Subject: OFFICIAL COMMENT: EDON-R
From: "Danilo Gligoroski" [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com)
Date: Mon, 15 Dec 2008 13:27:30 +0100
To: [hash-function@nist.gov](mailto:hash-function@nist.gov)
CC: [hash-forum@nist.gov](mailto:hash-forum@nist.gov)
Hi,
A new optimized C version of Edon-R hash function can be downloaded from: http://people.item.ntnu.no/~danilog/Hash/Additional_Implementations_edonr_Dec2008

With Intel C++ v11.0.061 for Windows it achieves the following speeds:
32-bit environment
Edon-R performance in Cycles/Byte with different message lengths in BYTES

|  |  | 1 | 10 | 100 | 1000 | 10000 | 100000 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| MD Size: 224 | 1801.00 | 182.50 | 33.13 | 7.22 | 6.43 | 6.46 |  |
| MD Size: 256 | 565.00 | 56.50 | 10.21 | 6.67 | 6.44 | 6.46 |  |
| MD Size: 384 | 1465.00 | 147.70 | 14.89 | 11.59 | 10.24 | 10.01 |  |
| MD Size: 512 | 1489.00 | 148.90 | 15.01 | 11.68 | 10.22 | 10.01 |  |

64-bit environment
Edon-R performance in Cycles/Byte with different message lengths in BYTES

|  |  | 1 | 10 | 100 | 1000 | 10000 | 100000 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| MD Size: 224 | 1441.00 | 144.10 | 24.25 | 4.92 | 4.56 | 4.41 |  |
| MD Size: 256 | 481.00 | 45.70 | 7.69 | 4.81 | 4.57 | 4.30 |  |
| MD Size: 384 | 529.00 | 49.30 | 4.93 | 2.44 | 2.26 | 2.29 |  |
| MD Size: 512 | 493.00 | 49.30 | 5.05 | 2.50 | 2.29 | 2.29 |  |

Regards,
Danilo Gligoroski

Subject: OFFICIAL COMMENT: EDON-R
From: "Danilo Gligoroski" [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com)
Date: Sun, 15 Mar 2009 18:02:54 +0100
To: [hash-function@nist.gov](mailto:hash-function@nist.gov)
CC: [hash-forum@nist.gov](mailto:hash-forum@nist.gov)
The memoryless meet-in-the-middle attack which is one part of the whole preimage attack of Khovratovich et. al. [1] on EDON-R hash function has complexity much bigger than $2^{\wedge}$ n.

We have showed that in the e-print note:
http://eprint.iacr.org/2009/120.pdf
Our analysis is based on the algorithm given by van Oorschot and Wiener in [2] for parallel memoryless meet-in-the-middle attack (which is based on the Floyd's memoryless algorithm).

Thus, the preimage attack of Khovratovich et. al. [1] on EDON-R is neither a threat nor a weakening of EDON-R.

Regards,
Danilo Gligoroski
[1] Dmitry Khovratovich, Ivica Nikoli’c, and Ralph-Philipp Weinmann. Meet-in-the-middle-attack on SHA-3 canditates.
In Fast Software Encryption - 2009, pages 233-250, 2009.
[2] Paul C. Van Oorschot and Michael J.Wiener.
Parallel collision search with cryptanalytic applications. Journal of Cryptology, 12:1-28, 1999.

Subject: Re: OFFICIAL COMMENT: EDON-R
From: Ivica Nikolic [cube444@gmail.com](mailto:cube444@gmail.com)
Date: Wed, 18 Mar 2009 08:06:55-0400
To: Multiple recipients of list [hash-forum@nist.gov](mailto:hash-forum@nist.gov)
Dear all,
we have two preliminary comments on this paper, both related to the cost estimation for the second block (Sec. 3)

1. It seems that the size of the space $R$ does not appear anywhere. In other words, if $|R|=1$ then the attacker still has to pay the cost given in Section 3?
2. The parameters $n \_1$ and $n \_2$ seem to be chosen arbitrarily. Where is the justification that these values are optimal for an attacker? In a traditional birthday attack (using memory), following the logic in the paper an attacker chooses $n \_l=n \_2=2^{\wedge} n$ and memory $2^{\wedge}\{n / 2\}$ and obtains T_m = 2^\{5n/4\}.

