

# Grøstl

Praveen Gauravaram, Lars R. Knudsen, Krystian Matusiewicz,  
Florian Mendel, Christian Rechberger,  
Martin Schläffer, Søren S. Thomsen

[www.groestl.info](http://www.groestl.info)

First SHA-3 Candidate Conference, 2009

MAT, DTU

IAIK, TU Graz

# The Grøstl Hash Function

- Grøstl is FAST
- Grøstl is PROVABLY SECURE
- Grøstl is SIDE-CHANNEL RESISTANT
- Grøstl is SIMPLE
- ...

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- Grøstl is SIMPLE
- ...
- Grøstl TASTES GOOD and is CO<sub>2</sub> NEUTRAL
- Grøstl is THE ANSWER to  
the question on life, the universe and everything.

# What sets Grøstl apart:

- The team
  - Hash design experience
  - Hash cryptanalysis experience
- Solid at every level
  - Hash function → compression function → two permutations
- Simplicity of Grøstl
  - Simplicity of design
  - Simplicity of analysis
- Balanced implementation characteristics

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# The Grøstl Design Team

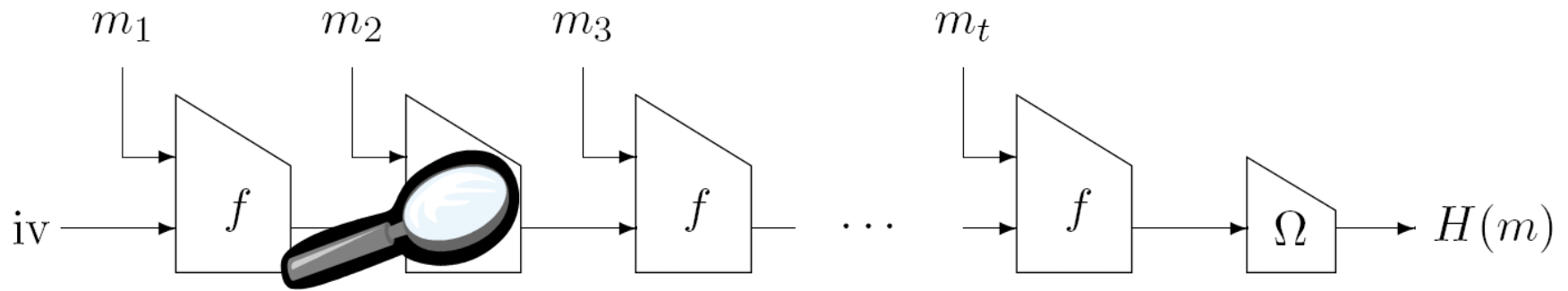


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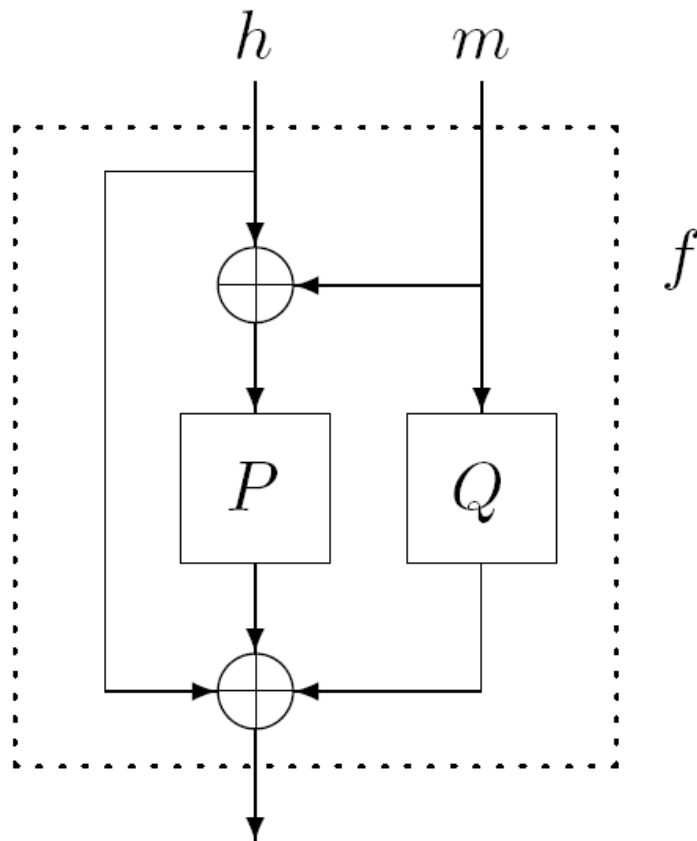


