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# Overview and Considerations of Access Control Based on Attribute Encryption

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Vincent C. Hu	8
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17	Encryption
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#### 69 Abstract

- 70 Encryption technology can be incorporated into access control mechanisms based on user
- 71 identities, user attributes, or resource attributes. Traditional public-key encryption requires
- 72 different data to have different keys that can be distributed to users who satisfy perspective
- 73 access control policies along with the encrypted version of the data. However, some distributed
- or pervasive system environments wish to avoid the public-key encryption's all-or-nothing data
- 75 access limitation when considering their performance requirements. Attribute-based encryption
- incorporates access control policies and attributes with encryption and decryption functions and a
- one-to-many authorization scheme that requires fewer keys than public-key encryption. It also
   utilizes collusion-resistance, which provides a more efficient and flexible attribute-based access
- utilizes collusion-resistance, which provides a more efficient and flexible attribute-based access
   control mechanism that supports high-performance systems (e.g., cloud, IoT, disrupt-tolerant
- networks, wireless sensor networks, mobile ad-hoc networks, and public search service systems).

#### 81 Keywords

- 82 access control; attribute-based access control; attribute-based encryption; authorization;
- 83 encryptions; identity-based encryption; public-key encryption.

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#### 159 **Executive Summary**

- 160 Traditional public-key encryption (PKE) requires different data to have different keys that can be
- 161 distributed to users who satisfy access control policies along with the encrypted version of the
- 162 data. With user-specific keys, communication complexity is linear to the number of users, and
- 163 pre-distributed keys are neither bound to the attributes of users and data nor to the respective
- 164 access control policy. If access policies and/or attributes change dynamically (especially in real
- 165 time), keys need to change as well, which could cause inefficient performance in the system.
- 166 Combining cryptography with access control mechanisms can avoid the PKE's all-or-nothing
- 167 limitation of keys and improve performance. Encryption technology that is typically used for key
- 168 exchange, data signature, and certification can be incorporated into access control mechanisms
- 169 based on user identities, user attributes, and resource attributes.
- 170 Attribute-based encryption (ABE) incorporates access control policies and attributes into
- 171 encryption and decryption functions for public-key cryptography protocols through broadcasting.
- 172 Fewer keys are used for ABE than for traditional PKE, which allows it to be an efficient and
- 173 flexible attribute-based access control method.
- 174 The main features of ABE access control include:
- One-to-many authorization scheme
- Fine-grained access control based on user (subject) or resource (object) attributes
- Message sending without obtaining public key certificates from public key infrastructure
- Data decryption without evaluating permissions from access control policy
- Collusion-resistance so that a user who holds multiple keys cannot combine different keys to access a resource that is only allowed by one key
- 181 The fine-grained, efficient, and collusion-resistant features of ABE support the physical
- 182 resources and performance demands of systems like the cloud, IoT, disrupt-tolerant networks,
- 183 wireless sensor networks, mobile ad hoc networks, and public search service systems.

#### 184 **1.** Introduction

185 Traditional public-key encryption (PKE) requires different data to have different keys that -

along with the encrypted version of the data – can be distributed to users who satisfy access

187 control policies. With user-specific keys, the communication complexity is linear to the number

188 of users, and pre-distributed keys are neither bound to the attributes of users and data nor to the

189 respective access control policy. Therefore, if access policies and/or attributes change

- 190 dynamically (especially in real time), then keys need to change as well, which could cause the 191 system's performance to become inefficient [GOLIC]. Combining cryptography with access
- 191 system's performance to become memclent [GOLIC]. Combining cryptography with access 192 control mechanisms can help avoid the PKE's all-or-nothing limitation of keys and lead to more
- efficient performance. To that end, encryption technology that is typically used for key
- exchange, data signature, and certification can be incorporated into access control mechanisms
- 195 that are based on user identities, user attributes, and resource attributes.
- 196 Attribute-based encryption (ABE) [GPSW] incorporates access control policies and attributes
- 197 into encryption and decryption functions for public-key cryptography protocols through
- 198 broadcasting. ABE encrypts only once by using a public key according to attributes associated
- 199 with the access control policy. Only users hold the correct private decryption keys, which
- 200 satisfies the access policies for decrypting data. ABE's fine-grained access control mechanism is

201 based on user (subject) attributes or data (resource) attributes. Thus, the size of ABE encrypted

202 data and the resulting communication complexity for key distribution are linear in the number of

- attributes, not users. Broadcasting enables ABE to utilize fewer keys than traditional PKE
- schemes, which allows it to be an efficient and flexible attribute-based access control method.
- 205 The main features of ABE access control include:
- One-to-many authorization scheme
- Fine-grained access control based on user (subject) attributes or resource (object) attributes
- Message sending without obtaining public key certificates from public key infrastructure
- Data decryption without evaluating permissions from access control policy
- Collusion-resistance so that a user who holds multiple keys cannot combine different keys to access data that is only allowed by one key

These fine-grained, efficient, and collusion-resistant features support the physical resources and performance demands of systems like the cloud, the Internet of Things (IoT), disrupt-tolerant networks, wireless sensor networks, mobile ad hoc networks, and public search service systems [ELT, SW].

- 217 This document is organized as follows:
- Section 1 is the introduction.
- Section 2 provides an overview of the fundamental theories the ABE is built on,
   including elliptic-curve cryptography, bilinear pairing, and bilinear pairing for elliptic
   curve cryptography.
- Section 3 introduces identity-based encryption (IBE).

- Section 4 illustrates ABE algorithms of CP-ABE and KP-ABE.
- Section 5 describes considerations for applications of ABE from the perspectives of security, performance, access control policies, and support models.
- Section 6 is the conclusion.

#### 228 **2.** Fundamental Theories

229 The underlying function of ABE is primarily based on public-private key cryptography

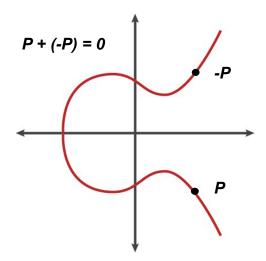
calculated in bilinear pairing on elliptic curve groups. This section outlines fundamental theories

- of elliptic curve, elliptic-curve cryptography, bilinear group, bilinear pairing, and elliptic-curve
- cryptography for ABE.

#### 233 2.1. Elliptic Curve

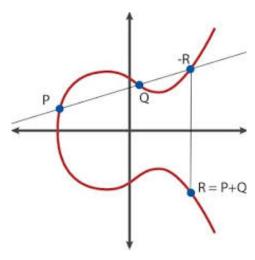
An elliptic curve is so named for being described by cubic equations (used for calculating the circumference of an ellipse), which is of the form  $y^2 = x^3 + ax + b$  ( $y^2 + axy + by = x^3 + cx^2 + dx + e$ ), where all the coefficients are real numbers that satisfy some simple conditions [ROBI, SP800-186]. However, elliptic curve is not an ellipse but rather a cubic ( $x^3$ ) formed by quadratic curves. Basic specifications for elliptic curve are:

- 2391. Single elliptic curve point at infinity or zero point are denoted by "0," which does not240satisfy an elliptic curve equation but is needed for addition as the additive identity, 0 = -0.241For any point P on an elliptic curve, P + 0 = P. All vertical lines intersect the curve at242infinity (0), and if three points on an elliptic curve lie on a straight line, their sum is 0.
- 243 2. The negative of a point *P* is the point with the same x coordinate but the negative of the y 244 coordinate of the elliptic curve's x-y coordinate. That is, if P = (x, y), then -P = (x, -y), 245 and these two points can be joined by a vertical line such that P + (-P) = P - P = 0, a 246 point adds negative of itself will become an infinity point (as shown in Figure 1). Any 247 non-vertical line will intersect the curve in three places at most [MATA].
- 248



**Fig. 1.** *P* + (-*P*) = *P* - *P* = 0 in an elliptic curve

- 251 3. Add distinct points P and Q in elliptic curve, if  $P \neq 0$  and  $P \neq Q$  (as shown in Figure 2),
- 252 where  $P = (x_P, y_P)$ ,  $Q = (x_Q, y_Q)$ . If  $R = P + Q = (x_R, y_R)$ , then  $x_R = s^2 x_P x_Q$  and  $y_R = -y_P$ 253  $+ s(x_P - x_R)$ , where  $s = (y_P - y_Q)/(x_P - x_Q)$ .
- 254



255 256

Fig. 2. P + Q in an elliptic curve

- 257 4. Doubling a point (also called *dot* function) P(P + P = 2P) uses P's tangent line to find 258 the second point in the curve, which will generate a new point -R and reflect -R from x 259 axis to give a new point R, such that from 3 above, if  $v_P \neq 0$ , 2P = R then replaces the O with P and replaces s with  $s = (3x_P^2 + a)/(2v_P)$  for the elliptic curve:  $v^2 = x^3 + ax + b$ . 260 Multiplying (also called dot, map, reflect) n (an integer) to a point P, X = nP means P + P261 262 +...+P (*n* times), the *nP* can be calculated by adding a doubling operation combined. 263 For example 5P = Double(Double P) + P (i.e.,  $2^2 + 1 = 5$ ). Note that for an elliptic curve point P, two integers n and m, m(n(P) = n(mP)), which is the same as the operation in a 264 finite field  $(g^{y})^{x} = (g^{x})^{y}$ , where g is an element in a finite field and x, y are integers. 265
- 266 5. Order of a point *P* on the elliptic curve is defined to be the smallest integer *n* such that nP267 = 0.
- 268 6. Elliptic curve cryptography (ECC) uses elliptic curves over a finite field.  $F_z$ : {0 ... z-1} is a set of points (x, y) that satisfy  $y^2 = x^3 + ax + b \mod z$ , where z is a prime number > 3, 269 and a, b, x,  $y \in F_z$ . For example, an elliptic curve  $y^2 = x^3 + 7 \mod 11$ , when x = 1,  $y^2 = 8$ 270 mod 11, but there is no real number y satisfy  $y^2 = 8 \mod 11$ . When x = 2,  $y^2 = (8 + 7) \mod 11$ 271  $11 = 4 \mod 11$ , y = 2, or y = 9 can satisfy the formula, so points (2, 2) and (2, 9) are in the 272 273 elliptic curve. When x = 3:  $y^2 = (27 + 7) \mod 11 = 1 \mod 11$ , y = 1 or 10. Continually, we conclude that points (2, 2), (2, 9), (3, 1), (3, 10), (4, 4), (4, 7), (5, 0), (6, 5), (6, 6), (7, 3), 274 275 and (7, 9) are in the elliptic curve over the finite field defined by mod 11.