Best Regards, Ivica and Ralf

On Sun, Mar 15, 2009 at 6:08 PM, Danilo Gligoroski [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com) wrote: The memoryless meet-in-the-middle attack which is one part of the whole preimage attack of Khovratovich et. al. [1] on EDON-R hash function has complexity much bigger than $2^{\wedge} n$.

We have showed that in the e-print note:
http://eprint.iacr.org/2009/120.pdf

Our analysis is based on the algorithm given by van Oorschot and Wiener in
[2] for parallel memoryless meet-in-the-middle attack (which is based on the

Floyd's memoryless algorithm).

Thus, the preimage attack of Khovratovich et. al. [1] on EDON-R is neither
a threat nor a weakening of EDON-R.

Regards,
Danilo Gligoroski
[1] Dmitry Khovratovich, Ivica Nikoli’c, and Ralph-Philipp Weinmann. Meet-in-the-middle-attack on SHA-3 canditates.

In Fast Software Encryption - 2009, pages 233-250, 2009.
[2] Paul C. Van Oorschot and Michael J.Wiener.
Parallel collision search with cryptanalytic applications.
Journal of Cryptology, 12:1-28, 1999.
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Ivica Nikolic
Laboratory of Algorithms, Cryptography and Security, University of Luxembourg, 6, rue Richard Coudenhove-Kalergi, L-1359 Luxembourg-Kirchberg Luxembourg
Tel: +352 4666445490

# Subject: RE: OFFICIAL COMMENT: EDON-R <br> From: "Danilo Gligoroski" [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com) <br> Date: Wed, 18 Mar 2009 11:50:58-0400 <br> To: Multiple recipients of list [hash-forum@NIST.GOV](mailto:hash-forum@NIST.GOV) 

$>1$. It seems that the size of the space R does not appear anywhere. In other words,
$>$ if $|\mathrm{R}|=1$ then the attacker still has to pay the cost given in Section 3?
For the size of space R are you referring to our note or to the paper and analysis of van Oorschot and Wiener? In our note - on page 2 we say $|R|=2^{\wedge} n$ (i.e. $|R|=n \_2$ ).
> 2. The parameters n_1 and n_2 seem to be chosen arbitrarily. Where is the justification $>$ that these values are optimal for an attacker?

We did not choose the parameters n_1 and n_2. You did it in your attack.
You are defining two mappings f1: D1 --> R, and f2: D2 --> R, where |D1|=2^(n-65) because of the padding, and $|\mathrm{D} 2|=2 \wedge \mathrm{n}$ and then you are trying to find a meet-in-the-middle i.e. two values $a$ and $b$ such that $f 1(a)=f 2(b)$.
If you as attackers are complaining that these parameters are not optimal, then try to define a new attack.
$>$ In a traditional birthday attack (using memory), following the logic in the paper an attacker $>$ chooses n_1 = n_2 = 2^n and memory $2 \wedge\{n / 2\}$ and obtains T_m = $2^{\wedge}\{5 n / 4\}$.

Uff, this is serious. You haven't understood the van Oorschot and Wiener paper. The parallel memoryless birthday attack (finding collision) is described in section 5.2, and there the attack have complexity of $\mathrm{O}(\mathrm{Sqrt}(|\mathrm{R}|) / \mathrm{m}$ ) ( m is the number of processors) - equation (7).

Your attack on EDON-R is meet-in-the-middle attack, and its parallel memoryless equivalent is described in section 5.3 of van Oorschot and Wiener paper.

Best regards, Danilo!

From: hash-forum@nist.gov [mailto:hash-forum@nist.gov] On Behalf Of Ivica Nikolic
Sent: Wednesday, March 18, 2009 1:05 PM
To: Multiple recipients of list
Subject: Re: OFFICIAL COMMENT: EDON-R

Dear all,
we have two preliminary comments on this paper, both related to the cost estimation for the second block (Sec. 3)

1. It seems that the size of the space $R$ does not appear anywhere. In other words, if $|\mathrm{R}|=1$ then the attacker still has to pay the cost given in Section 3?
2. The parameters n_1 and n_2 seem to be chosen arbitrarily. Where is the justification that these values are optimal for an attacker? In a traditional birthday attack (using memory), following the logic in the paper an attacker chooses $n \_1=n \_2=2^{\wedge} n$ and memory $2 \wedge\{n / 2\}$ and obtains $T \_m=2 \wedge\{5 n / 4\}$.