# The Grøstl Hash Function





# The Grøstl Compression Function

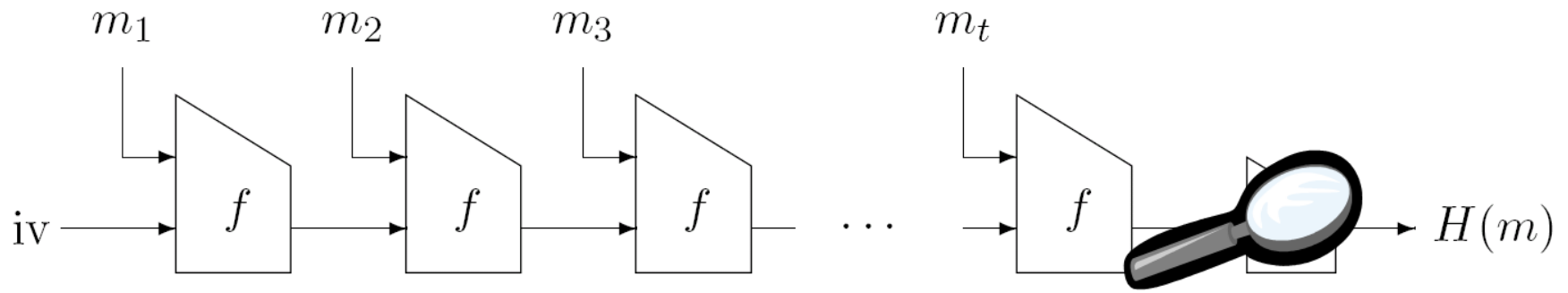


**Grøstl-256:**  
512-bit permutations

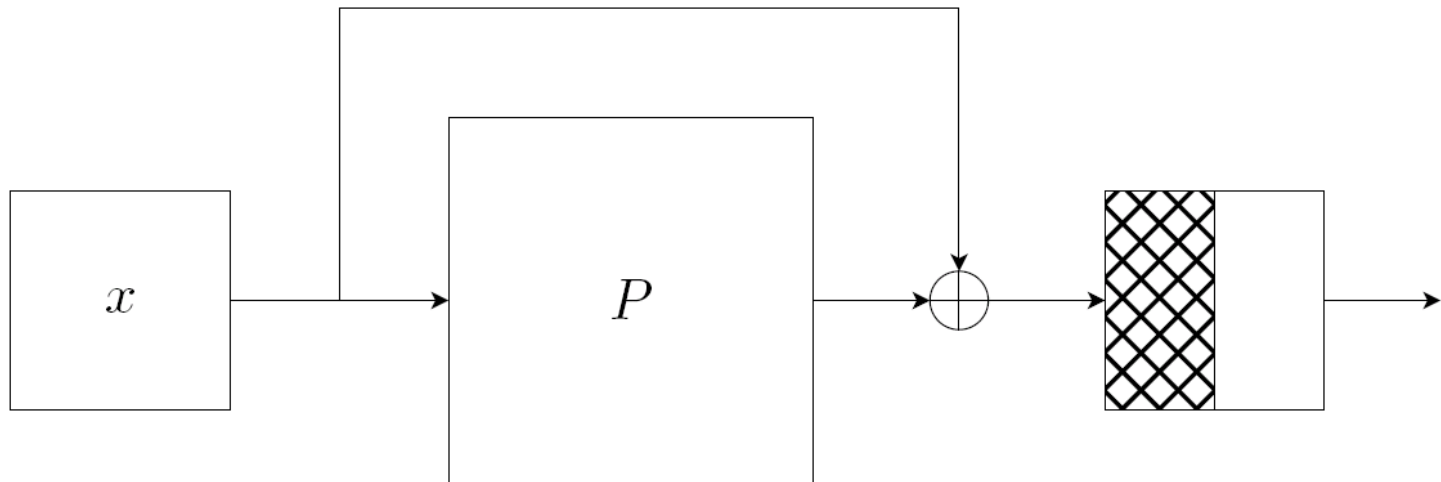
**Grøstl-512:**  
1024-bit permutations

$$f(h, m) = P(h \oplus m) \oplus Q(m) \oplus h$$

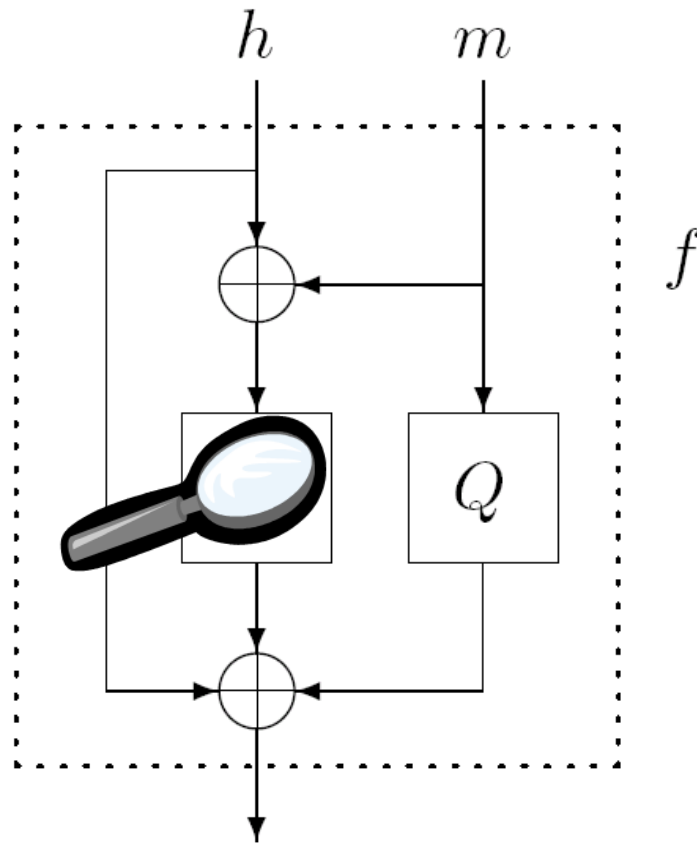
# The Grøstl Hash Function



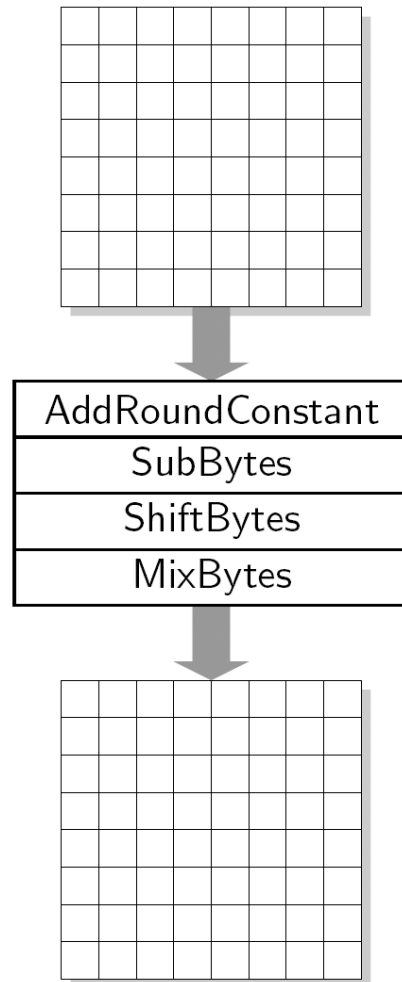
# The Output Transformation



# The Grøstl Compression Function



# The State / Round Transformation



AES-like

Grøstl-256:  
8x8 geometry  
10 rounds

Grøstl-512:  
8x16 geometry  
14 rounds

# Simple and proven solid

- Iteration
  - wide-pipe + MD + output transform
- Compression function
