Update on the Security Analysis of Ascon

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> https://ascon.iaik.tugraz.at

The Ascon Family

Designed in 2014 [DEMS16]

- Published in Journal of Cryptology in 2021 [DEMS21c]
- **Q** Extensive published third-party cryptanalysis confirming its security margin
- ★ This talk: Overview of recent third-party cryptanalysis results & our own work on new security bounds [EME22]

	2014	2015	2016	2018 2019	2021	2022
CAESAR	Round 1	Round 2	Round 3	Finalists Portfolic)	
NIST LWC				Round 1 &	2 Finalists	

Ascon's Mode for Authenticated Encryption



- Doubly-keyed initialization/finalization for higher robustness under misuse
- Duplex sponge mode using a 5 × 64 = 320-bit permutation



ASCON Permutation: a = 12, $b \in \{6, 8\}$ Rounds



Linear layer



 $\begin{aligned} x_0 &:= x_0 \oplus (x_0 \Longrightarrow 19) \oplus (x_0 \ggg 28) \\ x_1 &:= x_1 \oplus (x_1 \ggg 61) \oplus (x_1 \ggg 39) \\ x_2 &:= x_2 \oplus (x_2 \ggg 1) \oplus (x_2 \ggg 6) \\ x_3 &:= x_3 \oplus (x_3 \ggg 10) \oplus (x_3 \ggg 17) \\ x_4 &:= x_4 \oplus (x_4 \ggg 7) \oplus (x_4 \ggg 41) \end{aligned}$

Analysis of Ascon

Key recovery	Ascon initialization	7 / 12	2 ⁹⁷ 🖉	Cube-like	[LZWW17]
	Ascon initialization	7 / 12	2 ¹⁰⁴ 🚬	Cube-like	[LDW17]
	Ascon initialization	7 / 12	2 ¹²³ 🗸	Cube	[RHSS21]
	Ascon initialization	6 / 12	2 ⁷⁴ 📐	Cond. HDL	[HP22]
	Ascon initialization	5 / 12	2 ³¹ 🗸	Difflinear	[Tez20]
	Ascon-128a iteration	7/8	2 ¹¹⁸ Ø	Cond. cube	[CKT22]
	Ascon-80pq iteration	6/6	2 ¹³⁰ 🖉 🗡	Cond. cube	[CHK22]
Forgery	Ascon-128 finalization	6 / 12	2 ³³ 🖉	Cube tester	[LZWW17]
	Ascon-128 finalization	4 / 12	2 ¹⁰² 🔀	Differential	[DEMS15]
	Ascon-128 finalization	4 / 12	2 ⁹⁷ 🔀	Differential	[GPT21]
	Ascon-128a finalization	3 / 12	2 ²⁰ 🗸	Differential	[GPT21]
-		- CA		120	

 \bigcirc = nonce misuse > = exceeds data limit of 2⁶⁴ blocks Z = time exceeds 2¹²⁸ weak-key variants omitted

Analysis of Ascon: (Partial*) state recovery

State recovery	Ascon-128 iteration	6/6	240 🖉	Cond. cube	[BCP22]
	Ascon-128 iteration*	6/6	2 ⁴⁵ 🖉	Cond. cube	[CHK22]
	Ascon-128 iteration	5/6	2 ⁶⁶ 🖉	Cube-like	[LZWW17]
	Ascon-128a iteration	7/8	2 ¹¹⁸ Ø	Cond. cube	[CKT22]
	Ascon-128a iteration	3/8	2117 🗸	Differential	[GPT21]
	Ascon-128a iteration	2/8	- 🗸	Sat-Solver	[DKM+17]

 \oslash = nonce misuse \gtrsim = exceeds data limit of 2⁶⁴ blocks

weak-key variants omitted

Analysis of Ascon-Hash and Ascon-Xor

Туре	Target	Output size	Rounds	Time	Method	Reference
Preimage	Ascon-Xof Ascon-Xof	64 64	6 / 12 2 / 12	2 ^{63.3} 2 ³⁹	Algebraic Cube-like	[DEMS19] [DEMS19]
Collision	Ascon-Xof Ascon-Xof Ascon-Hash Ascon-Hash	all 64 256 256	4 / 12 2 / 12 2 / 12 2 / 12 2 / 12	- 🕗 2 ¹⁵ 2 ¹²⁵ 2 ¹⁰³	Differential Differential Differential Differential	[DEMS19] [ZDW19] [ZDW19] [GPT21]

(🖉 = chosen IV)