Best Regards,
Ivica and Ralf

On Sun, Mar 15, 2009 at 6:08 PM, Danilo Gligoroski [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com) wrote:
The memoryless meet-in-the-middle attack which is one part of the whole preimage attack of Khovratovich et. al. [1] on EDON-R hash function has complexity much bigger than $2 \wedge n$.

We have showed that in the e-print note:
http://eprint.iacr.org/2009/120.pdf

Our analysis is based on the algorithm given by van Oorschot and Wiener in
[2] for parallel memoryless meet-in-the-middle attack (which is based on the

Floyd's memoryless algorithm).

Thus, the preimage attack of Khovratovich et. al. [1] on EDON-R is neither
a threat nor a weakening of EDON-R.

Regards,
Danilo Gligoroski
[1] Dmitry Khovratovich, Ivica Nikoli’c, and Ralph-Philipp Weinmann.
Meet-in-the-middle-attack on SHA-3 canditates.
In Fast Software Encryption - 2009, pages 233-250, 2009.



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##  <br>  <br>   <br>  <br>  <br>  <br>   <br>  <br>  <br>  <br>  <br>  <br>   <br> \begin{abstract} $\qquad$ <br> $\qquad$ <br> $$
8
$$ <br> . \end{abstract}



$$
\begin{aligned}
& \text { AL COMMENT: EDON-R } \\
& 2] \text { Paul C. Van } 0
\end{aligned}
$$



# -- 

$\qquad$

# $[$ P <br> - 



## Subject: Re: OFFICIAL COMMENT: EDON-R

From: gaetan.leurent@ens.fr (Gaëtan Leurent)
Date: Thu, 19 Mar 2009 08:57:24-0400
To: Multiple recipients of list [hash-forum@nist.gov](mailto:hash-forum@nist.gov)
I think that the misunderstanding about the complexity of the meet-in-the-middle comes from the fact that two different things can be called meet-in-the-middle:

1. You have a function $f$ and a function $g$, and you look for a single golden value ( $x, y$ ) that happens to satisfies $f(x)=g(y)$, and that you can test with some other property. This is what you do when you attack 2DES, for instance: you want to recover the secret key, and you use a meet-in-the-middle to get a small set of candidates, that you test using an other plaintext/ciphertext pair. The important point is that you need to get *all* the colliding pairs.
2. You have a function $f$ and a function $g$, and you look for any value $(x, y)$ such that $f(x)=g(y)$. Here you only need *one* colliding pair.

The paper by van Oorschot and Wiener refer to situation 1 when they talk about meet-in-the-middle. This is why their complexity figure depends on the size of the *domains* of the functions $f$ and $g$.

On the other hand, the attack of Khovratovich, Nikolic and Weinmann refers to situation 2. In this setting the cost of a meet-in-the-middle is essentially the same as the cost of a collision thanks to the switching function trick, and it only depends on the size of the *range* of the functions $f$ and $g$.

Gaëtan Leurent

Subject: Re: OFFICIAL COMMENT: EDON-R
From: gaetan.leurent@ens.fr (Gaëtan Leurent)
Date: Fri, 20 Mar 2009 07:47:49-0400
To: Multiple recipients of list [hash-forum@nist.gov](mailto:hash-forum@nist.gov)

Danilo Gligoroski wrote on 19 Mar 2009 15:24:13 +0100:
The second part of meet in the middle attack of Khovratovich and Nikolic preimage attack on EDON-R cannot be interpreted as a your situation 2. That is because Khovratovich and Nikolic define two mappings
f1: D1 $-->R$, and f2: D2 $-->R$, where $|D 1|=2^{\wedge}(n-65)$ because of the padding, and $|D 2|=2 \wedge n$ and $|R|=2^{\wedge n}$. And then they are trying to find one pair (a,b) such that $f 1(a)=f 2(b)$.

NOTE different domains D1 and D2, and NOTE the DIFFERENT SIZE of the DOMAINS!!!

Granted, that is a slight detail that needs to be taken care of.
But you can just reduce the domain D2 to something of size $2^{\wedge}(n-65)$. (say by fixing some bits to zero). This means that A8 will not take any value but stay in some subset. Since $2^{\wedge}(n-65)$ is bigger that $2^{\wedge}(n / 2)$, the meet-in-the-middle will still work, and it will be enough for the attack because they just need *any* match.