#### 276 **2.2.** Elliptic Curve Cryptography

Elliptic curve cryptography (ECC) [SP800-56A, FIPS186-5] was invented by Neal Koblitz and 277 Victor Miller in 1985 [MMSC] and standardized in IEEE P1363a. The primary advantage of 278 279 using elliptic curve-based cryptography is that ECC has shorter key/parameter than RSA's PKE 280 to achieve the same security strength. [MY]. This property addresses performance issues for 281 systems such as wireless communication devices, smart cards, web servers, and applications that 282 need to handle many encryption sessions at the same time. These systems need security but lack 283 the power, storage, or computational capability required for RSA's PKE cryptographic scheme. 284 For example, Bitcoin and Ethereum use *secp256k1* elliptic curve to generate private and public

285 key pairs [MOBI] for their blockchain implementations. Discrete logarithm problem (DLP) (i.e., 286 given two points, P and Q on an elliptic curve, find an integer a such that Q = aP) on an elliptic 287 curve is hard. However, ECC is more difficult to explain when compared to traditional RSA's 288 PKE cryptographic scheme [ROBI]. As ECC gains popularity, more applications are using it, 289 such as Internet Key Exchange (IKE), TLS, Tor, iMessage, Bitcoin, and Ethereum [LXYS]. 290 The international consortium Standards for Efficient Cryptography Group (SECG) [DANI] 291 developed commercial standards for efficient and interoperable ECC. SECG published a 292 document with a recommend set of parameters referred by the tuple (p, a, b, G, n, h) called 293 Elliptic Curve Domain Parameters to describe an elliptic curve used for ECC, where p is a prime 294 number for defining the finite field such that  $F_p = \{0 \dots p-1\}, a \text{ and } b \text{ (are usually restricted by } b \text{ and } b$  $4a^3 + 27 + b^2 \neq 0$ ) are the coefficients of the elliptic curve equation  $v^2 = x^3 + ax + b$ . [SP800-186] 295 296 G is the generator point. n is the order of the G generator (base) point (also called n torsion 297 point), which determines the maximum value that can be turned into private key (ranging from 1 298 to n-1). h equals N/n called *cofactor* such that N is the order of the elliptic curve (the number of 299 points in the elliptic curve). For example, the finite field  $F_{37}$  with p = 37 for the elliptic curve:  $v^2$ 300  $=x^{3}-x+3 \mod 37$  (a = -1, b = 3) has order N = 42. For  $n = 7 \in \text{factors of } N \text{ in } \{1, 2, 3, 6, 7, 14, ...\}$ 21, 42}, we can decide the point P = (2, 3) is the base point G because  $P \neq 0, 2P \neq 0, 3P \neq 0, 6P$ 301 302  $\neq 0$ , but 7P = 0. According to Lagrange's theorem, the order of subgroup (generated by G) is a 303 factor of N. That is, N = nh. For any point P in the elliptic curve, NP = 0 (i.e., n(hP) = 0). Elliptic 304 curves defined by parameter sets have been given IDs in the standards for easier identification. For example, secp256k1 is EC  $y^2 = x^3 + 7$  (used by Bitcoin or Ethereum) [SP800-186, MOBI]. 305 For cryptographic usage, the elliptic curves are selected with a subgroup generated by the 306 307 generator point G such that the order is a prime and large enough for targeted security strength. 308 The steps are: 309 1. Select an elliptic curve pseudo randomly ((Note that ECC standards use recommended 310 curves with already defined subgroup and generator in C.3.1. in [SP800-186]). 311 2. Calculate the order N of the elliptic curve. (Schoof's algorithm [SCHOOF] can be applied 312 to find N, but it does not work for finding the order of a subgroup generated by a point.) 313 3. If N has a prime factor n, which is large enough to satisfy the required security strength, 314 go step 4. Otherwise, go to step 1. 315 4. Compute the cofactor h = N/n. 316 5. Choose a random point P as a candidate generator G on the curve. 317 6. Compute G = hP. 318 7. If G is 0 (i.e., the subgroup has order 1), then go back to step 4. Otherwise, G is the 319 generator (of a subgroup) with order *n* and cofactor *h*.

- Note that this algorithm only works if n is a prime. If n were not a prime, then the order of G could be one of the divisors of n [CORB].
- 322 In ECC, a point X = nG where *n* is an integer and *G* is the generator is used for the public key,
- 323 and *n* is used as the private key. For example, the message from the sender to the receiver with
- 324 the ciphertext  $C_m = \{KG, M + KP_{receiver}\}$  can be decrypted by function *Decrypt* ( $C_m$ ): M +
- 325  $KP_{receiver} S_{receiver}(KG) = M + K(S_{receiver}G) S_{receiver}(KG) = M$ , where M is the message converted

326 to an elliptic point, K is a random number, KG is a point in the elliptic curve, which can be 327 known by everyone sent through non-encrypted channel, Preceiver is the receiver's public key, 328  $S_{receiver}$  is the receiver's private key such that  $P_{receiver} = S_{receiver}G$ , and "+" is elliptic curve points 329 addition [ROBI]. ECC can also be applied to digital signature, for instance, The Elliptic Curve Digital Signature Algorithm (ECDSA): Assume that the private key Pr = d is an integer. The 330 331 public key Q = kG is an elliptic curve point. To sign a message *m*, compute e = H(m), where *H* is 332 a hash function and assume e is an integer such that  $1 \le e \le n$ . Randomly select an integer k,  $1 \le k$ 333 < n to compute  $R = kG = (x_R, y_R)$ , then convert finite field element  $x_R$  to an integer r, such that 1<334 r < n. Compute  $s = k^{-1}(e + r \cdot d) \mod n$ . The signature of m is (r, s). To verify the signature Sig(m)335 = (r, s), a verifier computes e = H(m). With the signature (r, s) and e, the verifier computes two values  $u = e \cdot s^{-1} \mod n$  and  $v = r \cdot s^{-1} \mod n$ , with u and v, computes an elliptic point  $R_1 = uG + vQ$ 336 337 =  $(x_{R'}, y_{R'})$ . After converting finite field element  $x_{R'}$  to an integer  $r_1$ , such that  $1 < r_1 < n$ . If  $r = r_1$ , 338 then (r, s) is a valid signature, otherwise, it is not a valid signature. As shown is the following 339 steps: 340 **Parameters** 341 342 G: a generator of the elliptic curve group over a finite field with order n, where n is a prime. 343 *d*: private key, an integer, 1 < d < n, 344 Q: public key, Q = dG = G + G + ... + G (d times) 345 346 Message to be signed 347 *m*: message to be signed. 348 349 Signing 350 1. Randomly select an integer k, 1 < k < n, compute  $R = kG = (x_R, y_R)$ 351 2. Convert finite field element  $x_R$  to an integer r, such that  $1 \le r \le n$ 352 3. Compute e = H(m), Here assumes that e = H(m) is an integer  $1 \le e \le n$ 353 4. Compute  $s = k^{-1}(e + r \cdot d) \mod n$ 354 5. Output (r, s) as the signature of m. 355 **Verifying** 356 1. Compute e = H(m)2. Compute  $u = e \cdot s^{-1} \mod n$  and  $v = r \cdot s^{-1} \mod n$ 357 358 3. Compute  $R_1 = uG + vQ = (x_{R'}, y_{R'})$ 359 4. Convert finite field element  $x_{R'}$  to an integer  $r_1$ , such that  $1 < r_1 < n$ 360 5. If  $r = r_1$ , then (r, s) is a valid signature.

#### **2.3. Bilinear Pair Mapping**

Based on elliptic curve, Bilinear Pairing Cryptography can be used for such as New Signature
[ST], Identity-based encryption (IBE) [BF], and Attribute-based Encryption (ABE) – by
applying bilinear pair mapping operations (i.e., bilinear pairing) on groups. For the consistency
of notation, from this point of document, we will use *G* to denote a group and elements in a

- 366 group will be denoted by letters in lower case. For instance, g to indicate a generator of G. In 367 general, a group is defined by a set of elements and an operation on the group. In Section 2.2, we
- introduced group consisting of points on an elliptic curve with operation addition "+". A prime
- 369 order subgroup with generator g is a cyclic group. That is, the group generated by g is  $\{0, g, 2g,$
- 370 ..., (n-1)g}, where *n* is the order of *G*. It can define a mapping from integer group  $\{0, 1, 2, ..., n-1\}$  to the cyclic group such that f(x) = xg. such that f(x + y) = xg + yg. For an integer *n*, a group is
- called a cyclic group of order *n*, if the group elements can be represented as  $\{0, g, 2g, ..., (n-1)g\}$ and ng = 0, where g is a generator. *G*.
- 575 and ng –0, where g is a generator. O.
- 374 Let  $G_1$  and  $G_2$  be cyclic groups of the same order (e.g.,  $G_1$  and  $G_2$  are cyclic additive groups
- 375 generated by g whose order is a prime n). The bilinear pairing is a computable function  $e: G_1 \times G_2$
- $\rightarrow G_T$  that associates pairs of elements from  $G_1$  and  $G_2$  with elements in groups  $G_T$ , which is a
- 377 group that contains the *n*th roots of unity [WF]. If (u, v) is a pair of elements such that  $u \in G_l$ , v
- 378  $\in G_2$  are points of  $G_1$  and  $G_2$ , respectively, then bilinear pairing function *e* takes *u* and *v* to 379 produce a value in Group  $G_T$ . Bilinear pairing has the following properties when *a*, *b*, *c*, *d*  $\in$  Z,
- 380 and  $u \in G_1$ ,  $v \in G_2$ , w is an element of  $G_1$  or  $G_2$ :
- 381 Computing e(u, v) is efficient.
- 382  $e(u, v)^a = e(u^a, v) = e(u, v^a)$
- 383  $e(u^a, v^b) e(u^c, v^d) = e(u, v)^{ab+cd}$  [QIAU]
- 384 e(u + w, v) = e(u, v)e(w, v)
- 385 e(u, w + v) = e(u, w)e(u, v)
- 386  $e(au, v) = e(u, av) = e(u, v)^{a}$  [HUBWIZ]
- 387 e(au, bv) = e(abu, v)
- 388  $e(-u, v) = e(u, v)^{-1} = e(u, -v)$
- 389 e(uw, v) = e(u, v)e(w, v)
- The mapping can also be  $G_1 \times G_1 \rightarrow G_T$ . In such cases, a pairing is called Symmetric: e(u, v) = e(v, u) for all u, v
- 392  $e(u^a, v^b) = e(u^b, v^a) = e(au, bv) = e(av, bu) = e(bu, av) = e(u, v)^{ab}$  when  $G_1 = G_2$ , and the 393 mapping is symmetric [BETH]
- Non-degenerate property  $e(u, v) \neq i$  identity for some u, v, which ensures that if nonidentical elements are selected for e, then the result of the pairing function will not be the identity of the target group. For example, assume 0 is the identity, then e(u, v) = 0 for all points v if and only if u = 0, and e(u, v) = 0 for all points u if and only if v = 0. Note that a degenerate property maps everything to the identity 0, that is  $\exists u \neq 0, v \neq 0, e(u, v) = 0$ .

- If  $e(u, u)^k = 1$ , then k is either 0 or a multiple of the order of the group when  $G_1 = G_2$ , and the mapping is symmetric [HUBWIZ].
- Skew-symmetric: e(u, v) = -e(v, u) when  $G_1 = G_2$ .

