Updates on Elephant

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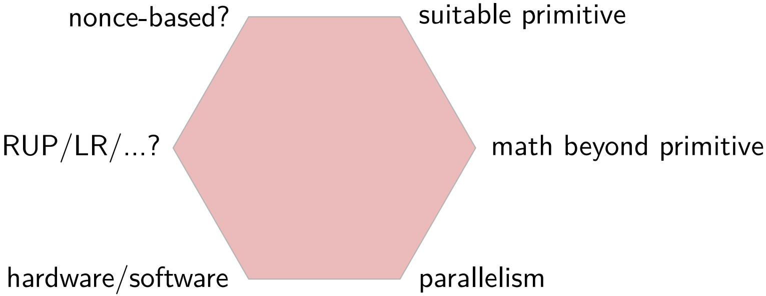
NIST Lightweight Cryptography Workshop 2020
October 19, 2020

Lightweight Authenticated Encryption



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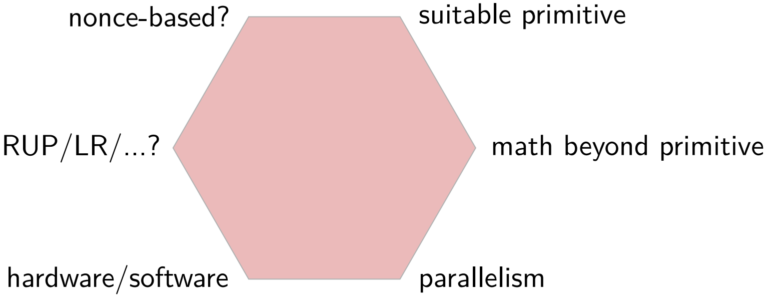


Our goal: minimize state size and complexity of design while still meeting expected security strength 2^{112} and limit on online complexity 2^{50} bytes

What Primitive?

Tweakable Block Cipher

Block Cipher

Permutation

What Primitive?

Tweakable Block Cipher

Block Cipher

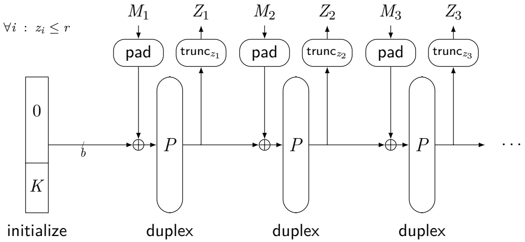
Permutation

Permutation is the best suited choice

What Mode?

Established Approach

- Keyed duplex/sponge [BDPV11,MRV15,DMV17]
- Inherently sequential



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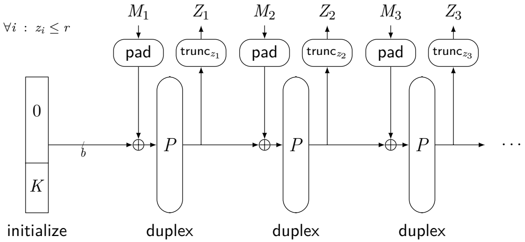
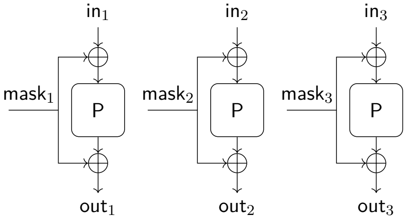


Our Approach

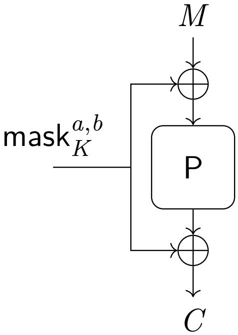
- Parallel evaluation of the permutation
  $\rightarrow$ requires proper masking
- Evaluating it in forward direction only
  $\rightarrow$ requires proper mode of use
- Goal: minimize permutation size



What Mask?

Simplified Version of MEM [GJMN16]

- φ_1 is fixed LFSR, $\varphi_2 = \varphi_1 \oplus \mathrm{id}$
- $\mathsf{mask}_K^{a,b} = \varphi_2^b \circ \varphi_1^a \circ \mathsf{P}(K \| 0^{n-k})$