Regards,

Gaëtan Leurent
.
$\square$

```
                    *
```




Subject: RE: OFFICIAL COMMENT: EDON-R
From: "Danilo Gligoroski" [danilo.gligoroski@gmail.com](mailto:danilo.gligoroski@gmail.com)
Date: Mon, 23 Mar 2009 07:00:12-0400
To: Multiple recipients of list [hash-forum@nist.gov](mailto:hash-forum@nist.gov)
On Fri, 20 Mar 2009, Danilo Gligoroski wrote: Reducing the size of D2 addresses one of the attack problems but not the the first problem that D1 and D2 are different domains mapped WITH TWO DIFFERENT functions f1 and f2. That situation is not described in memoryless birthday attack of van Oorschot and Wiener paper, but in memoryless meet-in-the-middle attack.

On Mon, 23 Mar 2009, Stefan Lucks wrote:
In short, once you did solve the issue of two different domains for f1 and
f2, you can apply a memoryless birthday attack for MITM purposes.
(This is true if f1 and f2 run at roughly the same speed. If f1 is *much* slower than f2, you may want to modify $f: f(x)=f 1(x)$ if $x \bmod 2 \wedge k=0$ and $f(x)=f 2(x)$ else. In that case, you need $2 \wedge k f-c o l l i s i o n s$ for one f1-f2-collision. The benefit is, you need to call f1 less frequent.)

Hi Stefen,
*EXACTTLY* that is what I am saying:
***** FSE paper does not address issues of two different domains and different sizes! *****
***** HOW YOU ARE GOING TO SOLVE THE ISSUE OF TWO DIFFERENT DOMAINS? *****
I feel that in this discussion we are standing stubbornly on our positions offering
our own arguments and it is overloading the attention of all others members of this forum.

I propose instead of *patching* via this forum the old attack that is not working or has
so many undefined parts, the authors of that attack (or maybe you, or anybody else) should
publish a new attempt and a new attack.

1. In the analysis of the new attack, please precise how you are going to *"fuse"*
two domains D1 and D2 for two different functions f1() and f2().
2. Compute the "slowing down" factor with additional $2 \wedge$ k f-collisions (since one
of the functions is much slower than the other)!
3. EDON-R team will analyze that new attack and give the appropriate opinion.

Best regards,
Danilo!

From: hash-forum@nist.gov on behalf of Danilo Gligoroski [danilo.gligoroski@gmail.com]
Sent: Monday, May 25, 2009 5:40 PM
To: Multiple recipients of list
Subject: OFFICIAL COMMENT: EDON-R
Hi,
If EDON-R hash function would be accepted to go in the second round of NIST SHA-3 hash competition it will be tweaked by the following tweak:

Instead of the old compression function
R(oldPipe, M),
now the compression function have the following feedback:
R(oldPipe, M) xor oldPipe xor M',
where $M$ is represented in two parts i.e. $M=(M 0, M 1)$, and $M^{\prime}=(M 1$, M0) .

The introduced tweak does not invalidates the cryptanalytic efforts so far to analyze the quasigroup operations used in EDON-R, as well as its function $R($ ). It also does not affect much the speed of the function. However, this tweak prevents finding free-start collisions and prevents all attacks based on free-start collisions. With the introduced tweak EDON-R has a structure as a double-pipe PGV7 hash scheme, since the function R(oldPipe, M) is a bijection if the value of $M$ is kept fixed.

The speed of the optimized 32 -bit version on defined reference platform with Intel C++ v11.0.072 is 6.70 cycles/byte for $\mathrm{n}=224,256$ and 10.73 cycles/byte for $n=384,512$.

The speed of the optimized 64-bit version on defined reference platform with Intel C++ v11.0.072 is 4.87 cycles/byte for $\mathrm{n}=224,256$ and 2.70 cycles/byte for $n=384,512$.