#### 402 2.4. Bilinear Paring for Cryptography

403Pairing-based cryptography [MD] applies bilinear pairing, which establishes the relationship404between cryptographic groups for solving Decisional Diffie Hellman problems. Weil and Tate405pairings [MEFF] were first used in an effort to break ECC. The idea was to reduce the discrete406logarithm problem in elliptic curves to a discrete logarithm problem in finite fields (called a407MOV reduction) [BETH]. Bilinear paring for ECC is based on the properties that add, double,408and multiply (Double means adding the same element, multiply with an integer k means adding409the same element k times) elliptic curve points to form an abelian group such that the bilinear

- 410 pairing  $e: G_1 \times G_2 \rightarrow G_T$  is defined by  $G_1, G_2$  are subgroups of points on elliptic curves over a
- 411 prime field  $F_p$ , and  $G_T$  is a subgroup of the multiplicative group of a finite field that contains the
- 412 *nth* (*n* is the order or the number of points in the elliptic curve) of unity in a prime field (usually
- 413 12 degrees of extension<sup>1</sup> of a prime field). These values are not points.  $G_1$ ,  $G_2$ , and  $G_T$  are all
- 414 isomorphic to one another since they have the same order and are cyclic [BUTE, MPPRRC,
- 415 IRON]. The bilinear pairing functions have the same properties as described in Section 2.3.
- 416 For this example, it is assumed that  $G_1$  and  $G_2$  are elliptic curve groups. But the notations are
- 417 different from the curves. It uses  $g_1$  as a point. It should be clear that private keys are integers.
- 418 Message M must be an element in  $G_T$ . By the way, here it is assumed that the operation in  $G_I$  and
- 419  $G_2$  are "addition" and in  $G_T$  "multiplication".
- 420 For public-key encryption, an EC key pair used for bilinear pairing is public key (PK) = private
- 421 key  $(SK)g_1$ , an integer, which means that the public key is just the private key times a fixed 422 generator point  $g_1$  in  $G_2$ . For example:
- 422 generator point  $g_1$  in  $G_1$ . For example:
- 423 1. *Alice* generates a key pair ( $SK_A$ ,  $PK_A$ ). *Bob* generates ( $SK_B$ ,  $PK_B$ ), and both public keys 424 are made available to public.
- 425 2. *Alice* can encrypt a message *M* to *Bob* by computing  $Me(PK_B, SK_Ag_2)$ , where  $g_2$  is a 426 generator point in  $G_2$ . Note that  $Me(PK_B, SK_Ag_2) = Me(SK_Bg_1, SK_Ag_2) = M e(SK_Ag_1, SK_Bg_2) = Me(PK_A, SK_Bg_2)$ .
- 428 3. Bob can recover M by computing  $Me(PK_A, SK_Bg_2) e(PK_A, -SK_Bg_2) = M e(PK_A, (SK_B-SK_B)$ 429  $g_2) = Me(PK_A, 0) = M.$
- 430 Note that *M* must be an element in  $G_T$ . And assumed that the operation in  $G_I$  and  $G_2$  are addition 431 and  $G_T$  is multiplication.
- 432 Bilinear pairing also works for message signatures. For example, *Alex* signs her message and
- 433 sends it to *Bob* such that *Alex* generates SKg = public key *PK*, signature C = SKH(M), where *SK*
- 434 is *Alex*'s secret key, g is the generator of elliptic curve that publicly known, M is the message
- 435 Alex signed, and H is a hash function for hashing message M to another point in the elliptic
- 436 curve. Bob receives C, PK, H(M) and then calculates to check if the pair mapping e of g and C

<sup>&</sup>lt;sup>1</sup> Numbers that consist of 12 different values between 0 and prime – 1 equivalent security of the degree extension of a 256-bit prime field are under 100 bits. [IRON]

- 437 equal the pair mapping of *PK* and *H*(*M*) for Alex's signature of *M*: e(g, C) = e(PK, H(M)) = e(g, C)
- 438 SKH(M) = e(SKg, H(M)) = e(PK, H(M)). If so, the signature is verified.
- 439 In addition to public-key encryption, bilinear paring is useful for functional encryption, which is
- 440 a generalization of public-key encryption in which possessing a secret key allows one to learn a
- 441 function of what the ciphertext is encrypting. It provides a mechanism for accessing the function
- 442 of the data without revealing actual data values. For example, if *Alice* wants to prove to *Bob* that
- she knew the answer of x + y without revealing the value of x and y, she can send  $xg_2$  and  $yg_2$  to
- 444 Bob, who then calculates  $A = e(g_1, xg_2)e(g_1, yg_2)$ , where  $g_1$  and  $g_2$  are generator points of elliptic
- 445 curve groups  $G_1$  and  $G_2$ . Since *Bob* knows the value of x + y, he can check whether  $e(g_1, g_2)^{x+y}$ 446 is equal to 4 to prove that *Alax* indeed knows the value of x and y [SUNDE DSW2011]
- 446 is equal to A to prove that Alex indeed knows the value of x and y [SHINDE, BSW2011, 447 DEW2012 DUCUL
- 447 BSW2012, BUCH].
- 448 Note that general ECC and bilinear pairing use <u>different curves</u>, based on <u>different security</u>
- 449 <u>assumptions</u>, and have <u>different trust models as listed in Table 1</u>.
- 450
- 451

 Table 1. Elliptic curve used for general ECC and bilinear pairing.

	General ECC	Pairing (IBE or ABE)
Elliptic curve	Often use pre-defined Montgomery Curves or Edward curves. They do not have small embedding degree. ECC cannot use supersingular curves.	Curves with embedding degree k, k is small to make it pairing friendly. It can use supersingular curves.
Security assumptions	Discrete logarithm or Computational/Decisional Diffie- Hellman	Bilinear Diffie-Hellman (BDH) Problem
Trust models	PKI, use CA as a trusted party but CA does not access private key	Parameters need to be certified by a trusted 3 <sup>rd</sup> party, e.g. PKI. The private key for each party is generated by a key generator which accesses everyone's private key.

452

#### 454 **3.** Identity-Based Encryption

- 455 Identity-based encryption (IBE) is a functional encryption proposed by Adi Shamir in 1984
- 456 [ADI] that requires a trusted key generator to publish a master public key and retains the
- 457 corresponding master private key (i.e., master key). The key generator allows any IBE user to
- generate a public key by combining the master public key with the user's identity value in text,
- 459 such as an email address, name, or home address. The key generator also uses the master private 460 key to generate the corresponding private key from the user's identity value. Thus, users may
- 460 key to generate the corresponding private key from the user's identity value. Thus, users may 461 encrypt messages sent to other users without the prior distribution of a public key to other users.
- 462 To decrypt or sign messages, the authorized user needs to obtain the appropriate private key from
- 463 the key generator.
- 464 The Boneh-Franklin IBE encryption scheme [BF] applies the Weil pairing on elliptic
- 465 curve over finite fields for setting up key management for public key and private key pairs from 466 user identities for encrypting and decrypting messages, as constructed in the following.
- 467 The bilinear pairing function  $e: G \times G \rightarrow G_T$ , g is the generator of G, and p is the order of G and 468  $G_T$ . The parameters are:
- 469 *Identity*  $I \in \{0, 1\}^*$  for message sender.
- 470 *Message*  $M \in \{0, 1\}^m$
- 471 Hash function  $H: \{0, 1\}^* \to G$
- 472 Extract function  $Q: G_T \rightarrow \{0, 1\}^m$
- 473
- 474 Functions include:
- 475 *Set up* () (by trusted key management server):
- 476 Return ( $msk = Random(Z_p)$ ;  $mpk = g^{msk}$ ). msk is the master secret key, which is for each 477 public key of each access control system. Random() generates a random number.
- 478 *Key generation(mpk, msk, I)* (by trusted key management server for message receiver):
- 479 Return  $sk = H(I)^{msk}$ ; sk is a private key for each identity.
- 480
- 481 *Encryption(mpk, I, M)* (for message sender):

482 
$$r = Random(Z_p); R = g^r; K = e(mpk, H(I)^r); W = Q(K) \oplus M; Return(R, W)$$

- 483
- 484 *Decryption(mpk, sk, R, W)* (for message receiver):
- 485 L = e(R, sk); Return  $M = Q(L) \oplus W$ ; because  $M = Q(L) \oplus Q(K) \oplus M$ , and L = K from the 486 following:
- 487  $L = e(R, sk) = e(g^r, H(I)^{msk}) = e(g^{msk}, H(I)^r) = e(mpk, H(I)^r) = K$ , where H() is a hash function. 488 (Assume  $H(I) = g^x$  for some x) [MIHIR].

- 489 Further, IBE offers the capability to encode additional information into identities. For example, a
- 490 sender can specify the expiration date of a message by appending a timestamp to the recipient's
- 491 identity (e.g., through some formal protocol like X.509). The receiver asks to retrieve the private
- 492 key from the key manager (usually the key generator), who can evaluate the identity and decline
- the request if the expiration date has passed. Generally, embedding information in the identity
- 494 provides an extra channel between the sender and the key manager with authenticity guaranteed
- in addition to the private key. The benefits of applying IBE can be demonstrated by an IBE emailsystem:
- Senders can send mail to recipients who have not yet set up a public key.
- When sending email, there is no need for an online lookup to obtain the recipient's certificate.
- Senders can send email that can only be read at some specified time in the future.
- The system can proactively refresh the recipient's private key for a short time
   period [BONEH].
- 503 Note that the key generator can access the encrypted data for any receiver. And the
- 504 communications between key generator and the receiver must be protected.
- 505

#### 506 **4.** Attribute-Based Encryption

507 Attribute-based encryption (ABE) stems from IBE and is an encryption scheme that combines 508 the principles of attribute-based access control [SP800-162] with the mechanisms of public-key 509 cryptography. ABE allows data owners and data consumers to encrypt and decrypt data based on 510 their attributes (e.g., organization, location, position), from which public and private keys are 511 derived through third-party key manager. ABE eliminates the need for public-key distribution 512 and certification, and the authenticity of the public keys is implicitly guaranteed as long as the 513 transport of the private keys to the corresponding user is secure. ABE is especially useful for the 514 system environment that requires pre-distribution of authenticated keys due to technical 515 limitations.

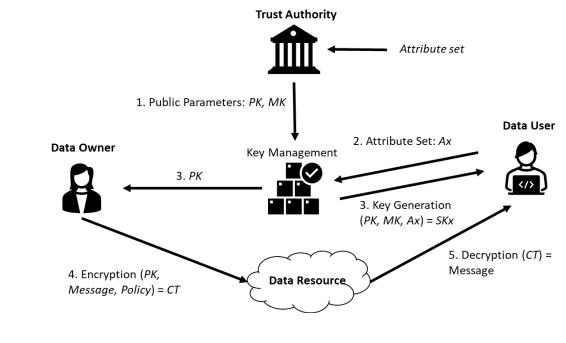
- 516 ABE has the following basic properties:
- Encryption time and ciphertext size are linear to the number of attributes involved.
- Collusion resistance means that it is impossible to decrypt any ciphertext for any new attribute set (CP-ABE) or new access policy (KP-ABE) by giving any number of randomized private keys.
- Randomized encryption prevents users from distinguishing repeated encryptions of the
   same message for privacy [GOLIC].
- 523 Popular distributed systems, such as cloud and IoT, make it possible for users to access dynamic
- 524 resources in flexible environments. However, their growth and the ubiquity of mobile devices for
- 525 data access have generated new security and performance challenges. Many studies have been
- 526 conducted on ABE, such as applying it to distributed systems [HL] for its one-to-many
- 527 cryptographic scheme as well as the capability to store, transmit, and retrieve high-dimensional 528 data with low computational time and high security. This shows that ABE can address security
- and privacy issues in outsourced and pervasive data access environments [ZDXSLZ]. For
- 530 example, for the large attribute universe of a cloud system. ABE allows data owner to compose
- access control policies based on their applications so that they can provide delegation capabilities
- to data users [BS]. However, the implementation of ABE requires complex support
- infrastructures including key generation services and data storing services to manage access
   structures and coordinate between clusters of users.
- 535 ABE is classified into two main schemes: Ciphertext-policy ABE (CP-ABE) [BSW2007] and
- 536 Key-policy ABE (KP-ABE) [GPSW]. Selective security<sup>2</sup> of CP-ABE is more suited to user
- 537 attributes, while adaptive (full) security of KP-ABE is more suited to data (resource) attributes
- 538 [GOLIC], as described in the following sections.