  - two permutations in well studied construction
- Permutation
  - “wide trail” design strategy → bounds on various attacks
  - undergone serious cryptanalysis
- Reduction proofs for collisions/preimages: done
- Reduction proofs for RO-indifferentiability: to be done

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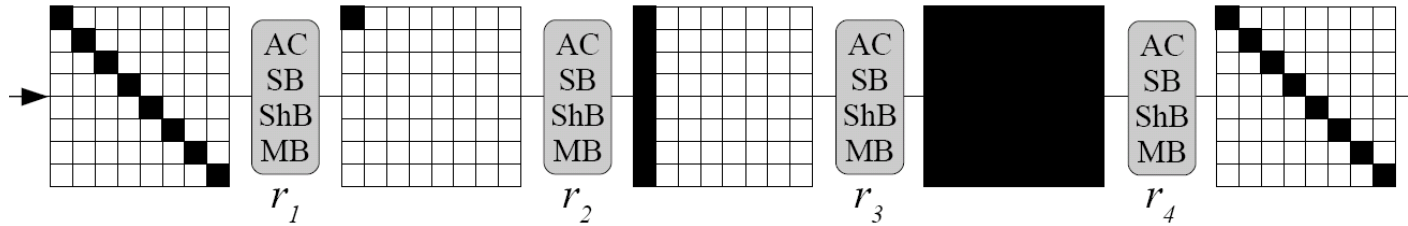
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  - Simplicity of design
  - **Simplicity of analysis**
- Balanced implementation characteristics





# Simplicity of Analysis



- Grøstl allows to construct optimal (truncated) differentials, and prove bounds on them
- ➔ Bounds on “standard” differential attack

