
- We require both
- ...currently lean more on black-box estimators
- ...trying to move to more modeling of source

Statistical Testing/Black Box Estimation

- Requirement: RAW BITS from noise source
 - Need access to unprocessed bits from noise source
 - Not always easy to define exactly what "raw" is
 - Collect lots of data
- Tests and entropy estimate depends on whether source claims to provide iid data or non-iid data.



This works better as a sanity check than as a direct entropy estimate.

IID sources

- If the source is really well behaved....
 - Every output independent of all other outputs
 - Not varying over time
- ...then entropy estimation is very easy
 - We just count the most common output
 - Apply a binomial bound and we're done

Most sources are not iid

IID evaluation

• Source is only considered as iid if designer claims it

Complicated set of tests to try to falsify claim of iid

• IID claim must also be justified in report (reviewer must verify that this is a reasonable claim for this source)

• If accepted as an IID source, entropy estimation is simple

Non-IID sources

- Most sources are not IID
- Even if source passes IID tests, it may not be reasonable to assume independence of nearby outputs.

Non-IID track: throwing spaghetti at the wall

- Apply a large set of black-box entropy estimators to dataset
 - Each one makes different assumptions about source distribution
- Take the lowest estimate as the entropy estimate

Black box testing, cont'd

- We collect sequential and restart data
- Derive entropy estimates from each
- The result is generally pretty conservative...
- ...but it's also extremely ad-hoc.

- Black box testing without knowing internals of entropy source is not very powerful.
- Works best as a sanity check on estimate that comes from modeling source.

Modeling

 Start with complete understanding and description of source Noise
Source

Conditioning conditioned outputs

Health Tests

error
message

- Stochastic model
 - Build a model to describe source behavior
 - Estimate parameters of model
 - Derive upper bound on P_{MAX} from model
 - --> lower bound on h_{min}

NOTE: this is only practical for physical sources

- Less rigorous justification for nonphysical sources
 - Describe measured behavior and experiments
 - Justify existence of entropy

Questions about the noise source

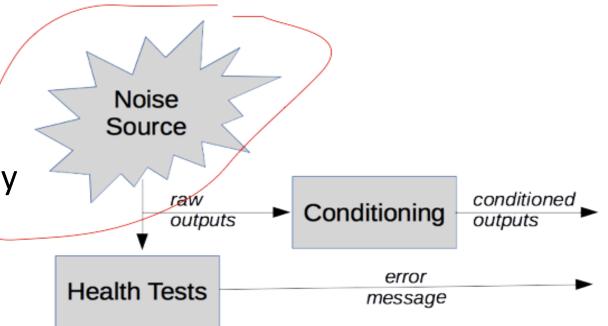
- How does the noise source work? (What's unpredictable about it?)

 "The operation of the noise source shall be documented..."
- Where does the unpredictability come from?
 - "...where the unpredictability comes from"
- How much entropy / output is produced?
 - "Documentation shall provide an explicit statement of the expected entropy provided..."
- How do you know? (Justify the entropy estimate.)
 - "...provide a technical argument for why the noise source can support that entropy rate."

Estimating Entropy: Summary

 We need to know how much entropy we're getting from noise source

- Two ways to do this:
 - Modeling
 - Statistical testing/black box estimation
- Questions to start with:
 - Where is the actual unpredictability coming from?
 - Can I quantify it?
 - ...at least a lower-bound?
- Black box estimators are a "sanity check," but can be badly wrong.
- Model estimate is better, assuming your model describes source well.



Part III: Validation

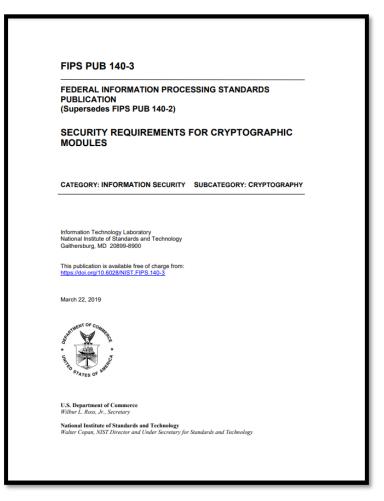
Validation Process



• In order to comply with Federal Information Processing Standards 140-3, all SP 800-90A DRBGs and SP 800-90B Entropy Sources must be validated.