The new package (documentation, source code, optimized code, new test values) can be downloaded from http://people.item.ntnu.no/~danilog/Hash/EdonRv20.zip

On behalf of the EDON-R team:
Danilo Gligoroski and Vlastimil Klima

| From: | Niels Ferguson [niels@microsoft.com] |
| :--- | :--- |
| Sent: | Friday, July 31, 2009 8:05 PM |
| To: | hash-function@nist.gov |
| Cc: | hash-forum@nist.gov |
| Subject: | OFFICIAL COMMENT: EDON-R |
| Attachments: | Edon-R-attack.pdf |

Peter Novotney and myself found detectable correlations in Edon-R.


#### Abstract

: The Edon-R compression function has a large set of useful differentials that produce easily detectable output bit biases. We show how to construct such differentials, and use them to create a distinguisher for Edon-R-512 that requires around $\$ 2^{\wedge}\{54\} \$$ compression function evaluations (or $\$ 2^{\wedge}\{28\} \$$ evaluations after a pre-computation of $\$ 2^{\wedge}\{66\} \$$ evaluations). The differentials can also be used to attack a variety of MAC and KDF constructions when they use Edon-R-512.


I have attached the paper; it should also appear soon on eprint.iacr.org as 2009/455

## Cheers!

Niels

# Detectable correlations in Edon- $\mathcal{R}$ 

Peter Novotney<br>peternov@microsoft.com

Niels Ferguson<br>niels@microsoft.com

July 31, 2009


#### Abstract

The Edon- $\mathcal{R}$ compression function has a large set of useful differentials that produce easily detectable output bit biases. We show how to construct such differentials, and use them to create a distinguisher for Edon- $\mathcal{R}$-512 that requires around $2^{54}$ compression function evaluations (or $2^{28}$ evaluations after a pre-computation of $2^{66}$ evaluations). The differentials can also be used to attack a variety of MAC and KDF constructions when they use Edon- $\mathcal{R}$-512.


## 1 Introduction

Edon- $\mathcal{R}$ [1] is one of the candidate hash functions in the NIST SHA-3 competition. ${ }^{1}$ It performs fewer operations per input bit than any of the other candidate functions. This makes it the fastest candidate by a significant margin [2], but also a tempting target for cryptanalysis.

One surprising property of Edon- $\mathcal{R}$ is that out of the 14 nonlinear bijective mappings used in the compression function, 7 have inputs that depend only on the message block and not on the previous chaining state. This allows the attacker to fully predict the propagation of values and differences in these functions. Due to the internal structure a differential from the message block can bypass another 4 nonlinear functions leaving only 3 'active' nonlinear functions that a differential has to pass through.

Our basic attack is a distinguishing attack. We show that an attacker can find two strings $L$ and $L^{\prime}$ such that the function $f: X \mapsto H(X \mid L) \oplus H\left(X \mid L^{\prime}\right)$

[^0]has easily detectable biases when $H$ is the Edon- $\mathcal{R}$ hash function. For an ideal hash function, $f$ behaves like a random mapping and does not have biases.

The attack can be extended to recover the intermediate hash state just before the last block, which breaks a number of common usage patterns for hash functions such as some KDF and MAC constructions.

## 2 An overview of Edon- $\mathcal{R}$

We give a short overview of those parts of Edon- $\mathcal{R}$ that are used in our attack. More details can be found in the Edon- $\mathcal{R}$ specifications [1].

Let $n \in\{256,512\}$ be the output size of the hash function. (The other output sizes are simple variations of these two sizes, which we will ignore.)
Given a message $M$ the first step is to pad it. We append a single ' 1 ' bit, and as many ' 0 ' bits as needed to make the length $2 n-64 \bmod 2 n$. We then append the length of $M$ as a 64 -bit integer to get a padded message whose length is a multiple of $2 n$ bits.

The padded message is split into $2 n$-bit blocks $M_{0}, \ldots, M_{k-1}$ where $k=$ $\lceil($ length $(M)+65) / 2 n\rceil$. The blocks are processed by iterating the compression function:

$$
\begin{aligned}
H_{0} & :=\text { some constant } \\
H_{i+1} & :=C\left(H_{i}, M_{i}\right)
\end{aligned}
$$

The chaining values $H_{i}$ are each $2 n$ bits long; the result of Edon- $\mathcal{R}$ consists of one half of the final chaining value $H_{k}$.