# Internal Cryptanalysis

- **Rebound-Attacks** on the compression function  
6 rounds out of 10 (FSE 2009)
- Side-effects of this work
  - Practical collision attack on Twister compress
  - Compression function attack on Cheetah-512 (8.5 out of 12)
  - Compression function attack on Maelstrom (8.5 out of 10)
  - Compression function attack on Whirlpool (7.5 out of 10)
- Freedom left for attacks on block ciphers based hashes
  - But not for Grøstl

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# Balanced implementation characteristics

- No preference for particular platform
  - No preference for particular wordsize
  - Allows table based implementations
  - Allows implementation techniques without tables
    - Bit-sliced
    - Special instructions (e.g. Intel)
- No Cache Attacks**

# Performance

	<b>Grøstl 256</b>	<b>Grøstl 512</b>
<b>AMD Opteron (64-bit)</b>	19,50	
<b>Intel Core2Duo (64-bit)</b>	21,45	30,45
<b>Intel Core2Duo (32-bit)</b>	23,11	36,70
<b>Intel Pentium M 760 (32-bit)</b>	28,90	67,40
ATMega 163 (8-bit), estimates	415,00	580,00

Numbers are cycles/byte for long messages

Further speed-ups to be expected

Hardware: many trade-offs possible, see Appendix

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# Summary

# Summary of Grøstl

- Solid construction at every level
  - Iteration
    - wide-pipe + MD + output transform
  - Compression function
    - provable query complexities for collision/preimage
  - Permutation
    - “wide trail” design strategy → bounds on various attacks
    - undergone serious cryptanalysis
- More flexible implementation characteristics than SHA-2
- Easier to get confidence in

# Grøstl Q&A

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# Supporting slides

# The name Grøstl



# An open call

What would be the name/pronunciation  
of the DISH „hash“  
in YOUR language/country?

- Examples:
  - Austrian/Austria: Gröstl
  - Danish/Denmark: Biksemad
  - Swiss-German/Switzerland: Röstli

# Security claims / attacks

- The Grøstl hash function:

Attack type	Claimed complexity	Best known attack
Collision	$2^{n/2}$	$2^{n/2}$
$d$ -collision	$\lg(d) \cdot 2^{n/2}$	$(d!)^{1/d} \cdot 2^{n(d-1)/d}$
Preimage	$2^n$	$2^n$
Second preimage	$2^{n-k}$	$2^n$

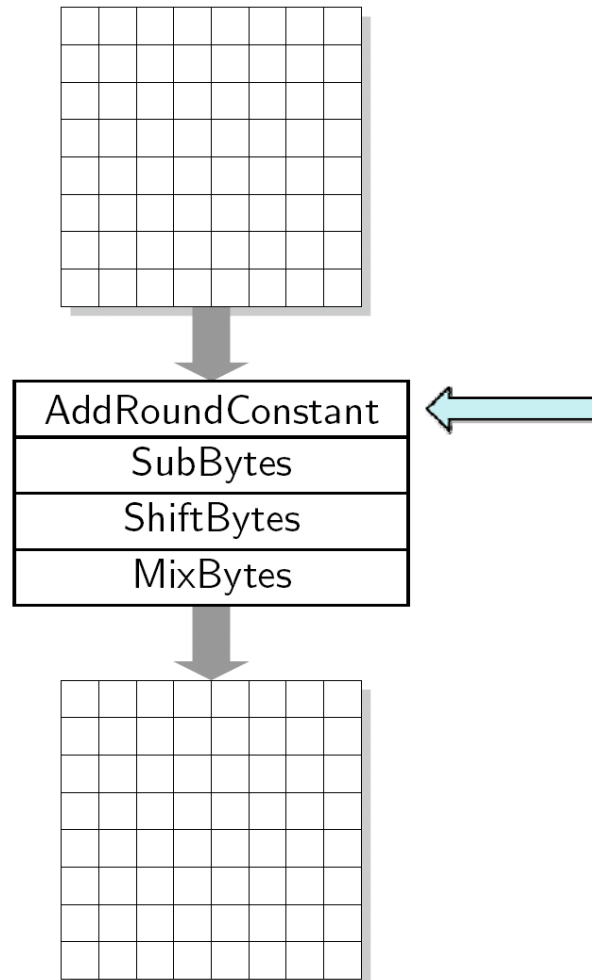
- The Grøstl compression function:

Attack type	Claimed complexity	Best known attack
Collision	$2^{\ell/4}$	$2^{\ell/3}$
Preimage	$2^{\ell/2}$	$2^{\ell/2}$

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# Supplementary Illustration for the Permutations P & Q