 DRBGs are validated through the Cryptographic Algorithm Validation Program (CAVP)

 Entropy sources and RBG constructions* are validated through the Cryptographic Module Validation Program (CMVP)



DRBG Validation



Information Technology Laboratory

COMPUTER SECURITY RESOURCE CENTER



PROJECTS

CRYPTOGRAPHIC ALGORITHM VALIDATION PROGRAM

Cryptographic Algorithm Validation Program CAVP

f y

Implementation Name Crypto HAL-Core

The ADRF88xx/89xx is an RF System-on-Chip designed for use in energy storage applications.

2.2.5 Version FIRMWARE Type

Analog Devices Vendor

Lei Poo Contacts Corporate Headquarters 1-617-583-2384 Jonathan Simon One Analog Way Wilmington, MA 01887 1-510-400-2936

(781) 935-5565 1-800-262-5643

A2728 First Validated: 7/26/2022

Collapsed Expanded Aggregated

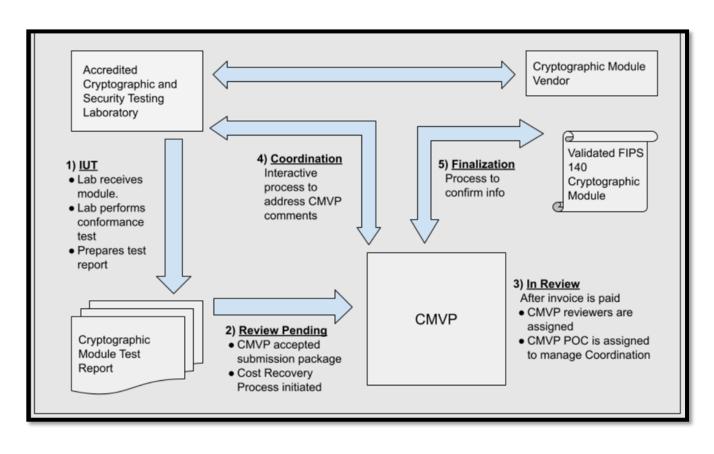
Operating Environment	Algorithm Capabilities
ARM Cortex M4F with ADRF8800/8900 Series Q	AES-CCM Q
ARM Cortex M4F with ADRF8800/8900 Series 🧕	Counter DRBG Q
	Prediction Resistance: No
	Supports Reseed
	Capabilities:
	Mode: AES-128
	Derivation Function Enabled: Yes
	Additional Input: 256
	Entropy Input: 312
	Nonce: 72
	Personalization String Length: 256

Entropy Source Validation



- Beginning 07 November 2020, entropy sources in FIPS 140-2 and FIPS 140-3 module submissions are required to be compliant to NIST SP 800-90B*
 - Previous submissions denoted "NDRNG" on validation certificate, met requirements in Implementation Guidance
- Until mid 2022, all entropy reports were submitted along with the module validation report
- Beginning mid 2022, Entropy Source Validation Test System (ESVTS) available for separate entropy source report submission

Entropy Source Review Process — With Module (until 01 Jan 2023)



- 1. Module includes entropy source (new reports tested to 90B). Same lab for both module and entropy report.
- 2. Separate cost for entropy will apply in the future.
- 3. Previously, module reviewers were also entropy reviewers. Now, dedicated entropy reviewers are assigned.
- 4. Entropy POC address entropy comments, while module POC address module comments. Both module and entropy comments are sent to the lab at the same time for each round.
- 5. Once finalized, module, inclusive of the entropy source (ENT) is validated and assigned a certificate number.