Analysis of Ascon's Permutation

Distinguisher	Permutation	12 / 12	2 ⁵⁵ 👁	Zero-sum	[HP22]
	Permutation	11/12	2 ⁸⁵ 🕗	Zero-sum	[DEMS21a]
	Permutation	8/12	2 ⁴⁶	Integral	[HP22]
	Permutation	7 / 12	2 ⁶⁵	Integral	[Tod15]
	Permutation	7 / 12	2 ⁶⁰	Integral	[RHSS21]
	Permutation	7 / 12	2 ³⁴ 🕗	Limited-Birthday	[GPT21]
	Permutation	5/12	2 ¹⁰⁹	Truncated Differential	[Tez16]
	Permutation	5/12	2 ⁸⁰	Rectangle	[GPT21]
	Permutation	5/12	-	Zero-Correlation	[DEMS21a]
	Permutation	5/12	-	Impossible Differential	[DEMS21a]
	Permutation	4/12	2 ¹⁰⁷	Differential	[DEMS21a]
	Permutation	4/12	2 ¹⁰¹	Linear	[DEM15a]
	Permutation	3/12	-	Subspace Trails	[LTW18]

(= non-black-box distinguisher)

Analysis of Round-Reduced Ascon



Recent third-party analysis

Improvements to 7-Round Cube Attacks

Misuse-Free Key-Recovery and Distinguishing Attacks on 7-Round Ascon

Raghvendra Rohit¹, Kai Hu^{2,5}, Sumanta Sarkar³ and Siwei Sun^{4,6}

¹ Univ Rennes. Centre National de la Recherche Scientifique (CNRS). Institut de Recherche en

[RHSS21] slightly reduced the data complexity of 7-round attacks to stay below the limit of 2⁶⁴ blocks.

Diving Deep into the Weak Keys of Round Reduced Ascon

Raghvendra Rohit¹ and Santanu Sarkar^{2,3}

¹ Cryptography Research Centre, Technology Innovation Institute, Abu Dhabi, UAE

[RS21] investigated classes of "weak keys" which permit slightly better cube attacks for 7 rounds.

Refined Results for Differential Attacks



[GPT21] investigate the applicability of differential distinguishers for forgeries and collisions. Towards Tight Differential Bounds of Ascon

[MR22] find characteristics with fewer active S-boxes for 4 rounds (44 \rightarrow 43) and 5 rounds (78 \rightarrow 72).

(Higher-Order) Differential-Linear Distinguishers

Differential-linear Attacks on Permutation Ciphers Revisited: Experiments on Ascon and DryGASCON

Aslı Başak Civek^{®4} and Cihangir Tezcan^{®b} tics Institute, Department of Cyber Security, CyDeS Laboratory, Middle East Technical University, Ankara

[CT22] provide experiments on differential-linear cryptanalysis to refine previous results on 7 rounds. Revisiting Higher-Order Differential(-Linear) Attacks from an Algebraic Perspective Applications to Ascon, GRAIN v1, XOODOO, and ChaCha

Kai Hu and Thomas Peyrin

[HP22] investigate higher-order DL distinguishers and find 8-round permutation distinguishers in a dedicated setting and 6-round key-recovery attacks.

Other Distinguishers

Simplified MITM Modeling for Permutations: New (Quantum) Attacks

André Schrottenloher and Marc Stevens

Cryptology Group, CWI, Amsterdam, The Netherlands firstname.lastname@cwi.nl

Exploring Differential-Based Distinguishers and Forgeries for ASCON

David Gerault^{1,2}, Thomas Peyrin¹ and Quan Quan Tan¹

¹ Nanyang Technological University, Singapore, Singapore

[SS22a; SS22b] show that structural MitM attacks can find a fixpoint x = P(x) for up to 2.5 rounds with complexity 2²⁷².

[GPT21] find limited-birthday distinguishers up to 7 rounds.

Misuse Analysis of Ascon

Recent third-party analysis

Analysis of Ascon in Misuse Settings

- Cryptanalysis in standard settings has only lead to small improvements in the last years
- Cryptanalysts increasingly consider misuse settings:
 - Nonce misuse
 - Decryption misuse
 - Implementation attacks

Analysis of Duplex Sponges in Misuse Settings

Generic nonce-misuse attacks on duplex designs include

Confidentiality break

with 1 + 1 misuse query per block of the challenge message.