# The State / Round Transformation

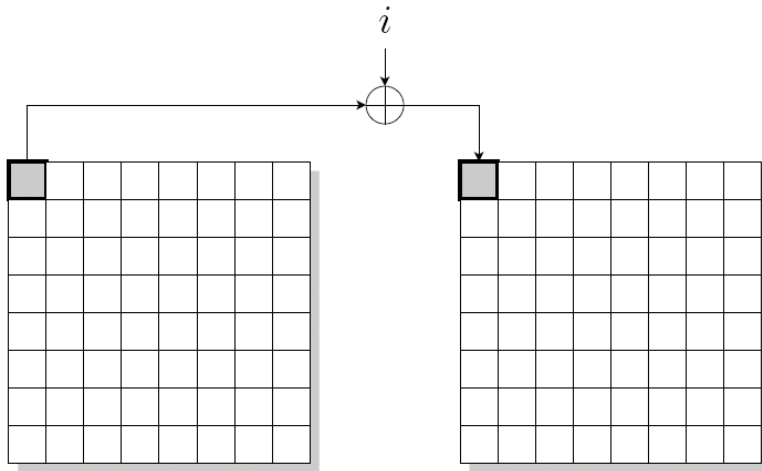


Grøstl-256:  
8x8 geometry

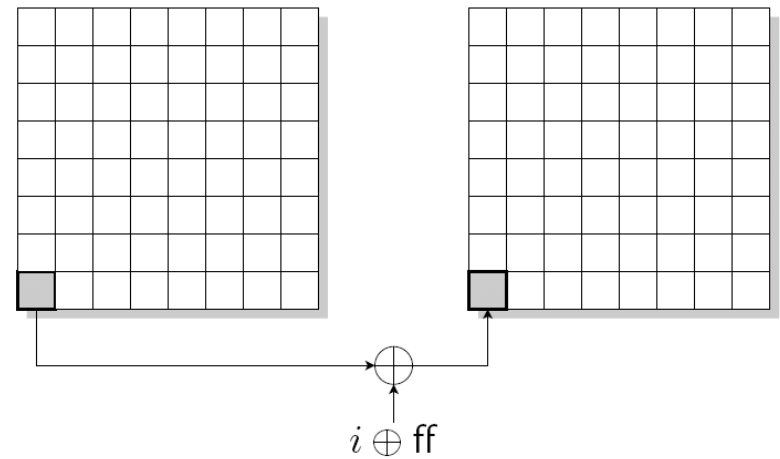
Grøstl-512:  
8x16 geometry

# AddRoundConstant

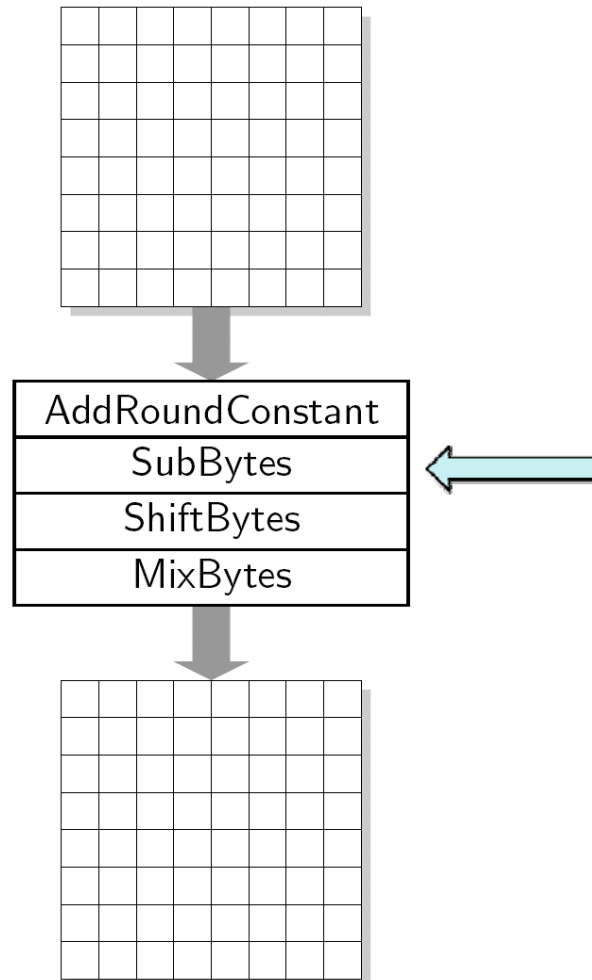
**P**



**Q**



# The State / Round Transformation



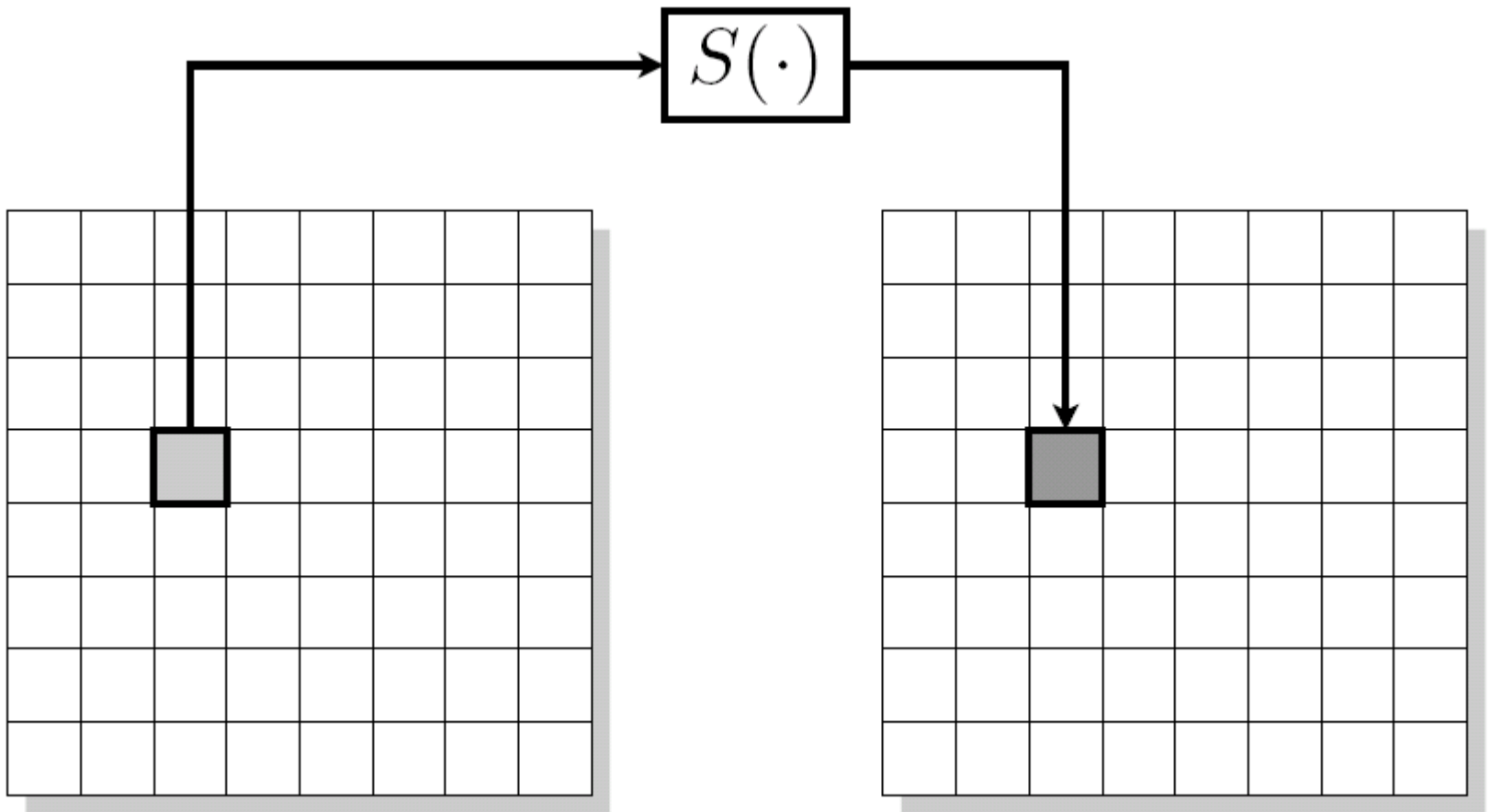
Grøstl-256:  
8x8 geometry

Grøstl-512:  
8x16 geometry

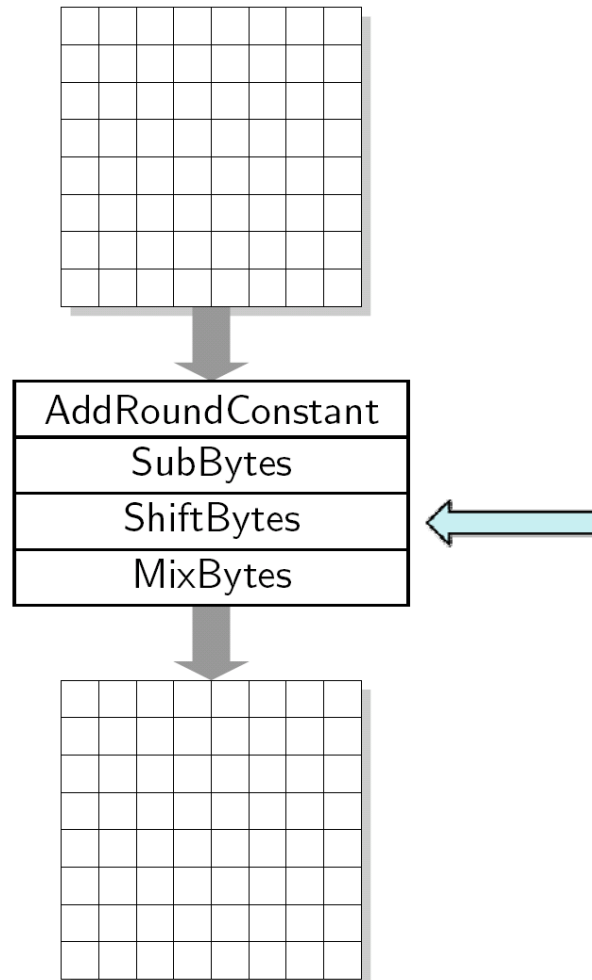


# SubBytes

same as the 8-bit AES Sbox



# The State / Round Transformation

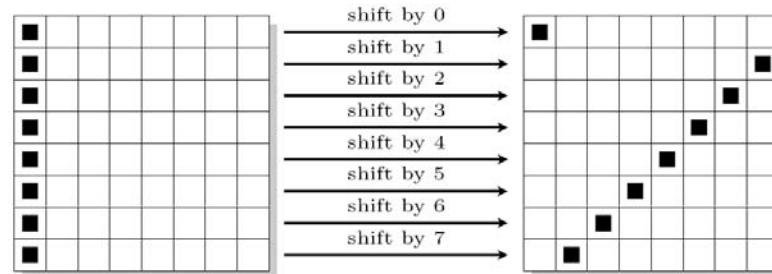