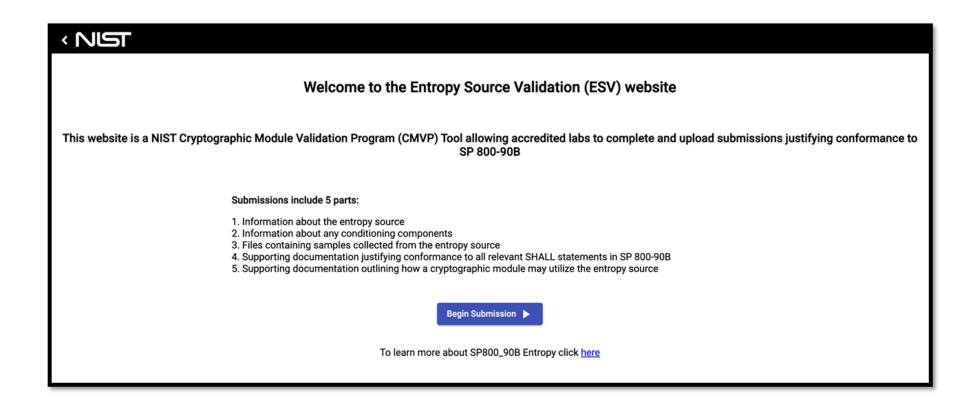
ESV Review Process (mandatory 01 Jan 2023)



- Decouple entropy source validation from module validation
- Lab submits raw noise, restart samples and any conditioned output sample data through ESVTS
 - SP 800-90B estimators run on ESV servers
- Reference ESV Cert in a similar manner to CAVP Certs
- Reuse validated entropy sources in multiple modules

ESV Web Client





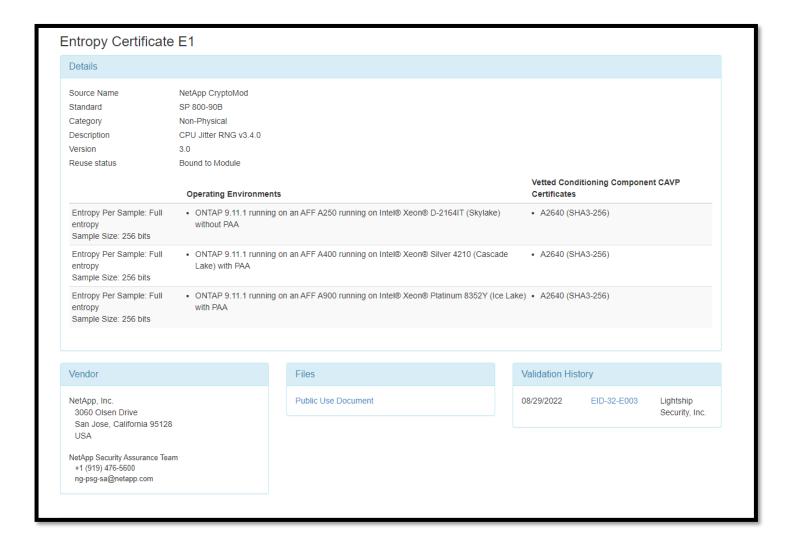
ESV Web Client



· NST							
1: 0	General Information						
Noi	ise Source Description						
Prin	mary Noise Source						
(64 c	character max)						
Bits	s Per Sample	Alphabet Size	IID:	○ True	False		
(Va	alid Values: 1 - 8)	(Valid Values: 2 - 256)	Physical:	True	○False		
	n-Entropy Estimate		ITAR:		False		
1			Additional Noise Source:	○ True	False		
Samj 0 Inva (Valid	alid value. Please correct.	Number of Restarts Olivalid value. Please correct. (Valid Values: > 1000)					
Imple O	ementation ID						
-							

First ESV Certificate Issued





Observations



- Entropy source validation is a review-intensive process
 - SP 800-90B estimators produce min-entropy estimate on collected data
 - 82 requirements (shall statements) in SP 800-90B
- Entropy report reviewers and lab staff need specialized technical background
 - Digital and analog circuits, semiconductor physics, information theory, stochastic processes
- 44 entropy sources validated to SP 800-90B up to September
 - 31 CPU Jitter (incl. Linux RNG)
 - 9 Oscillator(s)
 - 3 Other hardware
 - 1 Quantum source

Conclusion



- Generating random unpredictable numbers is hard.
- Many things can go wrong (unintentionally and intentionally)
- Standards/guidelines are useful, but they have limitations.
- A good understanding of the design is necessary to estimate entropy.

Development of guidelines on random number generation is an ongoing process.

Contact: <u>rbg_comments@nist.gov</u>