Our attack involves the last compression function, shown in figure 1. The lines are $n$-bit values; each $n$-bit value is internally represented as a vector of 8 words each of 32 bits (for the $n=256$ case) or 64 bits (for the $n=512$ case). At the top we have the two halves of the message block $M_{a}$ and $M_{b}$. The functions $f$ and $g$ are nonlinear bijections on $n$ bits, and $R$ is a function that reversed the order of the 8 words in the vector. The addition boxes represent word-by-word addition. The two halves of the chaining state come in as $H_{a}$ and $H_{b}$ and the final result of the hash function is $H$ at the bottom. The colors relate to some details of our attack and can be ignored for the moment.


Figure 1: Edon- $\mathcal{R}$ compression function

The $f$ and $g$ functions are the nonlinear elements used in Edon- $\mathcal{R}$. They have limited diffusion; each input bit will affect at least 15 of the output bits, but that is nowhere near full diffusion for a 256 -bit or 512 -bit function.

Our presentation is a little bit different from the one used in the Edon- $\mathcal{R}$ specifications. The Quasigroup operation $A * B$ from [1] can be written as $f(A)+g(B)$ where $f$ and $g$ can be expressed in terms of the $\pi$ functions from [1] section 2.1.2 as

$$
\begin{aligned}
f(x) & :=\pi_{1}\left(\pi_{2}(x)\right) \\
g(x) & :=\pi_{1}\left(\pi_{3}(x)\right)
\end{aligned}
$$

These are the $f$ and $g$ boxes in our figure. In the canonical description there are 16 of these functions. In two cases, the same function is applied twice to the same data; we have optimized that in our figure and have only $14 f$ and $g$ functions.

## 3 Our attack

Our attack is a differential attack. We treat the chaining value $\left(H_{a}, H_{b}\right)$ as unknown and try to find a differential from $\left(M_{a}, M_{b}\right)$ to $H$. If we can find an input difference that leads to a detectable bias in the output, then we have a distinguishing attack on Edon- $\mathcal{R}$.

In more detail, our attack finds a length $m$ and two strings $L$ and $L^{\prime}$ such that $H(X \mid L) \oplus H\left(X \mid L^{\prime}\right)$ has biased bits when $X$ varies over all $m$-bit strings. We always choose $m$ to be a multiple of $2 n$; we can then treat the hashing of $X$ as choosing a random chaining value $\left(H_{a}, H_{b}\right)$ as chaining input to the last compression function, and the strings $L$ consist of the message in the last message block.

We use the names of intermediate values as shown in figure 1. For the differential, $\left(H_{a}, H_{b}\right)$ is fixed; $C, D, E$, and $H$ are values in the compression function that processes $L$, and $C^{\prime}, D^{\prime}, E^{\prime}$, and $H^{\prime}$ values in the compression function that processes $L^{\prime}$.

To reduce the mixing of the message and the chaining value we always choose $L$ and $L^{\prime}$ such that $C=C^{\prime}$. This means that the white functions in the figure have inputs that do not change in our differential. The red Functions have inputs that depend only on the message, which is known. The green functions have inputs that depend only on the chaining value. The three yellow functions are the only ones whose inputs depend on both the message and the chaining value.

### 3.1 Biases when ignoring the padding

We first show how we can construct a differential from $\left(M_{a}, M_{b}\right)$ to $H$ if we ignore the padding that is always part of $M_{b}$. We choose a random fixed value for $C$ and choose low Hamming-weight values for $D$ and $D^{\prime}$. (Thus, $D$ and $D^{\prime}$ have most bits set to 0 .) As both $f$ and $g$ are invertible, these values determine $M_{a}, M_{b}, E, M_{a}^{\prime}, M_{b}^{\prime}$, and $E^{\prime}$.

| $w$ | median bias | largest bias |
| :---: | :---: | :---: |
| 1 | $\approx 2^{-2.9}$ | $\approx 2^{-1.7}$ |
| 2 | $\approx 2^{-3.6}$ | $\approx 2^{-2.7}$ |
| 4 | $\approx 2^{-5.8}$ | $\approx 2^{-4.6}$ |
| 6 | $\approx 2^{-8.4}$ | $\approx 2^{-6.1}$ |
| 8 | $\approx 2^{-11.6}$ | $\approx 2^{-10.3}$ |
| 10 | $\approx 2^{-13.6}$ | $\approx 2^{-10.9}$ |

Table 1: Biases of the most biased output bit for $D$ value of weight $w$

The values $H_{a}$ and $H_{b}$ represent the intermediate result of hashing the string $X$. To measure biases in $H(X \mid L) \oplus H\left(X \mid L^{\prime}\right)$ we choose random values for $\left(H_{a}, H_{b}\right)$ and compute the compression function with this chaining value and both $\left(M_{a}, M_{b}\right)$ and $\left(M_{a}^{\prime}, M_{b}^{\prime}\right)$ to get $H$ and $H^{\prime}$. We then look at the bits of $H \oplus H^{\prime}$ for biases taken over the random choice of the chaining values.