Grøstl-256:  
8x8 geometry

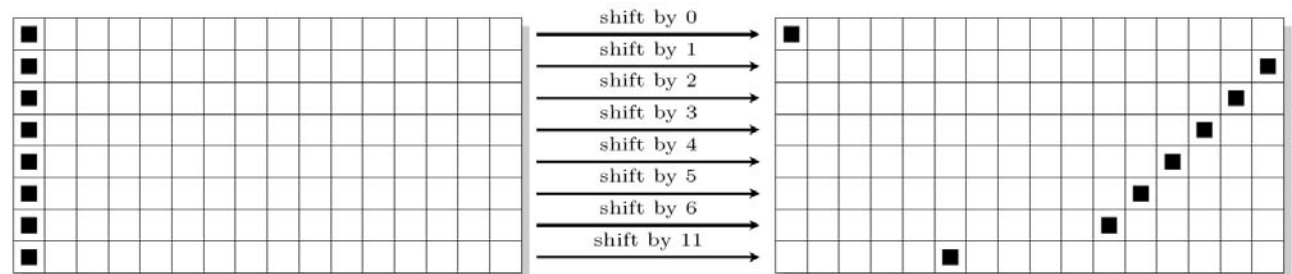
Grøstl-512:  
8x16 geometry

# ShiftBytes / ShiftBytesWide

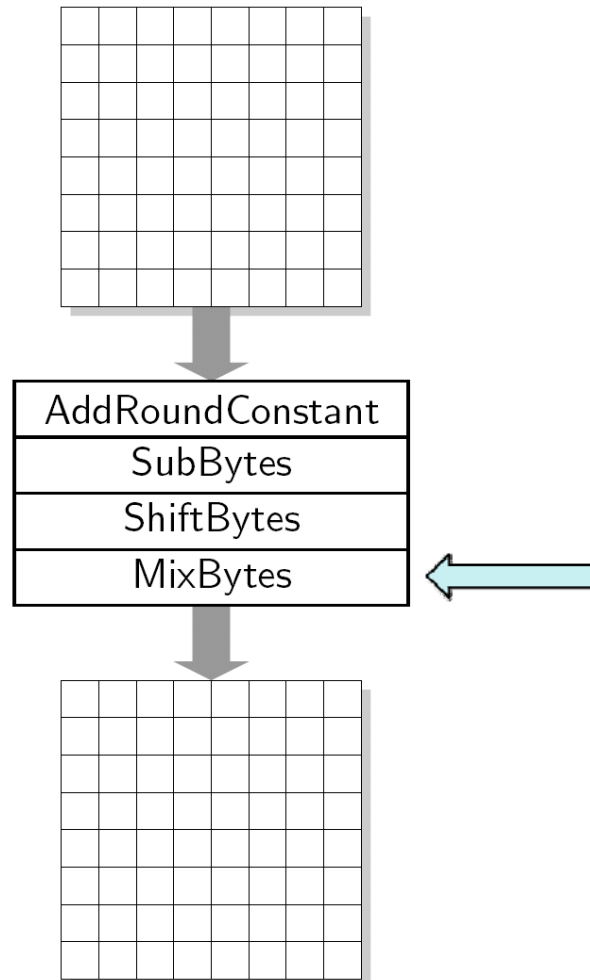
Grøstl-256



Grøstl-512



# The State / Round Transformation

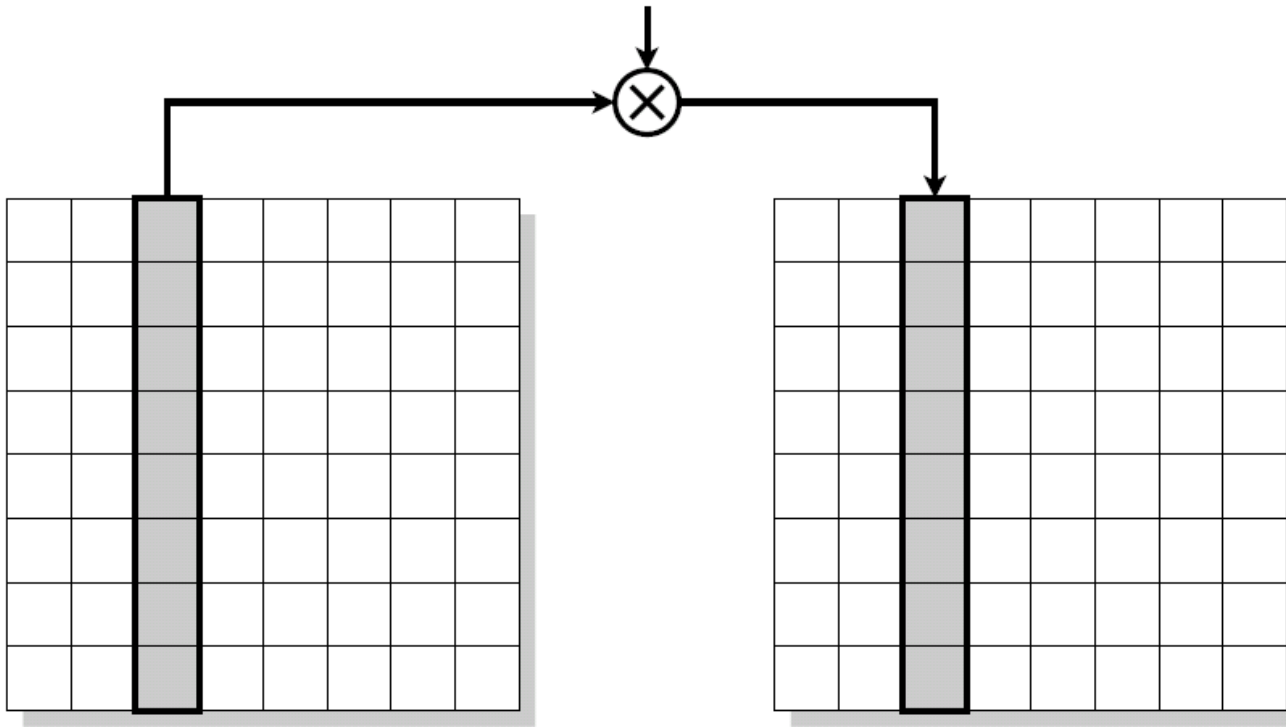


Grøstl-256:  
8x8 geometry

Grøstl-512:  
8x16 geometry

# MixBytes

$$B = \text{circ}(02, 02, 03, 04, 05, 03, 05, 07)$$



# Hardware Performance:

- Grøstl allows extremely flexible implementations  
