



Randomness Testing of the NIST Light Weight Cipher Finalist Candidates

Lightweight Cryptography Workshop 2022 Emanuele Bellini, Yun Ju Huang @ Tll



Contribution

- Propose a randomness test to all possible reduced rounds of the underlying primitives of NIST LW cipher candidates to analyze their randomness level.
- Make observation of these underlying primitives and provide a metric to compare how conservative is the choice of the number of rounds in each candidate.



Related Works - AES

NIST released the analysis of the Advanced Encryption Standard candidate algorithms with respect to some statistical properties in 2000. [Sot99 , BS00]







- 1. Avalanche Plaintext
- 2. Avalanche Key
- 3. Plaintext-Ciphertext correlation
- 4. Cipher Block Chaining Mode
- 5. Random
- 6. Low-Density with Plaintext
- 7. Low-Density with Key
- 8. High-Density with Plaintext
- 9. High-Density with Key





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Data generation

- 1. Avalanche Plaintext
- 2. Avalanche Key
- 3. Plaintext-Ciphertext correlation

4. Cipher Block Chaining Mode

- 5. Random
- 6. Low-Density with Plaintext
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P_{n+2} P_{ℓ} P_1 P_2 P_{n+1} .. 0 0 0 ... 1 0 0 ... 1 0 0 ... 0 1 0 ... 0 n bits n bits n bits n bits n bits random low density key K \rightarrow enc encencencenc.... \rightarrow ... n bits n bits n bits n bits n bits ciphertext C_{n+1} ciphertext C_{n+2} ciphertext C_{ℓ} ciphertext C_1 ciphertext C_2 low density sequence unit $n\ell$ bits low density sequence 1M bits 128 seqs ...

Experiments Setup

- 1. Avalanche Plaintext
- 2. Avalanche Key
- 3. Plaintext-Ciphertext correlation
- 4. Cipher Block Chaining Mode
- 5. Random
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- 7. Low-Density with Key
- 8. High-Density with Plaintext
- 9. High-Density with Key



NIST Statistical Tools

Using the tools provided on the NIST website

https://csrc.nist.gov/Projects/Random-Bit-Generation/Documentation-and-Software

| Statistical Test | No. of P-values | Test ID | Statistical Test | No. of P-values | Test ID |
|---------------------|-----------------|----------|------------------------------|-----------------|-----------|
| Monobit | 1 | 1 | Periodic Template | 1 | 157 |
| Block Frequency | 1 | 2 | Universal Statistical | 1 | 158 |
| Cusum | 2 | 3-4 | Approximate Entropy | 1 | 159 |
| Runs | 1 | 5 | Random Excursions | 8 | 160 - 167 |
| Long Runs of Ones | 1 | 6 | Random Excursions Variant | 18 | 168 - 185 |
| Rank | 1 | 7 | Serial | 2 | 186 - 187 |
| Spectral DFT | 1 | 8 | Linear Complexity | 1 | 188 |
| Aperiodic Templates | 148 | 9-156 | and an annual state of an an | | |

Table 1: Breakdown of the 188 statistical tests applied during experimentation.



Environment

- Currently, we generated total around 462 GB datasets for the test.
- The executing time of current result is 1 month.
- Running environment
 - Server 1 and 2: 16 Intel(R) Xeon(R) Gold 5222 CPUs, 4-cores, 3.80GHz, 252G RAM
 - Server 3: 112 Intel(R) Xeon(R) Platinum 8280 CPUs, 28-cores, 2.70GHz, 1152G RAM
- The dataset generation has been performed using the NumPy library and an independent non-optimized python implementation of each cipher.
- GRAIN-128 is excluded.
- CBC data of Spongent-pi is excluded.