- State recovery with *D* misuse queries, $T \cdot D = 2^c$.
 - Does not lead to trivial key recovery in Ascon

With more massive nonce misuse, some dedicated attacks are possible:

Conditional Cube Attacks on Ascon in Misuse Settings

 $\begin{array}{c} \mbox{Practical cube-attack against nonce-misused} \\ \mbox{Ascon}^{\dagger} \end{array}$

Jules Baudrin, Anne Canteaut and Léo Perrin

Inria, France

[BCP22] find conditional cube attacks with nonce misuse for the full 6 encryption rounds of Ascon-128.

Ascon-80pq in a Nonce-misuse Setting

Donghoon Chang^{1,2}, Deukjo Hong^{1,3}, and Jinkeon Kang¹

A New Conditional Cube Attack on Reduced-Round Ascon-128a in a Nonce-misuse Setting

Donghoon Chang^{1,2}, Jinkeon Kang¹ and Meltem Sönmez Turan¹

[CKT22] find conditional cube attacks with nonce misuse for 7 of 8 round in Ascon-128A and a key-recovery attack.

 \blacksquare [CHK22] find similar results and KR attacks for Ascon-80pq (> 2¹²⁸).

Differential & Linear Cryptanalysis: New Bounds



ToSC 2022/1

Differential and Linear Characteristics of Ascon

- S-box has max. differential probability 2⁻², max. squared correlation 2⁻²
- Goal: Prove lower bound on number of active S-boxes of characteristics
- Weak alignment → proving bounds is challenging, need bitwise model



Gap of provable bounds vs. best known characteristics [DEMS15; DEM15b; GPT21]:



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Approach for SAT Model to Prove Bounds

Continuized SAT model

SAT encoding for characteristics by Sun et al. [SWW21; SWW18] Different counter encodings

Approach for SAT Model to Prove Bounds

Optimized SAT model

SAT encoding for characteristics by Sun et al. [SWW21; SWW18]
Different counter encodings

📥 Parallelization

- Solver-based [HKWB11; HFB20; BSS15; SS21]
- Ӯ Manual partitioning

O Partition the search space into many independent problems

- S Categorize characteristics based on "girdle patterns"
 - S-box activity within the round with fewest active S-boxes





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S Reduce the number of subproblems to be solved

Optimize the individual SAT models

Consider rotational symmetries

Use necklace theory to eliminate redundant checks [Mor72]



C Consider rotational symmetries

- Use necklace theory to eliminate redundant checks [Mor72]
- **T** Prefilter individual problems
 - Reduces model complexity



Consider rotational symmetries

- Use necklace theory to eliminate redundant checks [Mor72]
- **T** Prefilter individual problems
 - Reduces model complexity
- Pooling individual problems
 - Reduces overhead



New Bounds

- Single characteristic for 4-round Ascon
 - $\odot \ge$ 36 active S-boxes
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 - $\odot \ge$ 54 active S-boxes
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 - Outilizing intermediate results from our 4 round bound

New Bounds

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- Single characteristic for 6-round Ascon
 - $\odot \ge$ 54 active S-boxes
 - Runtime \approx 60 CPU days
 - Outilizing intermediate results from our 4 round bound
- Almost certainly not tight, but good enough to support trust in the permutation





Authenticated Encryption: Initialization and Finalization

- 12 round configuration
- Ample security margin for 128-bit security



Authenticated Encryption: Data processing

- Ascon-128: 6 rounds
- Ascon-128A: 8 rounds
- Data limit of 2⁶⁴ encrypted blocks
- Goal: Find better (tighter) 6-round bound



Ascon-Hash and Ascon-Xof

- Difficult to evaluate unkeyed modes based on probability
- Assumption: 2^{-128} (attempts) $\times 2^{-64}$ (degrees of freedom)



Ascon-Mac and Ascon-Prf [DEMS21b]

- Ascon-Mac, Ascon-Prf: 12 rounds
- Ascon-MacA, Ascon-PrFA: 8 rounds

Bounds for ISAP



- Scenario: Create collision based on 1-bit absorption
- For 1 to 4 rounds (consecutive bits), no solution exists
- For 5 rounds, collision-producing characteristic with 105 active S-boxes exists
- General bound: For 3+ final rounds in any collision-producing characteristic with 1-bit rate, there are at least 64 active S-boxes

Bounds for ISAP – 5-round characteristic



Conclusion

Ascon has received a lot of attention by cryptanalysts

- during CAESAR and during NIST LWC
- **Q** Main results: Optimizations of 7-round cube attack; Misuse attacks
- No cryptanalytic breakthroughs
- Improved bounds

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