various memory/gates/throughput/latency/... trade-offs

Some implementation results:

	<b>Area</b>	<b>Throughput(Gbits/s)</b>
<b>High throughput ASIC (0,18<math>\mu</math>m)</b>	58 kGates	6,30
<b>High throughput ASIC (0,18<math>\mu</math>m)</b>	50 kGates	2,70
<b>Low cost ASIC (0,18<math>\mu</math>m)</b>	19 kGates	0,90
<b>Low cost ASIC (0,18<math>\mu</math>m)</b>	16 kGates	0,33
<b>Spartan 3 FGPA</b>	6.5 kSlices	4,40
<b>Virtex 5 FGPA</b>	1,7 kSlices	10,20

# Proven track record:

Hash design experience:

Three published hash design proposals before Grøstl

Hash cryptanalysis experience:

(First/Best) attacks on  
MD2, (MD5), SHA family, FORK  
GOST, Tiger, Whirlpool, ...

Hash function cryptanalysis papers (last few years only):

CRYPTO (2), Eurocrypt (2), Asiacrypt (3), FSE(9), SAC (5), ...  
J. of Cryptology, IEEE Transactions on Information Theory, ...

# Grøstl SHA-3 cryptanalysis

Recent SHA-3 related breaks/cryptanalysis of the Grøstl team:

- Blender, JH, Sarmal, TIB3, Twister, Vortex, Boole, DCH, SHAMATA
- BMW, Essence, JH, Vortex, MeshHash, Tangle