Randomness Test Results

| NIST LW cipher | Underlying Primitives Permutation | Block Size | Key Size | Avalanche | | |
|---------------------|-----------------------------------|--|----------|--|--------------|--|
| | | | _ | Plaintext | Кеу | |
| | SPN-based I | Permutation | | | | |
| Ascon | Ascon's Permutation | 320 | - | 4 [6 , 12] | - | |
| | Dumbo: Elephant-Spongent-π[160] | 160 | - | 8 80 | - | |
| Elephant | Jumbo: Elephant-Spongent-π[176] | 176 | - | 8 90 | - | |
| | Delirium: Elephant-Keccak-f[200] | 200 | - | Avalanche Plaintext 4 [6,12] 8 80 8 90 3 18 4 [1,12] 3 [1,20] 3 12 4 12 3 [1,20] 3 12 4 12 3 [7,10] 3 [7,11] 3 [7,11] 3 [7,11] 3 [7,11] 3 [8,12] 17 [20,32] 17 [20,36] 17 [20,40] 8 40 | - | |
| ТСАР | Ascon's Permutation | 320 | - | 4 [[1 , 12] | - | |
| ISAF | Keccak-p[400] | 400 | - | Size Avalanche Plaintext - 4 [6,12] - 8 80 - 8 90 - 8 90 - 3 18 - 4 [1,12] - 3 [1,20] - 3 [1,20] - 3 [7,10] - 3 [7,11] - 3 [7,11] - 3 [8,12] 128 17 [20,32] 128 8 40 | - | |
| PHOTON-Beetle | PHOTON256 | 256 | - | 3 12 | - | |
| Xoodyak | Xoodoo | 384 | - | 4 12 | - | |
| | Sparkle256ns | 256 | - | 3 [7,10] | - | |
| SPARKLE | Sparkle384ns | 384 | - | 3 [7,11] | - | |
| (SCHWAEMM and ESCH) | Sparkle512ns | ion320-4 [6,12]-nt- π [160]160-8 80-nt- π [176]176-8 90-ak-f[200]200-3 18-ion320-4 [1,12]-400-3 1,20]-256-3 12-384-4 12-256-3 7,10]-256-3 7,10]-256-3 7,11]-521-3 8,12]-Keyed PermutationD2412812812817 20,36]21 20,328012825617 20,40]23 20,4SPN-based Block CipherTweakable Block Cipher | - | | | |
| | Keyed Per | cmutation | | | | |
| TinyJambu | TinyJambu-128 P1024 | 128 | 128 | 17 [20,32] | 19 [20,32] | |
| | TinyJambu-192 P1152 | 128 | 192 | 17 [20,36] | 21 [20,36] | |
| | TinyJambu-256 P1280 | 128 | 256 | Plaintext 4 [6,12] 8 80 8 90 3 18 4 [1,12] 3 1,20] 3 1,20] 3 1,20] 3 1,20] 3 1,20] 3 1,20] 3 1,20] 3 1,20] 1,10] 3 1,20] 1,10] 3 1,20] 17 1,20,32] 17 1,20,32] 17 1,20,36] 21 17 1,20,40] 23 8 40 7 40 | 23 [20,40] | |
| | SPN-based B | lock Cipher | | | | |
| GIFT-COFB | GIFT-128 | 128 | 128 | 8 40 | 10 40 | |
| | Tweakable B | lock Cipher | | | | |
| Romulus | skinny-128-384+ | 128 | 384 | 7 40 | 8 40 | |



Randomness Test Results

| | Underlying Primitiyes | Block Key | | Plaintext/Cinhertex | | | | |
|------------------------|----------------------------------|-----------|------|---------------------|--------------|--------------|--|--|
| NIST LW cipher | Permutation | Size | Size | t Correlation | CBC | Random | | |
| | | 5110 | 5110 | | | | | |
| SPN-based Permutation | | | | | | | | |
| Ascon | Ascon's Permutation | 320 | - | 1 [6,12] | 1 [6,12] | 1 [6,12] | | |
| Elephant | Dumbo: Elephant-Spongent-π[160] | 160 | - | 1 80 | - | 1 80 | | |
| | Jumbo: Elephant-Spongent-π[176] | 176 | - | 1 90 | - | 1 90 | | |
| | Delirium: Elephant-Keccak-f[200] | 200 | - | 1 18 | 1 18 | 1 18 | | |
| ISAP | Ascon's Permutation | 320 | - | 1 [1 , 12] | 1 [1,12] | 1 [1,12] | | |
| | Keccak-p[400] | 400 | - | 1 [1,20] | 1 [1,20] | 1 [1,20] | | |
| PHOTON-Beetle | PHOTON256 | 256 | - | 1 12 | 1 12 | 1 12 | | |
| Xoodyak | Xoodoo | 384 | - | 1 12 | 1 12 | 1 12 | | |
| CDADKIE | Sparkle256ns | 256 | - | 1 [7,10] | 1 [7,10] | 1 [7,10] | | |
| SPARKLE | Sparkle384ns | 384 | - | 1 [7,11] | 1 [7,11] | 1 [7,11] | | |
| (SCHWAEMM and ESCH) | Sparkle512ns | 512 | - | 1 [8,12] | 1 [8,12] | 1 [8,12] | | |
| Keyed Permutation | | | | | | | | |
| TinyJambu | TinyJambu-128 P1024 | 128 | 128 | 4 [20,32] | 4 [20, 32] | 1 [20, 32] | | |
| | TinyJambu-192 P1152 | 128 | 192 | 4 [20,36] | 4 [20,36] | 1 [20,36] | | |
| | TinyJambu-256 P1280 | 128 | 256 | 4 [20,40] | 4 [20,40] | 1 [20,40] | | |
| SPN-based Block Cipher | | | | | | | | |
| GIFT-COFB | GIFT-128 | 128 | 128 | 2 4 0 | 2 40 | 1 40 | | |
| Tweakable Block Cipher | | | | | | | | |
| Romulus | skinny-128-384+ | 128 | 384 | 1 40 | 1 40 | 1 40 | | |