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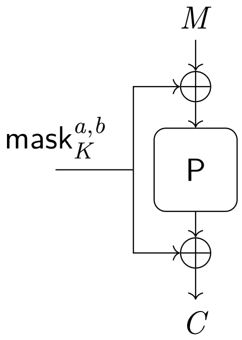
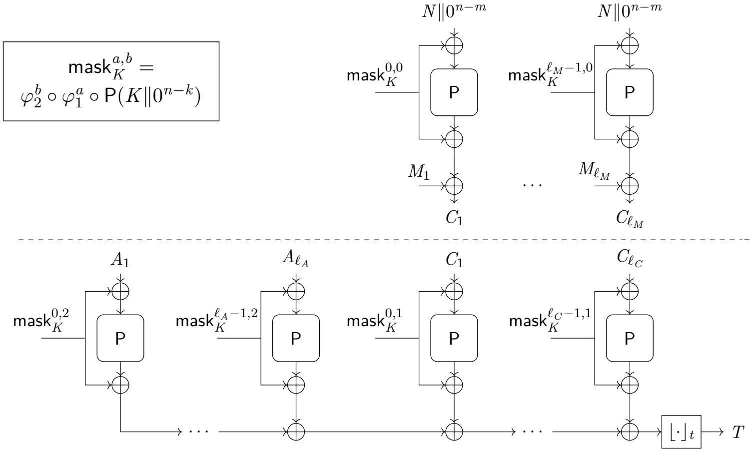


Features

- Constant-time
- Simple to implement
- More efficient than alternatives

Elephant Authenticated Encryption Mode

$$\mathsf{mask}_K^{a,b} = \varphi_2^b \circ \varphi_1^a \circ \mathsf{P}(K\|0^{n-k})$$



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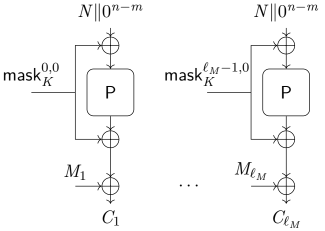
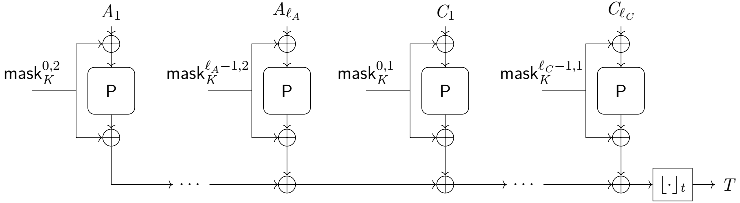


Encryption

- Nonce N input to all P calls
- K and counter in mask
- Padding $M_1 \dots M_{\ell_M} \xleftarrow{n} M$
- Ciphertext $C \leftarrow \lfloor C_1 \dots C_{\ell_M} \rfloor_{|M|}$



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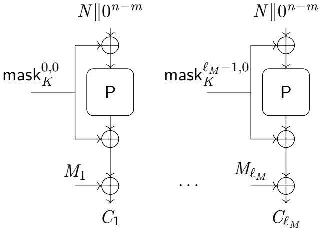

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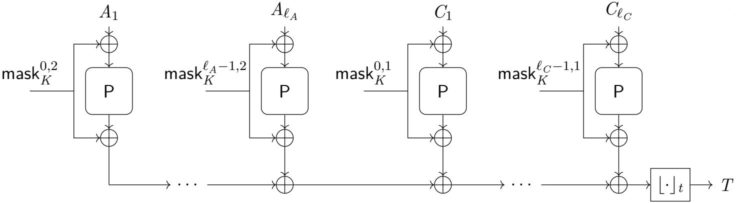
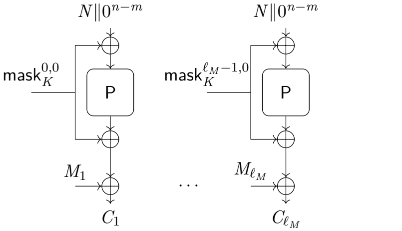


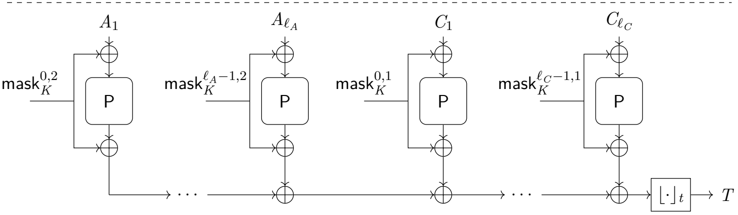
Authentication

- Padding $A_1 \dots A_{\ell_A} \xleftarrow{n} N \| A \| 1$
- Padding $C_1 \dots C_{\ell_C} \xleftarrow{n} C \| 1$
- K and counter in mask
- Tag T truncated to t bits

Elephant Authenticated Encryption Mode

$$\boxed{\mathsf{mask}_K^{a,b} = \varphi_2^b \circ \varphi_1^a \circ \mathsf{P}(K \| 0^{n-k})}$$