#### 539 4.1. Ciphertext-Policy Attribute-Based Encryption

- 540 CP-ABE [BSW2007] enables data owners to define their own access policies over the user
- 541 attributes and enforce those policies on data to be distributed. It provides a certain level of
- flexibility and scalability by removing the need for data owners to manage every individual
- 543 access request and maintains an access control policy instead. Encryption and decryption of CP-

<sup>&</sup>lt;sup>2</sup> For the challenger to private keys in the selective security model, the adversary has to commit the target attributes and declare the challengemessage (ciphertext) before public parameters are set up. The selective security model is weaker than the fully secure (adaptive) model, which has no restrictions as selective model, and both are given a public key, several secret keys, and one challenge ciphertext [WSOE].

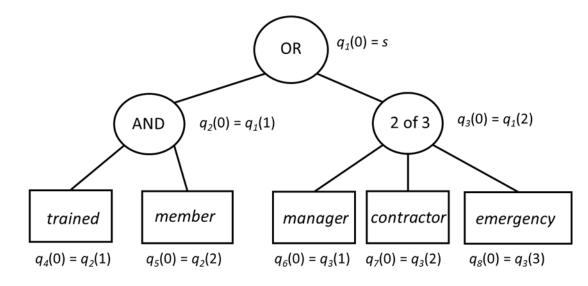
- ABE are based on the policy specified over the attributes so that a user can gain access to data if
- 545 they have appropriate attributes. For example, the attribute set {*student*, *professor*, *TA*, *RA*,
- 546 *registration*} contains attributes for student records. To encrypt *student records*, the school
- administrator specifies a policy rule: *professor* OR (*student* AND *TA*) OR *registration* for
- 548 permitting access to *student records*. Thus, users who have attribute sets {*professor*} or {*student*,
- 549 TA can decrypt *student records*, but users who have attribute sets {TA} or {*student*, RA} cannot.
- 550 CP-ABE is a useful scheme for addressing the risks associated with data security in a cloud
- system that needs key management and data storing services [MHH, BCSES] and to handle
- 552 costumers with complex attribute structures.
- 553 Figure 4 shows the basic process steps of a CP-ABE scheme:
- 1. A trust authority generates public key *PK* and master key *MK* according to the applied attribute set and sends them to the key management service.
- 556 2. To access data, requester x sends their attribute set Ax to the key management service.
- 557
  3. The key management service sends the public key *PK* to the data owner and generates
  558 secret key *SKx* for the data requester according to their attributes.
- 4. Using the public key, the data owner generates ciphertext *CT* for the data (*message*)
  based on the rules of their access control policy and then uploads the data to the data
  resource service.
- 562 5. The requester decrypts ciphertext *CT* from the resource service by using their secret key and attributes.
- 564



566 567

- Fig. 3. Basic process steps of CP-ABE scheme
- 568 The master secret key *MK* can decrypt all ciphertexts, which CP-ABE uses to derive user secret 569 keys associated with different attributes. Formally, global attribute set  $A = \{a_1...a_n\}$ , where  $a_1$ ,

- 570  $\dots$  an are attribute elements. User x has the attribute set  $A_x$ , which elements may or may not be in 571 A. Let B be the Boolean rule structure (i.e., access control policy). For example,  $B = a_1$  AND  $a_2$ 572 OR ( $a_3$  AND  $a_4$ ) for the data of a data owner. Note that the fundamental CP-ABE can only be 573 applied to the Boolean logic of a policy rule with a non-monochrome (i.e., including "NOT" gate) structure. Key generation function *Keygen* (*PK*, *MK*,  $A_x$ ) = *SK*<sub>x</sub>, where *PK* is the public key, 574 575 and *MK* is the master key. Decryption function *Decry* (*CT*, *SK*<sub>x</sub>) = *M*, where *CT* is the ciphertext, 576  $SK_x$  is the secret (private) key for the user x, and the message M is rendered if the function 577  $B(SK_x)$  checks the  $SK_x$  against the policy B is satisfied. Otherwise, M is NULL. Figure 5 shows 578 an example structure of the access control rule and demonstrates the CP-ABE's algorithms for 579 setup, encryption, key generation, and decryption functions.
- 580



581 582

Fig. 4. The tree structure of an example access control policy

#### 583 Setup function:

- 584 1. Master key MK = randomly chosen  $\alpha, \beta \in \mathbb{Z}_p$
- 585 2. Public key  $PK = (G, g, g^{\beta}, e(g, g)^{\alpha}, g^{\frac{1}{\beta}})$ , *G* is an elliptic curve group, *g* is the generator of 586 the elliptic curve,  $g^{\beta} = h$ , and  $g^{\frac{1}{\beta}} = f$  are for the delegation function (will not be discussed 587 in this document).
- 588 Encryption function:
- 5891. Let T be a tree representing an access structure as shown in Figure 5. Each non-leaf node590of the tree represents a threshold gate, described by its children and a threshold value. If n591is the number of children of a node x and  $k_x$  is its threshold value, then  $0 < k_x \le n$ . The592threshold value equals 1 for an OR gate (represented in a tree node of the Boolean593operator on the node's children in the rule structure) and equals n for an AND gate with n594elements or an n-out-of-m gate. Each leaf node x of the tree is described by an attribute595and a threshold value  $k_x = 1$ .

- 596 2. Choose a polynomial  $q_i$  for each node  $q_1, q_2, \dots, q_8$  for the tree structure that represents 597 the access permission paths in the access control policy, as shown in Figure 5. Set 598 Polynomial degree  $d_i(q_i)$  = Threshold value  $k_i(q_i) - 1$  for each node  $q_i$ . 599 3. Choose random s, such that root note  $q_R(0) = s \in Z_p$ , where p in Z is the order of the 600 group G. For each node  $q_i$ , set  $q_i(0) = q_i(n)$ , where  $q_i$  is the parent node of  $q_i$ , and n is the 601 sibling order from left to right. As shown in Figure 5,  $q_1(0) = s$ ,  $q_2(0) = q_1(1)$ ,  $q_3(0) = q_1(1)$ 602  $q_1(2), q_4(0) = q_2(1), q_5(0) = q_2(2), q_6(0) = q_3(1), q_7(0) = q_3(2), q_8(0) = q_3(3),$  and according to 1, and 2 above,  $q_1$  has degree 0,  $q_2$  and  $q_3$  has degree 1,  $q_4$ ,  $q_5$ ,  $q_6$ ,  $q_7$ , and  $q_8$ 603 604 has degree 0. 605 4. Encryption  $(M, T, PK) = CT = \{T, Me(g, g)^{\alpha s}, C = h^s, \text{ and for each leaf } q_x:$  $C_x = q^{q_x(0)}$ ,  $C_x' = H(l)q^{q_x(0)}$ , where x is the sibling order, and l is a string of one of a 606 607 leaf in T}. For example,  $C_4 = q^{q_4(0)}, C_4' = H("trained")q^{q_4(0)}$ 608  $C_5 = a^{q_5(0)}, C_5' = H("member")a^{q_5(0)}$ 609  $C_6 = g^{q_6(0)}, C_6' = H("manager")g^{q_6(0)}$ 610  $C_7 = q^{q_7(0)}, C_7' = H("contractor")q^{q_7(0)}$ 611  $C_8 = q^{q_8(0)}, C_8' = H("emergency")q^{q_8(0)}$ 612 Where *M* is the message (data), *T* is the access control policy tree of attributes, as shown 613 614 in Figure 5. e(, ) is a bilinear mapping function, and H() is a hash function mapping to a point in G. 615 616 **Key generation function:** Choose  $\gamma \in \mathbb{Z}_p$ , and for each attribute of a user, for example, a user has attributes:  $A = \{$ *"trained"*, 617 618 "manager", "contractor"}, choose  $\gamma_{trained}$ ,  $\gamma_{manager}$ ,  $\gamma_{contractor} \in \mathbb{Z}_p$ . Key generations  $(A, MK) = SK = \{D = g^{\frac{(\alpha+\gamma)}{\beta}}, D_l = g^{\gamma}H(l)^{\gamma_l}, D'_l = g^{\gamma_l}\}$  for all attributes the 619 620 user has. For example, 621  $D_{trained} = g^{\gamma} H("trained")^{\gamma} trained, D'_{trained} = g^{\gamma} trained,$
- 622  $D_{manager} = g^{\gamma} H("manager")^{\gamma_{manager}}, D'_{manager} = g^{\gamma_{manager}},$
- 623  $D_{contractor} = g^{\gamma} H("contractor")^{\gamma} contractor, D'_{contractor} = g^{\gamma} contractor,$
- 624 where l is the string of one of a leaf in T.
- 625 (Note: *MK* contains  $\alpha$ ,  $\beta$ )
- 626 **Decryption function:**
- 627 Recursively go through the tree *T* to call *DecryptNode* (*CT*, *SK*, *x*). If the node *x* is a leaf node
- 628 then we let i = att(x) is a string of one of a leaf in T and define as follows: If  $i \in S$  the set of all
- 629 attributes in the tree, then
- 630 DecryptNode (CT, SK, x) =

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631 
$$\frac{e(D_i, C_x)}{e(D'_i, C'_x)} = \frac{e(g^{\gamma}H(i)^{\gamma}i, g^{q_x(0)})}{e(g^{\gamma}i, H(i)^{q_x(0)})} = \frac{e(g^{q_x(0)}, g^{\gamma})e(H(i)^{\gamma}i, g^{q_x(0)})}{e(g^{q_x(0)}, H(i)^{\gamma}i)} = e(g, g)^{\gamma q_x(0)}$$
[MUKH].

- 632 Note that all leaves are attributes.
- 633 For example,

634 
$$\frac{e(D_{manager}, C_6)}{e(D'_{manager}, C'_6)} = e(g, g)^{\gamma q 6(0)} \text{ (Note that } e(g, g)^{\gamma q_1(0)} = e(g, g)^{\gamma s})$$

- 635 For any leaf, return  $\perp$  (false) if it is not an user attribute.
- 636 If a node x is a non-leaf node, the algorithm proceeds such that for all nodes z that are 637 children of x, it calls *DecryptNode*(*CT*, *SK*, z) and stores the output as  $F_z$  as following: 638 Let  $S_x$  be an arbitrary  $k_x$ -sized set of child nodes z such that  $F_z \neq \bot$ . If no such set exists, 639 then the node was not satisfied and returns  $\bot$ . Otherwise, compute:

640 
$$F_x = \prod_{z \in S_x} F_z^{\Delta_{i,S'x}(0)}$$
, where  $i = index(z)$  is the order number of the child. That is,  $S'_x = \{index(z), z \in S_x\}$ .