Randomness Test Results

| NIST LW cipher | Underlying Primitives | Block Size | Key Size | Low Density | | High Density | |
|------------------------|---------------------------------------|------------|----------|-------------|------------|--------------|--------------|
| | Perindtation | | | Plaintext | Кеу | Plaintext | Кеу |
| SPN-based Permutation | | | | | | | |
| Ascon | Ascon's Permutation | 320 | - | - | - | - | - |
| | Dumbo: Elephant-Spongent-m[160] | 160 | - | - | - | - | - |
| Elephant | Jumbo: Elephant-Spongent- π [176] | 176 | - | - | - | - | - |
| - | Delirium: Elephant-Keccak-f[200] | 200 | - | - | - | - | - |
| телр | Ascon's Permutation | 320 | - | - | - | - | - |
| ISAF | Keccak-p[400] | 400 | - | - | - | - | - |
| PHOTON-Beetle | PHOTON256 | 256 | - | - | - | - | - |
| Xoodyak | Xoodoo | 384 | - | - | - | - | - |
| CDADZI E | Sparkle256ns | 256 | - | - | - | - | - |
| SPARALE | Sparkle384ns | 384 | - | - | - | - | - |
| (SCHWAEFFF and ESCH) | Sparkle512ns | 512 | - | - | - | - | - |
| Keyed Permutation | | | | | | | |
| TinyJambu | TinyJambu-128 P1024 | 128 | 128 | 14 [20,32] | 17 [20,32] | 14 [20,32] | 17 [20,32] |
| | TinyJambu-192 P1152 | 128 | 192 | 14 [20,36] | 17 [20,36] | 14 [20,36] | 17 [20,36] |
| | TinyJambu-256 P1280 | 128 | 256 | 15 [20,40] | 19 [20,40] | 14 [20,40] | 20 [20,40] |
| SPN-based Block Cipher | | | | | | | |
| GIFT-COFB | GIFT-128 | 128 | 128 | 7 40 | 9 40 | 7 40 | 8 40 |
| Tweakable Block Cipher | | | | | | | |
| Romulus | skinny-128-384+ | 128 | 384 | 6 40 | 8 40 | 6 40 | 8 40 |



Conclusion

We can see that most of the underlying primitives produce datasets which seem random in the first third of the total number of rounds. For the Spongent-pi this proportion is much higher, which seems to indicate a very conservative choice in the number of rounds of this cipher. Also, the schemes which using block ciphers as the underlying primitives also have parameter with higher rounds.

In some scheme, different rounds of the underlying primitives are used. Ascon and Sparkle family choose this parameters in more conservative way. On the other hand, we can see that in some cipher like ISAP and TinyJambu seems more aggressive to have some none random choice when doing the small task such as initialization or metadata encryption.

Reference

- [Sot99] Juan Soto. NISTIR 6390: Randomness testing of the advanced encryption standard candidate algorithms. NIST Internal or Interagency Reports, 1999
- [BS00] Lawrence Bassham and Juan Soto. NISTIR 6483: Randomness testing of the advanced encryption standard finalist candidates. NIST Internal or Interagency Reports, 2000.

For more details, please refer to the paper.



Q & A