Our differential consists of two paths; a low Hamming-weight difference from D going down through two functions, and a heavy differential from $E$ going through one function. These two differences are combined to give the difference in $H$.

We experimentally measured the biases this produces in Edon- $\mathcal{R}-512$. For each maximum weight $w$ we ran 10 experiments. In each experiment we chose $C$ random, and chose $D$ and $D^{\prime}$ randomly in the set of all values with Hamming weight $w$. We then computed the corresponding $M_{a}, M_{a}^{\prime}$, $M_{b}, M_{b}^{\prime}, E$, and $E^{\prime}$, and finally computed $H \oplus H^{\prime}$ for $2^{30}$ random values of $\left(H_{a}, H_{b}\right)$. We then measured the bias of the most biased bit. Table 1 reports the median and largest bias of our 10 experiments for each of the maximum weights $w$. For a truly random function, we'd expect one of the 512 output bits to have a bias of around 3.1 standard deviations, which is a bias of $2^{-14.4}$ for our $2^{30}$ samples. As can be seen, the biases in Edon- $\mathcal{R}$ 512 are easily detectable. Even the median bias for $w=10$ is 5.2 standard deviations away from the mean.

### 3.2 Dealing with the padding

The procedure above does not produce an $M_{b}$ and $M_{b}^{\prime}$ with suitable padding. We can construct a differential that respects the padding rules using some more computing power.

| L | B9E8C2EB4052E4A897599BAE4E429C7015C5D754EA06AE2C1B7BD38706DA9EF4 <br>  <br>  <br>  <br>  <br>  <br> 3329A53CDD47883F63E72A67917E4BBF64983BB7E50B9C0CCBE9A04C23158B5F <br> 28687DBE5D5063EA85AFBDDD839DB59A1AFC715B4469EB056320447244C3B302 <br>  <br> 76A1020D19507242CD5E081FBCF17C793366B7D2BE63A285BF333E2F3E119427 |
| :--- | :--- |
|  | 5D57AE8FCA5E979AD6A78D0C4213D42A32DDFE07C394C2F4CD0140A1B44ECEE2 |
|  | 045CA1D71E9B634E0EA06AA3A4F00F3F73FB75DD3C11194DE92AF59AE360FF9C |
|  | CBB512243ABAE0A25FBFC6D8412E935B79B15F1188CC225FBF333E2F3E119427 |

Table 2: Trailing strings for $m=2851923422810615808$ with bias $2^{-6.6}$

To get the most freedom, we restrict ourselves to Edon- $\mathcal{R}-512$ and always choose our last message block to contain $2 n-65$ bits of message, one padding bit, and 64 bits of length encoding.

If we are given a length $m$ for the string $X$ then we have a 65 -bit restriction on the value of $M_{b}$ and $M_{b}^{\prime}$. We thus expect to have to try $2^{65}$ different values for $D$ before we find one with the right padding value. (There are $\binom{512}{10} \approx 2^{68}$ values of Hamming-weight 10 , so we can use $w=10$.) Another $2^{65}$ tries will produce a suitable value for $D^{\prime}$ so there is a one-off cost of $2^{66}$ to find suitable $L$ and $L^{\prime}$ for a given length $m$.

Thus, for any length of $X$ that is a multiple of $2 n$ we can, in about $2^{66}$ operations, find values for $L$ and $L^{\prime}$ that produce easily detectable biases.

If the length $m$ is only partially specified or can be freely chosen, we can do better. We choose random $D$ values in our low Hamming-weight set and we keep those whose corresponding $M_{b}$ has an acceptable length value. (There are 11 bits in $M_{b}$ that always have to have an exact value; the padding bit must be ' 1 ' and the 10 least significant bits of the length field must encode the integer $1024-65=959$.) Once we collect enough suitable values for $D$ we will find two that have the same length value.