Mode Properties

- Encrypt-then-MAC
  - CTR encryption
  - Wegman-Carter-Shoup
- Fully parallelizable
- Uses single primitive P
- P in forward direction only

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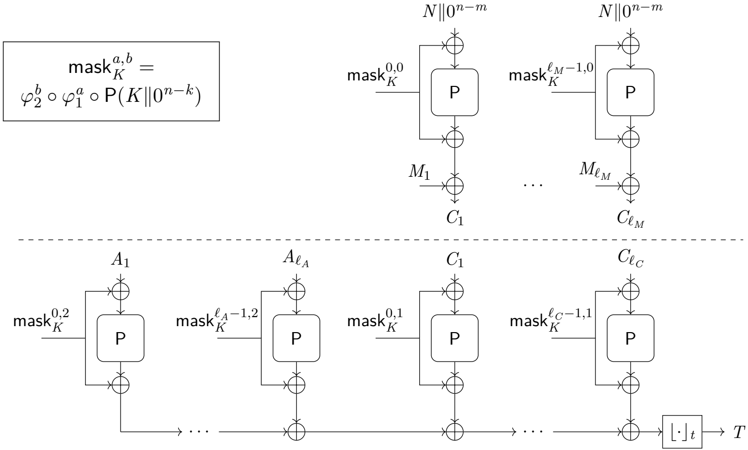

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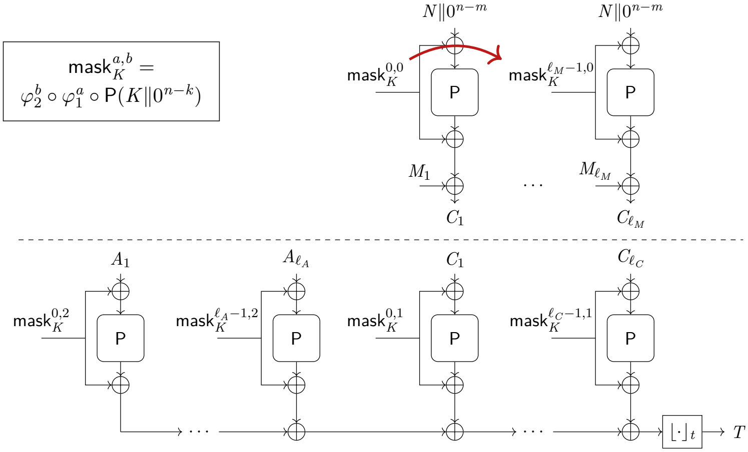

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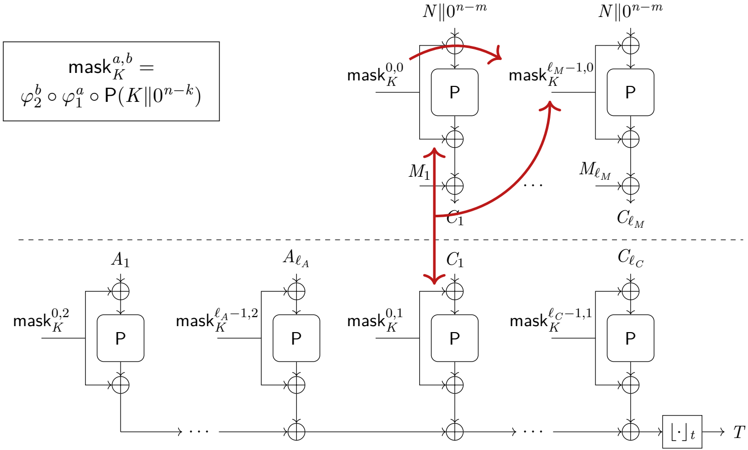

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- $\text{mask}_K^{i,0} = \varphi_1 \circ \text{mask}_K^{i-1,0}$
- $\text{mask}_K^{i-1,0} \oplus \text{mask}_K^{i-1,1} = \text{mask}_K^{i,0}$

Security of Mode

$$\mathbf{Adv}^{\mathrm{ae}}_{\mathsf{Elephant}}(\mathcal{A}) \lesssim \frac{4\sigma p}{2^n}$$

- σ is online complexity, p is offline complexity
- Assumptions:
  - P is random permutation
  - φ_1 has maximal length and $\varphi_2^b \circ \varphi_1^a \neq \varphi_2^{b'} \circ \varphi_1^{a'}$ for $(a, b) \neq (a', b')$
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Parameters of NIST lightweight call
can be met with a 160-bit permutation!