642 
$$= \prod_{z \in S_{\chi}} (e (g, g)^{\gamma q_{z}(0)})^{\Delta_{i, S'_{\chi}}(0)}$$

643 
$$= \prod_{z \in S_x} e(g,g)^{\gamma q_x(i)\Delta_{i,S'x}(0)} \text{ (i.e., } \prod_{z \in S_x} (e(g,g)^{\gamma q_x(index(z))})^{\Delta_{i,S'x}(0)} \text{ by construction)}$$

644 = 
$$e(g, g)^{\gamma q_x(0)}$$
 (using polynomial interpolation)

645 For example:  $i = index(z) \in \{1, 2, 3\}, z \in \{"manager", "contractor", "emergency"\}$ 

646 
$$F_{2of3} = F_{manager} \Delta_{1,(1,2,3)}(0) F_{contractor} \Delta_{2,(1,2,3)}(0) F_{emergency} \Delta_{3,(1,2,3)}(0)$$

$$647 = (e(g,g)^{\gamma.q_6(0)})^{\Delta_{1,(1,2,3)}(0)} (e(g,g)^{\gamma.q_7(0)})^{\Delta_{2,(1,2,3)}(0)} (e(g,g)^{\gamma.q_8(0)})^{\Delta_{3,(1,2,3)}(0)}$$

$$648 = e(g,g)^{\gamma(q_6(0)\Delta_{1,(1,2,3)}(0)+q_7(0)\Delta_{2,(1,2,3)}(0)+q_8(0)\Delta_{3,(1,2,3)}(0)}$$

649 
$$= e(g,g)^{\gamma.q_3(0)}$$

Note that Lagrange coefficient:  $\Delta_{i,s}(x) = \prod_{j \in S, j \neq i} \frac{x-j}{i-j}$ ,  $i \in Z_p$  and a set, *S*, of elements in  $Z_p$ . For example:

652 
$$\Delta_{I,(1,2,3)}(0) = \frac{0-2}{1-2} \frac{0-3}{1-3} = 3, \Delta_{2,(1,2,3)}(0) = \frac{0-1}{2-1} \frac{0-3}{2-3} = -3, \text{ and } \Delta_{3,(1,2,3)}(0) = \frac{0-1}{3-1} \frac{0-2}{3-2} = 1.$$
 So,

653 
$$q_6(0)\Delta_{1,(1,2,3)}(0) + q_7(0)\Delta_{2,(1,2,3)}(0) + q_8(0)\Delta_{3,(1,2,3)}(0)$$

654 = 
$$3q_6(0) - 3q_7(0) + q_8(0) = q_3(0)$$
 (i.e.,  $q_3(0) = 3q_3(1) - 3q_3(2) + q_3(3)$ .

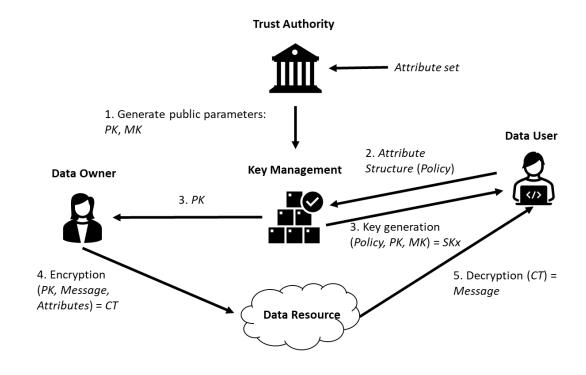
- 655 Since the algorithm started by simply calling the *DecryptNode* function on the root node *R* of the
- 656 tree *T*, if the tree is satisfied by *S*, then *DecriptNote* (*CT*, *SK*, *R*) =  $e(g, g)^{\gamma, q_R(0)} = e(g, g)^{\gamma, s}$ .
- 657 Then calculate the following to retrieve the message M (note that  $q_1 = q_R$ ,  $g^{\beta s} = h^s = C$ ) [KB, 658 BSW2007]:

659 
$$\frac{Me(g, g)^{\alpha s}}{\frac{e(g^{\beta s}, g^{\frac{\alpha+\gamma}{\beta}})}{e(g, g)^{\gamma s}}} = \frac{Me(g, g)^{\alpha s}}{e(g, g)^{(\alpha+\gamma)s-\gamma s}} = M$$

- 660 An increasing number of organizations and individual users store their private data in open
- resources, such as cloud storage, for sharing with others. Unlike traditional access control, the
- data owners prefer to define their own access control policy rather than be controlled by a
- 663 centralized access control policy. Thus, the data owners encrypt their data on the open resource
- according to their defined access control policy so as not to compromise it. CP-ABE provides
- appropriate solutions to meet data owners' needs because it enables data owners to define access
- 666 control policies and hide them by masking off attributes [HR].

# 667 4.2. Key-Policy Attribute-Based Encryption

- 668 Another variation of ABE scheme is the KP-ABE [GPSW], wherein access control policies are
- associated with keys, and data is associated with attributes such that secret keys (private keys)
- are generated based on an access requester's attributes in the form of an access control policy.
- 671 The ciphertext is labeled with a set of attributes so that decryption with a secret key works if and 672 only if an attribute set built in ciphertext satisfies the structure of the access policy of the
- 672 only if an attribute set built in ciphertext satisfies the structure of the acce673 requester. Note that attribute sets can vary with each encryption.
- 0/5 requester. Note that autibute sets can vary with each encryption.
- 674 Some access control models, such as multi-level and separation of duty security, are difficult to
- 675 represent with straightforward Boolean formulas. In such cases, defining KP-ABE schemes to
- 676 work with general Boolean circuits of attributes can be applied [TDN]. For example, to encrypt a
- 677 secret document with attributes "*project\_A*," "*project\_B*," and "*project\_C*," such that members 678 involved in project A project P OP project C and project A OP project D can decount the
- 678 involved in *project A*, *project B* OR *project C*, and *project A* OR *project D* can decrypt the 679 document, but members involved in *project A* AND *project D*, and *project A* AND NOT
- 680 project C cannot decrypt it.
- 681 Figure 6 shows the basic process steps of KP-ABE functions:
- 6821. The trust authority generates public parameters the public key *PK* and master key *MK* –683according to the applied attribute set and sends them to the key management service.
- 684
   685
   2. To access data, the requester *x* sends their attributes and access structure (policy) to the key management service.
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- 4. Data owners generate ciphertext for the data (message) based on the applied attribute set and public key *PK* and then upload the data to the data resource provider.
- 6915. The requester retrieves and decrypts ciphertext from the data source provider using their692secret key *SKx* and attributes associated with access structure.
- 693



694 695

696

Fig. 5. Basic process steps of KP-ABE scheme

697 In general, the size of the public key of KP-ABE is linear to the total number of applied attribute 698 sets. That is, the public key size is linear to the maximum number of attributes effectively used in 699 encryption. However, it can be a fixed size in a random oracle large universe construction with 700 hash function [GOLIC]. Using the example in Figure 5, instead of a policy structure of data, it 701 now represents an attribute structure of a data requester. The following demonstrates an example

702 of KP-ABE's algorithms of setup, encryption, key generation, and decryption functions.

#### 703 Setup function:

- Bilinear map function  $e: G_1 \ge G_2, G_1$  has prime order p, and g is a generator of  $G_1$ .
- 705  $U = \{a_1, a_2, \dots, a_n\}$  is a set of applicable *n* attributes. For this example,  $a_1 =$  "*trained*," 706  $a_2 =$  "*member*," ... from Figure 5.
- $t: U \to Z_p$ . Randomly choose  $t_1, t_2, \dots, t_n \in Z_p$  from  $G_1, t_x$  for attribute x in U.
- Master key *MK*: Random  $y \in \mathbb{Z}_p$ ,  $t_1$ ,  $t_2$ , ...  $t_n$  and  $Y = e(g, g)^y$

• Public key *PK*: *Y*, 
$$T_1 = g^{t_1}, T_2 = g^{t_2}, ..., T_n = g^{t_n}$$

- 710 **Encryption function:**
- 711  $Encrypt(M, \gamma, PK) = C = (\gamma, MY^s, T_i^s \quad \forall i \in \gamma)$ , where random  $s \in Z_p$ , message  $M \in G_2$ ,  $\gamma \subseteq U$ .
- For example,  $\gamma = \{$  "trained", "manager", "contractor" $\}$  for a user.
- 713 Key generation function:
- The algorithm is the same as CP- ABE, but it is applied to each data requester instead.
- 715 att(x): if x is a leaf node, then return the attribute associated with x

- 716 num(x): the number of children of a node x
- 717 K(x): threshold value,  $0 \le K(x) \le num(x)$
- 718 K(x) = 1, for an OR gate
- 719 K(x) = num(x), for an AND gate with *n* elements or an *n*-out-of-*m* gate.
- 720 index(x): return node's index
- Choose a polynomial  $q_x$  for each node:  $q_1, q_2, q_3, \ldots, q_8$
- 722
   degree  $(q_x) = K(x) 1$ , degree  $(q_1) = 0$ , degree  $(q_2) = 1$ , degree  $(q_3) = 1$ , degree  $(q_4) = 0$  

   723
   ..... degree  $(q_8) = 0$  as Figure 5 example.
- Access Tree: set root note  $q_1(0) = y$ , and chooses *degree*  $(q_1)$  other points of the polynomial  $q_1$  randomly to define it completely. For example, in Figure 5:  $q_1(0) = y \in Z_p$ ,  $q_2(0) = q_1(1), q_3(0) = q_1(2), q_4(0) = q_2(1), q_5(0) = q_2(2), q_6(0) = q_3(1), q_7(0) = q_3(2), q_8(0)$  $= q_3(3)$ .
- For each leaf node x, i = att(x) generates:
- 729 D

 $D = \{D_x = g^{\frac{q_x(0)}{t_i}} \text{ for all attributes a user has}\}, \text{ for example,}$ 

730 
$$D = \{ D_4 = g^{\frac{q_4(0)}{t_{trained}}}, D_5 = g^{\frac{q_5(0)}{t_{member}}}, D_6 = g^{\frac{q_6(0)}{t_{manager}}} \}$$

- 731 **Decryption function:**
- 732 Inputs:
- 733  $C = (\gamma, MY^s, T_i^s \quad \forall i \in \gamma)$
- 734 Private Key : D
- 735 Access Tree: T
- 736
- With inputs, define a recursive algorithm *DecryptNode* (*C*, *D*, *x*) that takes a node *x* in the tree and outputs a group element of  $G_2$  or  $\perp$ :
- 739 let i = att(x). If the node x is a leaf node,

740 DecryptNode 
$$(C, D, x) = e(D_x, T_i^s) = e(g^{\frac{q_x(0)}{t_i}}, g^{s \cdot t_i}) = e(g, g)^{s \cdot q_x(0)}$$
, if  $i \in \gamma$ , for example:

741 
$$e(D_6, T_{manager}^s) = e(g^{\frac{q_6(0)}{t_{manager}}}, g^{s \cdot t_{manager}}) = e(g, g)^{s \cdot q_6(0)}$$

742  $e(D_7, T_{contractor}^s) = e(g^{\frac{q_7(0)}{t_{contractor}}}, g^{s \cdot t_{contractor}}) = e(g, g)^{s \cdot q_7(0)}$ 

- 743 If x is not an attribute in leaf, then return  $\perp$ . If x is a non-leaf node, then proceeds as follows: for
- all nodes z that are children of x, call DecryptNode(C, D, z), and store the output as  $F_z$ . Let  $S_x$  be
- an arbitrary  $k_x$ -sized set of child nodes z such that  $F_z \neq \bot$ . If no such set exists, then the node was

not satisfied, and the function returns  $\perp$ . Otherwise, compute:

747 
$$F_x = \prod_{z \in S_x} F_z^{\Delta_{i,S'_x}(0)}$$
, where  $i = index(z)$ , is the index number of child node  $z$ ,  $S'_x = (index(z), Z)$ 

- 748  $\in S_x$  ), and Lagrange coefficient:  $\Delta_{i,s}(x) = \prod_{j \in S, j \neq i} \frac{x-j}{i-j}$ ,  $i \in Z_p$  and a set, S, of elements in  $Z_p$ .
- 749 =  $\prod_{z \in S_x} (e(g,g)^{sq_z(0)})^{\Delta_{i,S'_x}(0)}$
- 750 =  $\prod_{z \in S_x} (e(g,g)^{sq_{parent}(index(z))})^{\Delta_{i,S'x}(0)}$  (by construction)
- 751  $= \prod_{z \in S_{\mathcal{X}}} e(g,g)^{sq_{\mathcal{X}}(i)\Delta_{i,S'_{\mathcal{X}}}(0)}$
- 752  $= e(g,g)^{sq_{\chi}(0)}$  (using polynomial interpolation). For example:

753 
$$(e(g,g)^{sq_6(0)})^{\Delta_{1,(1,2,3)}(0)} (e(g,g)^{sq_7(0)})^{\Delta_{2,(1,2,3)}(0)} e(g,g)^{sq_3(0)} = e(g,g)^{sq_1(0)} = e(g,g)^{sy_1(0)} = e(g,g)^$$

754 Hence, 
$$q_6(0) = q_3(6), q_7(0) = q_3(7), q_3(0) = q_1(3)$$
.

- If and only if the ciphertext satisfies the tree, then  $DecryptNode(C, D, x) = e(g, g)^{sy}$ . Since  $MY^{s} =$
- 756  $Me(g, g)^{ys}$ , simply divide out  $e(g, g)^{ys}$  to recover the message M [HALL, GPSW].
- 757 KP-ABE is also useful for searching encryption contents from categorized attributes. For
- example, searching video from attribute set =  $\{a, b, c, d, e\}$  (*a* is title, *b* is actors, *d* is directors, *e*
- 759 .....), users can decrypt with search criteria such as a, b OR c, d AND e, and a OR e because
- they are all in the attribute set, but users cannot decrypt with search criteria *a* AND *f*, *d* AND
- 761 (NOT e), b AND (NOT c), f because the attribute set cannot satisfy the search criteria defined by
- 762 attribute set [GOLIC].

#### 763 **5. ABE System Considerations**

The ABE encryption scheme allows for higher data scalability, less computational time, low

765 memory usage, and large-scale deployments of system platforms [KKB] in comparison to

traditional PKE. However, for applications, it suffers from the drawbacks of low efficiency, less

- expressive access policies, and the use of random oracle models. Thus, the deployment andadoption of ABE have been slow. According to [ELT], ABE is absent from common data
- 769 products and formats that are generated by widely used commercial authoring products (e.g.,
- 770 Microsoft Word documents, Excel spreadsheets, PowerPoint slides) for lacking selective and
- fine-grained control over what is shared and with whom. In general, even with specific
- 772 modifications or add-on applications (e.g., blockchain), implementation of ABE applications
- should consider security, performance, and access control policies/model supports.

#### 774 **5.1.** Security

ABE provides confidentiality and data integrity when used in a public environment with a large

- scope (e.g., cloud) of users. However, relying only on user-specified attributes may create
- various security issues from the perspectives of key management processes and intentional
- threats or attacks.

### 779 5.1.1. Key Management

780 Secure communication: To distribute keys to users, a secure communication channel between a

vul user and the key management service is required such that an SSL-like connection is a common

solution for a large-scale ABE system. Hence, it is important for users to authenticate themselves

through – for example – usernames, passwords, or public key pairs managed on user devices.

784 Non-repudiation: Because the key management service generates private keys for users, it may

decrypt without authorization. If the secret key is abused, it is difficult to judge whether the

abused private key comes from users or the key management service [WZZGZZ]. Therefore,

- ABE systems are difficult for non-repudiation. This may not be an issue for organizations that
- host their own key management service and are willing to trust their system administrators or that do not require non-repudiation. A caveat is that the key management service must be highly
- 790 trusted.
- 791 **User tracking:** The problem of the basic ABE scheme is that there is no mechanism to identify
- the user who is issued a key. The secret key does not contain the specific information of users, so
- it is impossible to identify the user who misuses the distributed key or shares their secret key
- with other users [WZZGZZ]. A tracking function might be required for higher security
- requirements. However, providing traceability may infringe on a user's privacy by exposing the
- user's identifier value when the key is issued by the attribute verification [HL] process of the key
- 797 management service.
- 798 Key escrow: Because a user's private key is generated through the key management service,
- ABE has the capability of key escrow. However, such a capability can be a positive or negative
- 800 feature depending on the usages, such as a private organization using it for security control while
- 801 sacrificing the privacy of its users. Several variant ABE systems have been proposed that remove

- 802 the escrow by replacing encryption or key generation processes with certificate-based encryption
- 803 [CRAI], secure key issuing cryptography [BCEKJS], or certificateless cryptography [AP].
- 804 Key revocation: One of the major advantages of any identity encryption scheme is that a third

party's secret key can be destroyed after all users have been issued keys and if there is only a

806 finite number of users. This can take place for ABE system as well because it assumes that keys

- are always valid once issued, and there is no method for key revocation to handle secret keys due
- to expiry of embedded attributes, faulty access policies, or key compromise. Key revocation for
- ABE can be handled by including the expiry time/date among the attributes, periodic refreshing,
- and revocation lists [GOLIC].

#### 811 **5.1.2. Threats and Attacks**

812 **Compromised key management server:** ABE relies on a key management service for the

- 813 generation of cryptography keys. If the key management service is compromised, data protected
- by the public-private key pair used is also compromised. Hence, a key management service is a
- 815 high-value target for adversaries who wish to decrypt all ciphertexts. A countermeasure for this
- 816 vulnerability is to frequently update the master private-public key pairs with new independent
- 817 key pairs for all users. However, this complicates the key management process.
- 818 **Collusion:** CP-ABE users can infer other users' attributes through collusion with each other,
- generate another user's secret key with the inferred attributes, and share private decryption keys
- 820 (and maybe attribute certificates if applicable) [MIHIR]. Therefore, when a key management
- service generates a secret key, it must do so by applying various variables in addition to the
- 822 user's attributes. If data leaks through a collusion attack on resource providers, security
- technology is required so that only a legitimate user can decrypt and view the ciphertext
- 824 [MIHIR].
- **Fully secure:** Fully secure (i.e., adaptive) ABE is more advantageous than selectively secure
- ABE because it does not require adversaries to specify their target access policies or attribute
- 827 lists until they receive the system public keys. General ABE schemes based on prime order
- groups for cryptography lack the proof of fully secure, so efforts in proof methods are needed to
- 829 promote more secure and efficient designs. Existing fully secure ABE solutions are usually
- 830 designed on composite-order groups or re-encryption<sup>3</sup> systems, and complex assumptions are
- 831 involved in the security proof [ZDXSLZ, HL].
- 832 **Integrity:** Outsourcing servers for an ABE system requires trust so that the decrypted ciphertext
- is a legitimate message based on legitimate user attributes. Additionally, the message uploaded
- to the resource provider can be falsified, and it is unknown whether the value calculated by the
- outsourcing server is the correct value. Accordingly, it is necessary to verify whether the user's
- final decrypted value is the original message from the data owner [HL]. Specifically, verification
- processes are required to prove that the results computed from key management and resource
- 838 servers are properly computed.

<sup>&</sup>lt;sup>3</sup> Proxy re-encryption (PRE) allows a proxy to convert a ciphertext encrypted under one key into an encryption of the same message under another key. The main idea is to place as little trust and reveal as little information to the proxy as necessary to allow it to perform its translations [uma].

- 839 Quantum resistant: ABE systems are insecure against quantum computer attacks. Many public-
- 840 key encryption schemes including ABE require security enhancements to resist possible
- quantum attacks. Although lattice-based algorithms can resist quantum attacks, there are only a
- 842 few lattice-based ABE constructions that are selectively secure. In addition, lattice-based
- schemes lack practicability because they have only been considered secure for inefficiently large
- 844 parameters. Thus, more attention should be paid to anti-quantum ABE for better security
- 845 assurance [ZDXSLZ, DKW, WWW].

### 846 **5.2.** Performance

A performance bottleneck of ABE is the high computation overhead due to the complexity of the embedded bilinear pairing algorithm and the requirement for large security parameters [OD] to

849 cover a wider scope of attributes.

# 850 **5.2.1. Computational Complexity**

851 Most of the existing ABE schemes, (e.g., such as revocable ABE, accountable ABE, policy-

hiding ABE, ABE with policy updating, and multi-authority ABE) have a high order of

853 computational complexity for typical cryptographic operations – including exponentiation, point

multiplication, group arithmetic operations, and especially, the bilinear pairing calculation – that

are much greater than that of symmetric and traditional PKE [ZDXSLZ]. Therefore, it may be more efficient to apply alternative schemes like non-bilinear pairing-based ABE schemes [KAB]

for practical uses of ABE, especially in a resource-constrained system environment such as IoT.

for practical uses of ABE, especially in a resource-constrained system environment such as I

# 858 **5.2.2. Keys and Ciphertext Size**

859 Both CP-ABE and KP-ABE schemes have overhead issues with key size. In CP-ABE, the public key size can be fixed with a hash function or made linear to the number of attributes applied. In 860 861 KP-ABE, the size of the public key is linear to the maximum number of attributes applied to the system [GOLIC]. The size of the ciphertext depends on the number of available attributes 862 863 contained in the access structure, and it increases linearly with the number of attributes, which 864 requires significant system storage and computation time for users to decrypt ciphertext. 865 Therefore, it might be necessary to introduce assistant systems to accommodate the heavier 866 computation (e.g., increase the computational efficiency with architecture options, such as proxy 867 devices [MHR]), but a verification process is needed to prove that the results on the outsourcing 868 server are properly computed [HL]. Further, CP-ABE is not efficient for modern enterprise 869 environments when compared to KP-ABE due to that the resource access policies needed for 870 central management such that when a policy changes, secret keys need to be re-established for 871 users. In contrast, KP-ABE is made more flexible by its broadcast type of encryption [UMAS]

872 for user policies.