Instantiation

Dumbo

- Spongent-$\pi[160]$
- Minimalist design
  - Time complexity 2^{112}
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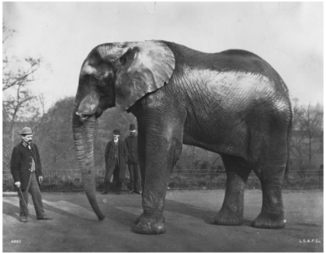

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- Spongent-$\pi[176]$
- Conservative design
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- ISO/IEC standardized

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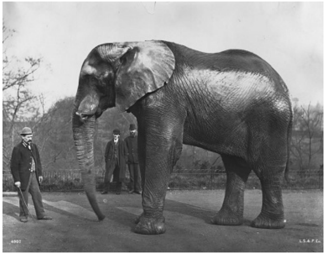

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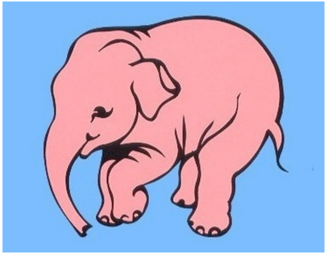


Delirium

- Keccak-$f[200]$
- High security
  - Time complexity 2^{127}
  - Data complexity 2^{70}
- Specified in NIST standard

Technical Specification of Instances

instance	k	m	n	t	P	φ_1	expected security strength	limit on online complexity
Dumbo	128	96	160	64	80-round Spongent-$\pi[160]$	φ_{Dumbo}	2^{112}	$2^{50}/(n/8)$
Jumbo	128	96	176	64	90-round Spongent-$\pi[176]$	φ_{Jumbo}	2^{127}	$2^{50}/(n/8)$
Delirium	128	96	200	128	18-round Keccak-$f[200]$	$\varphi_{\text{Delirium}}$	2^{127}	$2^{74}/(n/8)$

- All LFSRs operate on 8-bit words:

$$\varphi_{\text{Dumbo}} : (x_0, \dots, x_{19}) \mapsto (x_1, \dots, x_{19}, x_0 \lll 3 \oplus x_3 \ll 7 \oplus x_{13} \gg 7)$$

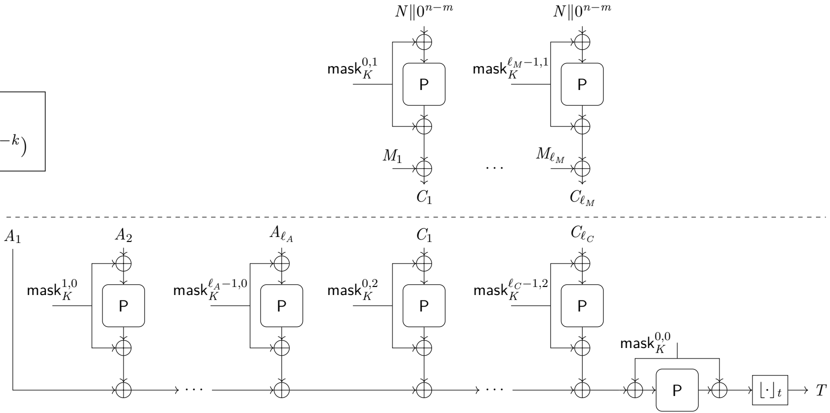
$$\varphi_{\text{Jumbo}} : (x_0, \dots, x_{21}) \mapsto (x_1, \dots, x_{21}, x_0 \lll 1 \oplus x_3 \ll 7 \oplus x_{19} \gg 7)$$

$$\varphi_{\text{Delirium}} : (x_0, \dots, x_{24}) \mapsto (x_1, \dots, x_{24}, x_0 \lll 1 \oplus x_2 \lll 1 \oplus x_{13} \ll 1)$$

- All have maximal length and $\varphi_2^b \circ \varphi_1^a \neq \varphi_2^{b'} \circ \varphi_1^{a'}$ for $(a, b) \neq (a', b')$

Tweak Proposal

$$\mathsf{mask}_K^{a,b} = \varphi_2^b \circ \varphi_1^a \circ \mathsf{P}(K \| 0^{n-k})$$



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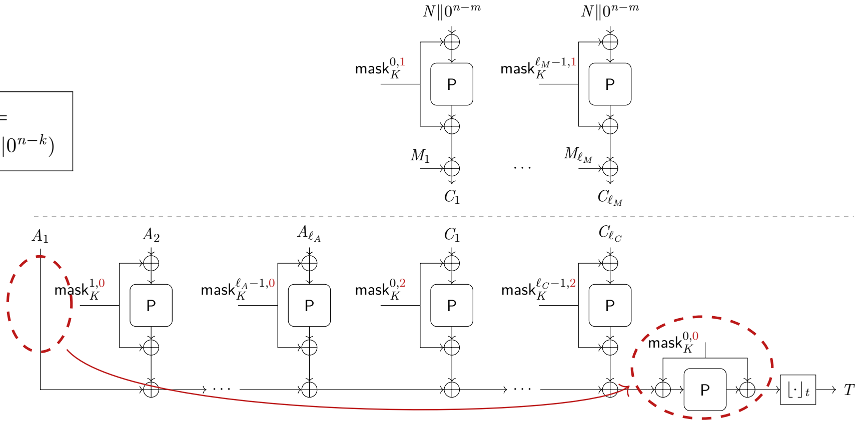

Changes to v1

- Authentication via protected counter sum
- Slight change in roles of mask parameters

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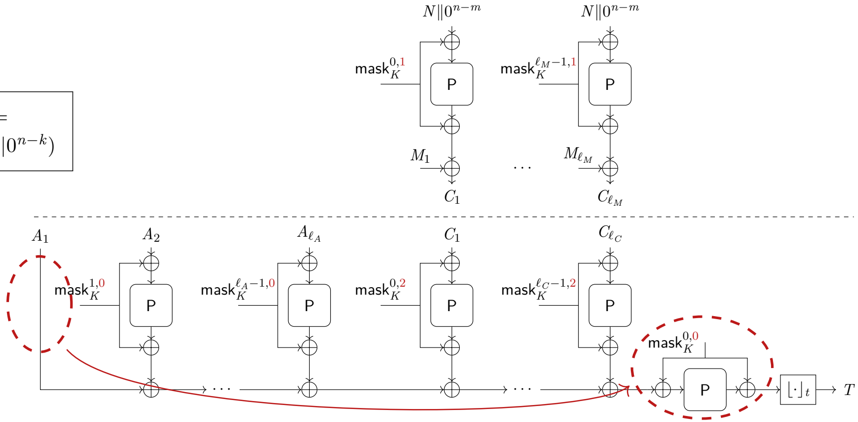

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Security and Efficiency

- v2 retains all good properties of v1
- Bonus: authenticity under nonce-reuse

Tweak Proposal: Security in a Nutshell

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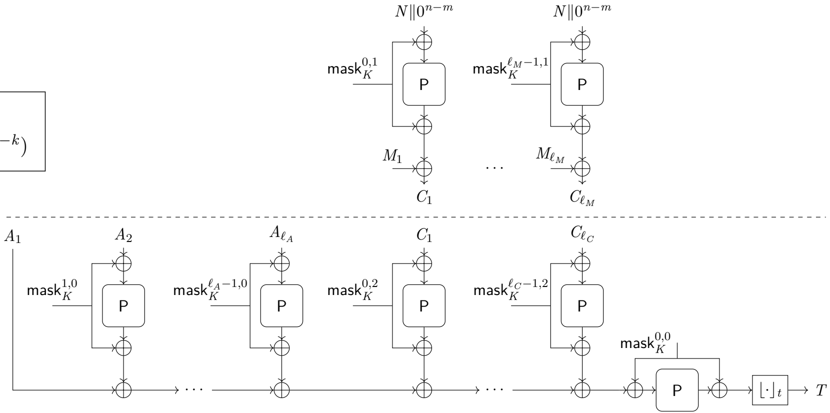

security	Elephant v1.1 confidentiality	Elephant v1.1 authenticity	Elephant v2 confidentiality	Elephant v2 authenticity
nonce-respecting	✓	✓	✓	✓
nonce-misuse	✗	✗	✗	✓

Implementation Update

- Implementations of Elephant can and should exploit parallelism so far only used in Delirium implementation of Campos et al. [CJL+20] (unoptimized Keccak-f)
- New parallel reference implementation for Delirium
  - Processes up to 8 blocks in parallel using modified Keccak-$f[1600]$ implementation
  - Speedup between 8 and 80 (depending on compilation options)
  - Other word sizes: same approach with different number of blocks

  `https://github.com/TimBeyne/Elephant`
- Dumbo and Jumbo
  - Hardware: exploit parallelism to achieve better trade-offs
  - Software: bitslicing (reuse techniques developed for Present and GIFT)

Conclusion

Elephant

- Parallel lightweight AE with small state
- Mode: provably secure in random permutation model
- Primitives: standardized and well-studied
- Dumbo and Jumbo for hardware
- Delirium for software

Thank you for your attention!