# 873 **5.2.3.** Physical Limitations

874 The physical properties of ultra-low energy mobile devices [OD] include low processing power,

- a distributed nature, and a lack of standardization [RPRMK], which limit their capabilities for
- 876 performing complex computations to support ABE's (especially CP-ABE's) encryption and

- 877 decryption. These drawbacks hinder ABE adoption for advanced applications, such as IoT and
- 878 cloud systems, due to the much greater heterogeneity and resource restrictions of their devices.
- 879 Therefore, further investigation into the application of ABE is needed to decide device sizing
- against levels of computation, communication, and performance. Mobile computing for ABE has
- established its own paradigm, which has extended to researching whether ABE for mobile
- devices can be translated to the application of IoT [MHR].
- 883 Researchers are currently working on blockchain fundamentals and customizing blockchain-
- based ABE models for IoT applications to provide privacy and minimize computational
- 885 overhead. For example, [QYLPYH] use a lightweight blockchain ABE to outsource decryption
- based on the blockchain, which can be extended to effectively reduce the burden of encryption
- 887 computation on the user side. Blockchain technology can also provide integrity (i.e., the secret
- key does not contain the specific information of users who may share their secret keys with other users) and the non-repudiation of data, as well as prevent the leaking of sensitive information
- 890 from ABE access structure [WZZGZZ].

# 891 5.3. Access Control Policies and Model Supports

- 892 In addition to functionalities like revocation, accountability, attribute privacy protection, policy
- updating, decentralization (multi-authorities), and key hierarchy for practical access control
- system deployments [ZDXSLZ], the applicable access policy structure for ABE is restricted to
- 895 supporting non-monotone and stated policy rules [TKN]. For example, CP-ABE allows data 896 owners to define their own access policies (structures) by attributes and, thus, support complex
- access control policy structure. However, by only associating attributes, decryption keys are
- 898 organized logically as a static set. Users can only use all possible combinations of attributes in
- the set of keys issued to compose their policies, and it has restrictions for specifying policies,
- 900 attribute managements (e.g., applying environment conditions and dynamic attributes), and the
- 901 application of deny rules, which fails to satisfy the enterprise requirements of access control in
- 902 terms of flexibility and dynamic requirements [BS].
- 903 In KP-ABE, the secret key and ciphertext relate to a set of attributes to offer fine-grained access
- 904 control [BCSES] for which permission evaluation depends only on the resources' attributes. The
- 905 resource provider (i.e., data owner or encrypted) cannot specify the access policy except by
- 906 choosing descriptive attributes for permissions. This means there is no choice but to trust the key
- 907 issuer. Such accountability for user secret keys provides fine-grained access without flexibility or
- scalability [BS], making it unsuitable for certain applications unless supported by re-encryption
- 909 techniques [GOLIC].
- 910 Further, from the perspective of full access, action capabilities including write, modification,
- 911 and execute privileges are not straightforwardly implemented in ABE schemes and thus require
- 912 other layers of operational support.
- 913

#### 914 **6. Conclusion**

- 915 ABE supports fine-grained access control for encrypted data and is a cryptographic scheme that
- 916 go beyond the all-or-nothing approach of public-key encryption schemes. This document
- 917 reviewed the interplay between cryptography and the access control of ABE, from fundamental
- 918 theories on which the ABE scheme is based to various main algorithms of IBE, CP-ABE, and
- 919 KP-ABE, as well as considerations for deploying ABE systems.
- 920 Due to security, performance, and access control policy/model support considerations, the
- 921 deployment and adoption of ABE have been slow. Few commercial widely used products (e.g.,
- 922 Microsoft Word, Excel, PowerPoint) use it to date. This shortcoming of selective and flexible
- access control might impact its adoption for government and commercial applications as well as
- 924 applications for highly secure demanding areas (e.g., life sciences, healthcare, financial sectors)
- 925 [ELT]. However, with additional exploration and the support of additional outsources or
- 926 processing systems, a mature ABE technology can address these challenges.

#### 928 **References**

929	[ADI]	Adi S (1984) Identity-Based Cryptosystems and Signature Schemes. Lecture
930		Notes in Computer Science. Vol. 196. Springer, pp 47–53. Available at
931		https://doi.org/10.1007/3-540-39568-7_5
932	[AP]	Al-Riyami SS, Paterson KG (2003) Certificateless public key cryptography,
933		ASIACRYPT 2003, 9th International Conference on the Theory and Application
934		of Cryptology and Information Security, Taipei, Taiwan, Proceedings. Lecture
935		Notes in Computer Science. Vol. 2894. Springer. pp. 452–473. doi:10.1007/978-
936		3-540-40061-5 29. Available at https://eprint.iacr.org/2003/126.pdf
937	[BC2018]	Buchanan B (2018) Having Fun With BN-curves, Published in Coinmonks.
938		Available at https://medium.com/coinmonks/having-fun-with-bn-curves-
939		37fb5b816f67
940	[BCEKJS]	Byoungcheon L, Colin B, Ed D, Kwangjo K, Jeongmo Y, Seungjae Y (2004)
941	L ]	Secure key issuing in ID-based cryptography, 2004 ACSW Workshops – the
942		Australasian Information Security Workshop (AISW2004), Vol. 32. Australian
943		Computer Society. pp. 69–74. Available at
944		https://dl.acm.org/doi/10.5555/976440.976449
945	[BCSES]	Bagyalakshmi C, Samundeeswari ES (2018) A Survey on Attribute Based
946		Encryption Techniques in Data Security Using Cloud Environment, Journal of
947		Advanced Research in Dynamical and Control Systems, Vol. 10, 03-Special
948		Issue. Available at
949		https://www.researchgate.net/publication/346095629 A survey on attribute bas
950		ed encryption techniques in data security using cloud environment
951	[BETH]	Bethencourt J (2015) Intro to Bilinear Maps, Computer Sciences Department
952		Carnegie Mellon University. Available at
953		https://people.csail.mit.edu/alinush/6.857-spring-2015/papers/bilinear-maps.pdf
954	[BF]	Boneh D, Franklin M (2001) Identity-Based Encryption from the Weil Pairing,
955		Advances in Cryptology — CRYPTO 2001. CRYPTO 2001. Lecture Notes in
956		Computer Science, vol 2139. Springer. https://doi.org/10.1007/3-540-44647-8_13
957	[BONEH]	Boneh D, et. Al (2002) IBE Secure E-mail, Standford University. Available at
958		https://crypto.stanford.edu/ibe/
959	[BS]	Bagyalakshmi C, Samundeeswari ES (2018) A survey on attribute based
960		encryption techniques in data security using cloud environment, Journal of
961		Advanced Research in Dynamical and Control Systems 10(03):926-931.
962		Available at
963		https://www.researchgate.net/publication/346095629 A survey on attribute bas
964		ed encryption techniques in data security using cloud environment
965	[BSW2007]	Bethencourt J, Sahai A, Waters B (2007) Ciphertext-Policy Attribute-Based
966		Encryption, 2007 IEEE Symposium on Security and Privacy (SP '07).
967		https://doi.org/10.1109/SP.2007.11
968	[BSW2011]	Boneh D, Sahai A, Waters B (2011) Functional Encryption: Definitions and
969	-	Challenges, In: Ishai, Y. (eds) Theory of Cryptography. TCC 2011. Lecture Notes
970		in Computer Science, vol 6597. Springer, Berlin, Heidelberg.
971		https://doi.org/10.1007/978-3-642-19571-6 16

972	[BSW2012]	Boneh D, Sahai A, Waters B (2012) Functional encryption: a new vision for
973		public-key cryptography, Communications of the ACM Volume 55 Issue 11
974		November 2012 pp 56–64. <u>https://doi.org/10.1145/2366316.2366333</u>
975	[BUCH]	Buchanan B (2022) Pairing-based Cryptography, OBE presentation. Available at
976	[boch]	https://www.youtube.com/watch?v=4zu-kXIiXA4
977	[BUTE]	Buterin V (2017) Exploring Elliptic Curve Pairings, <i>Midium</i> . Available at
978		https://medium.com/@VitalikButerin/exploring-elliptic-curve-pairings-
978 979		c73c1864e627
979 980	[CORB]	Corbellini A (2015) Elliptic Curve Cryptography: finite fields and discrete
980 981	[COKD]	logarithms. Available at https://andrea.corbellini.name/2015/05/23/elliptic-curve-
981 982		•
982 983	[CRAI]	<u>cryptography-finite-fields-and-discrete-logarithms/</u> Craig G (2003) Certificate-based encryption and the certificate revocation
985 984	[UKAI]	problem, Biham, Eli (ed.). Advances in Cryptology – EUROCRYPT 2003,
984 985		
985 986		International Conference on the Theory and Applications of Cryptographic
		Techniques, Warsaw, Poland, Proceedings. Lecture Notes in Computer Science.
987 088		Vol. 2656. Springer. pp. 272–293. <u>https://doi.org/10.1007/3-540-39200-9_17</u>
988	[DANI]	Daniel RLB (2009) SEC 1: Elliptic Curve Cryptography, https://www.secg.org
989 000		Certicom Research Version 2.0. Available at <u>https://www.secg.org/sec1-v2.pdf</u>
990 001	[DKW]	Datta P, Komargodski I, Waters B (2021) Decentralized Multi-Authority ABE for DNEs from LWE A major revision of on LACP publication in EUROCRYPT
991 992		DNFs from LWE, A major revision of an IACR publication in EUROCRYPT
992 993		2021. Available at <u>https://eprint.iacr.org/2020/1386.pdf</u>
993 994	[ELT]	Eldefrawy K, Lepoint T, Tam L (2022). In-App Cryptographically-Enforced
994 995		Selective Access Control for Microsoft Office and Similar Platforms. Cyber
995 996		Security, Cryptology, and Machine Learning. CSCML 2022. Lecture Notes in Computer Science, vol 13301. Springer, Cham. Available at
990 997		https://doi.org/10.1007/978-3-031-07689-3
998	[FIPS186-5]	Federal Information Processing Standards Publication. Digital Signature Standard
999 999	[111 5160-5]	(DSS), https://doi.org/10.6028/NIST.FIPS.186-5
1000	[GOLIC]	Golic J (2018) Attribute-based Encryption and Signatures, presentation. Available
1000	[GOLIC]	at <u>https://www.youtube.com/watch?v=l0yCigNqv5w</u>
1001	[GPSW]	Goyal V, Pandey O, Sahai A, Waters B (2006) Attribute-Based Encryption for
1002		Fine-Grained Access Control of Encrypted Data, CCS '06: Proceedings of the
1005		13th ACM conference on Computer and communications security pp 89–98.
1005		Available at https://eprint.iacr.org/2006/309.pdf
1005	[GW]	Gong J, Wee H (2020) Adaptively Secure ABE for DFA from K-Lin and More,
1007	[0,,]	International Association for Cryptologic Research. Available at
1008		https://www.youtube.com/watch?v=IYzRYWSoE
1009	[HALL]	Hallsted S (2015) Attribute-based Encryption, Presentation on theme: "Attribute
1010	[]	Based Encryption", slideplayer.com. Available at
1010		https://slideplayer.com/slide/3246359/
1012	[HL]	Hwang Y, Lee I (2020) A Study on CP-ABE-Based Medical Data Sharing System
1012	[]	with Key Abuse Prevention and Verifiable Outsourcing in the IoMT
1012		Environment, Special Issue of Internet of Medical Things in Healthcare
1015		Applications, Department of Computer Science and Engineering, Soonchunhyang
1016		University, Korea. https://doi.org/10.3390/s20174934
-		

1017	[HR]	Nurmamat Helil N, Rahman K (2017) CP-ABE Access Control Scheme for
1018		Sensitive Data Set Constraint with Hidden Access Policy and Constraint Policy,
1019 1020		Security and Communication Networks, vol. 2017, Article ID 2713595.
1020	[HUBWIZ]	https://doi.org/10.1155/2017/2713595 hubwiz.com (2020) Bilinear Pairs. Available at
1021		http://blog.hubwiz.com/2020/06/04/bilinear-pairing/
1022	[IRON]	IRONCORE LABS (2018) Pairing Based Transform Cryptography (Proxy Re-
1023	[IKON]	Encryption - PRE), Presented at DEF CON 26. Available at
1024		https://www.slideshare.net/IronCoreLabs/pairing-based-transform-cryptography-
1025		proxy-reencryption-pre
1020	[KAB]	Karati A, Amin R, Biswas G.P. (2016) Provably Secure Threshold-Based ABE
1027		Scheme Without Bilinear Map, Arab J Sci Eng 41, 3201–3213 (2016).
1020		https://doi.org/10.1007/s13369-016-2156-9
1029	[KB]	Kar D, Bezawada B (2018) Attribute Based Encryption, Presentation on theme:
1031	[122]	"Attribute Based Encryption" – Presentation transcript, Colorado State
1032		University. Available at https://slideplayer.com/slide/13691307/
1033	[KKB]	Kavuri A, Kancherla GR, Bobba, B (2017) An Improved Integrated Hash and
1034	LJ	Attributed based Encryption Model on High Dimensional Data in Cloud
1035		Environment, International Journal of Electrical and Computer Engineering, 7(2),
1036		950. <u>https://doi.org/10.11591/ijece.v7i2.pp950-960</u>
1037	[LXYS]	Lin G, Xia Y, Ying C, Sun Z (2019) F2P-ABS: A Fast and Secure Attribute-
1038		Based Signature for Mobile Platforms, Security and Communication Networks
1039		Research Article of Hindawi. https://doi.org/10.1155/2019/5380710
1040	[MATA]	Matarazzo, L (2015) A Look Into Elliptic Curve Cryptography (ECC). Available
1041		at <u>https://www.youtube.com/watch?v=5wDvlq-MrLg</u>
1042	[MEFF]	Meffert D (2009) Bilinear Pairings in Cryptography, Radboud Universiteit
1043		Nijmegen Computing Science Department. Available at
1044		https://www.math.ru.nl/~bosma/Students/MScThesis_DennisMeffert.pdf
1045	[MD]	Moody D, Peralta R, Perlner R, Regenscheid A, Roginsky A, Chen L (2015)
1046		Report on Pairing-based Cryptography, Journal of Research of the National
1047		Institute of Standards and Technology, Volume 120 (2015).
1048		https://doi.org/10.6028/jres.120.002
1049	[MPR]	Maji HK, Prabhakaran M, Rosulek M(2011) Attribute-Based Signatures, Kiayias,
1050		A. (eds) Topics in Cryptology – CT-RSA 2011. CT-RSA 2011. Lecture Notes in
1051		Computer Science, vol 6558. Springer, Berlin, Heidelberg.
1052		https://doi.org/10.1007/978-3-642-19074-2_24
1053	[MHH]	Moffat S, Hammoudeh M, Hegarty R (2017) A Survey on Ciphertext-Policy
1054		Attribute-based Encryption (CP-ABE) Approaches to Data Security on Mobile
1055		Devices and its Application to IoT, ICFNDS '17: Proceedings of the International
1056 1057		Conference on Future Networks and Distributed Systems Article No.: 34. https://doi.org/10.1145/3102304.3102338
1057	[MHR]	Moffat S, Hammoudeh M, Robert R (2017) A Survey on Ciphertext-Policy
1058		Attribute-based Encryption (CP-ABE) Approaches to Data Security on Mobile
1059		Devices and its Application to IoT, ICFNDS '17: Proceedings of the International
1060		Conference on Future Networks and Distributed Systems Article No.: 34.
1061		https://doi.org/10.1145/3102304.3102338
1002		

10(2		Milia D (2021) Institution to Mailane Constant and the Islandity have 1 Encounting
1063	[MIHIR]	Mihir B (2021) Invitation to Modern Cryptography - Identity-based Encryption,
1064		presentation for CSE207, UCSD Computer Science. Available at
1065	DAMCCI	https://www.youtube.com/watch?v=kdf0u2TGgNg
1066	[MMSC]	Microprocessor and Microcomputer Standards Committee of the IEEE Computer
1067		Society (2004) IEEE Standard Specifications for Public-Key Cryptography—
1068		Amendment 1: Additional Techniques, IEEE Computer Society. Available at
1069		https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=1335427
1070	[MOBI]	Mobilefish.com (2016) Blockchain tutorial 11: Elliptic Curve key pair generation.
1071		Available at <u>https://www.youtube.com/watch?v=wpLQZhqdPaA</u>
1072	[MPPRRC]	Moody D, Peralta R, Perlner R, Regenscheid A, Roginsky A, Chen L (2015)
1073		Report on Pairing-based Cryptography, Journal of Research of the National
1074		Institute of Standards and Technology Volume 120.
1075		http://dx.doi.org/10.6028/jres.120.002
1076	[MUKH]	Mukhopadhyay D (2017) Attribute Based Encryption (ABE), Department of
1077		Mathematics IIT Kharagpur NPTEL Online Certification Course. Available at
1078		https://www.youtube.com/watch?v=ZogQMKzoQdw
1079	[MY]	Mahto D, Yadav D K (2017) RSA and ECC: A Comparative Analysis,
1080		International Journal of Applied Engineering Research ISSN 0973-4562 Volume
1081		12, Number 19 (2017) pp. 9053-9061.
1082		https://www.ripublication.com/ijaer17/ijaerv12n19_140.pdf
1083	[OD]	Odelu V, Das AK (2016) Design of a new CP-ABE with constant-size secret keys
1084		for lightweight devices using elliptic curve cryptography, Security and
1085		Comunication Networks Security Comm. Networks 2016, Published online in
1086		Wiley Online Library. <u>https://doi.org/10.1002/sec.1587</u>
1087	[QIAU]	Qiau P (2020) Bilinear Paring for Cryptograph Application, Hyperchain
1088		Technology Incop. https://zhuanlan.zhihu.com/p/321902465
1089	[QYLPYH]	Authors: Qin X, Yang Z, Li Q, Pan H, Yang Z, Huang Y(2022) Attribute-based
1090		encryption with outsourced computation for access control in IoTs. ASSE' 22: 2022
1091		3rd Asia Service Sciences and Software Engineering Conference, pp 66-73.
1092		https://doi.org/10.1145/3523181.3523191
1093	[ROBI]	Robinson E (2015) Elliptic Curve Cryptography, YSL Information Security –
1094		Public-Key Cryptography. Available at
1095		https://player.slideplayer.com/16/4898906/#
1096	[RPRMK]	Rahulamathavan Y, Phan RC, Rajarajan M, Misra S, Kondoz A (2017) Privacy-
1097		preserving Blockchain based IoT Ecosystem using Attribute-based Encryption,
1098		2017 IEEE International Conference on Advanced Networks and
1099		Telecommunications Systems (ANTS).
1100		https://doi.org/10.1109/ANTS.2017.8384164
1101	[SCHOOF]	Schoof R (1995), Counting points on elliptic curves over finite fields, Journal de
1102		Theorie des Nombres de Bordeaux 7, 219-254. Available at
1103		http://www.numdam.org/item/JTNB_1995_7_1_219_0.pdf
1104	[SHINDE]	Shinde S (2020) Privacy Teaching Series: What is Functional Encryption.
1105		OpenMined Functional Encryption. Available at
1106		https://blog.openmined.org/privacy-teaching-series-what-is-functional-encryption
1107	[SP800-162]	Hu VC, Ferraiolo D, Kuhn R, Schnitzer A, Sandlin K, Miller R, Scarfone K
1108		(2014) Guide to Attribute Based Access Control (ABAC) Definition and

1100		
1109		Considerations, NIST Special Publication 800-162.
1110	[CD000 10/]	https://doi.org/10.6028/NIST.SP.800-162
1111	[SP800-186]	Chen L, Moody D, Regenscheid A, Randall K (2023) Recommendations for
1112		Discrete Logarithm-Based Cryptography (Elliptic Curve Domain Parameters),
1113		Draft NIST Special Publication 800-186. <u>https://doi.org/10.6028/NIST.SP.800-</u>
1114		$\frac{186}{100}$
1115	[SP800-56A]	Barker E, Chen L, Roginsky A, Vassilev A (2018) Recommendation for Pair-
1116		Wise Key-Establishment Schemes Using Discrete Logarithm Cryptography, NIST
1117		Special Publication 800-56A Revision 3. https://doi.org/10.6028/NIST.SP.800-
1118	[077]	56Ar3
1119	[ST]	Tahat N, Shatnawi S (2022) New Signature Scheme Based on Elliptic Curve and
1120		Factoring Problems Using Chaotic Map, Journal of Applied Security Research.
1121		https://www.tandfonline.com/doi/full/10.1080/19361610.2022.2041157
1122	[SW]	Sahai A, Waters B (2005) Fuzzy Identity-Based Encryption Cryptology,
1123		Proceedings of the 24th annual international conference on Theory and
1124		Applications of Cryptographic Techniques 2005 Pages 457–473.
1125		https://doi.org/10.1007/11426639_27
1126	[TDN]	Tiplea FL, Dragan C, Nica A (2017) Key-Policy Attribute-Based Encryption from
1127		Bilinear Maps, International Conference for Information Technology and
1128		Communications. <u>https://doi.org/10.1007/978-3-319-69284-5_3</u>
1129	[TKN]	Tomida J, Kawahara Y, and Nishimaki R (2021) Fast, Compact, and Expressive
1130		Attribute-Based Encryption, Designs, Codes and Cryptography (2021) 89:2577-
1131		2626. https://doi.org/10.1007/s10623-021-00939-8
1132	[UMAS]	Umashankar SKA (2016) A Review on Attribute Based Encryption (ABE) and
1133		ABE Types, Semantic Scholar - Computer Science. Available at
1134		https://www.semanticscholar.org/paper/A-Review-on-Attribute-Based-
1135		Encryption-(ABE)-and-
1136		Umashankar/c3910ecacc2a6c1ceb3c54eb493f2c8c801e9e25
1137	[WF]	Wall B, Frederickson C (2018) Implementing a Library for Pairing-based
1138		Transform Cryptography, DEF CON 26 Crypto and Privacy Village Conference
1139		video 23:09. Available at https://cryptovillage.org/implementing-a-library-for-
1140		pairing-based-transform-cryptography
1141	[WWW]	Water B, Wee H, Wu D J (2022) Multi-Authority ABE from Lattices without
1142		Random Oracles, A major revision of an IACR publication in TCC 2022.
1143		Available at <u>https://eprint.iacr.org/2022/1194.pdf</u>
1144	[WZZGZZ]	Wu A, Zhang Y, Zheng X, Guo R, Zhao Q, Zheng D (2019) Efficient and
1145		Privacy-preserving Traceable Attribute-based Encryption in Blockchain, Annals
1146		of Telecommunications 74:401–411. <u>https://doi.org/10.1007/s12243-018-00699-y</u>
1147	[ZDXSLZ]	Zang Y, Deng RH, Xu S, Sun J, Li Q, Zeng D (2020) Attribute-based Encryption
1148		for Cloud Computing Access Control: A Survey, Computing Surveys, Vol. 53,
1149		No. 4, Article 83. <u>https://doi.org/10.1145/3398036</u>
1150		