We implemented this variant with no restriction on the length (other than the 11 bits mentioned above) and for length $m=2851923422810615808$ found the strings $L$ and $L^{\prime}$ which are shown, including the padding, in table 2. To generate such pairs we have to try $2^{11}$ values for $D$ to generate one valid $M_{b}$ value, and then collect $2^{27}$ valid $M_{b}$ values before we get a collision on the 54 remaining length bits. Thus the total computational cost of finding the $L$ 's is around $2^{38}$. This took less than a day on one of our
home machines. This pair produces an output bias in one bit of $2^{-6.6}$.
The bias produced by the $L$ values is easily measured by computing just the last block with random chaining inputs. But to measure the bias using only the full hash function requires the hashing of very long $X$ values. If we want to minimize the overall cost of creating the $L$ values and verifying the bias using the full hash function we can restrict $m$ to be at most $2^{k}$ for some $k$. We have to try $2^{11+64-k}$ values for $D$ to get a valid $M_{b}$ value, and then collect $2^{(k-10) / 2}$ valid $M_{b}$ values to create the collision on the length value. Finally, detecting a bias of $2^{-14}($ for $w=10)$ requires around $2^{28}$ evaluations each of which uses $2 \cdot 2^{k-10}$ block computations for a cost of $2^{k+19}$. The total cost is thus $2^{11+64-k+k / 2-5}+2^{k+19}=2^{70-k / 2}+2^{k+19}$ which is minimal when we choose $k \approx 34$. We thus estimate that finding suitable $L$ and $L^{\prime}$ values and then detecting the resulting bias on the full hash function can be done in about $2^{54}$ compression function evaluations.

### 3.3 Further attacks

Suppose we have an oracle with an unknown string $K$ that is a multiple of $2 n$ bits long. On input of a non-empty string $L$ the oracle returns $H(K \mid L)$. We can use our differentials to recover the intermediate state after hashing $K$, and thus impersonate the oracle in future.

We use our differentials in the same way differentials are used in key-recovery attacks on block ciphers. We think of $\left(H_{a}, H_{b}\right)$ as the 'key', the green functions in figure 1 as the key schedule, and the yellow functions as the block cipher. We generate a large set of differential pairs $\left(L, L^{\prime}\right)$ for the length of $K$. We then guess the value for one or more bits of the last 'round key' (e.g. the output of the lowest green $g$ function) and experimentally compute the expected bias for each of our differential pairs for this guess. We then compare that to the actual results. With enough ( $L, L^{\prime}$ ) pairs it quickly becomes obvious what the right value is for the key bit. Once we know a few of the key bits, the biases will tend to increase and make our work even simpler.

Our biases for $w=1$ are in the order of $2^{-3}$ so we need around $2^{6}$ differential pairs for one bit. (We can choose a new random $C$ value for each pair so we don't have to use heavier values for $D$.) It costs $2^{66}$ to produce each differential pair so the total cost of the attack is around $2^{72}$ per recovered bit. Thus, we expect that the full $\left(H_{a}, H_{b}\right)$ state can be recovered in around
$2^{16}$ queries and $2^{82}$ computational steps.
There are several common constructions that are susceptible to this type of attack. For example, many key derivation functions, including NIST SP80056 A , can be attacked in this way, giving the attacker the power to compute all derived keys.

Also $\operatorname{MAC}(K, M):=H(K \mid M)$ is a strong MAC function if $H$ is a good hash function, but our attack allows existential forgeries in around $2^{15}$ queries after a pre-computation of $2^{82}$ steps when Edon- $\mathcal{R}$ - 512 is used as the hash function.

### 3.4 Edon- $\mathcal{R}-256$

We have not tried our methods on Edon- $\mathcal{R}-256$. Because the block size is smaller the diffusion is slightly better, so we expect the workload of the attack to increase somewhat. We think it is likely that applying our techniques to Edon- $\mathcal{R}$-256 will result in an attack, but the computational cost might be too large for us to generate an actual example.

### 3.5 Possible improvements

Our attack is the result of a very preliminary analysis of Edon- $\mathcal{R}$. Rather than study the propagation of differentials through the Edon- $\mathcal{R}$ function we used brute computational force to show that correlations exist. This takes less time, but it ignores a lot of the structure of the function, and thus misses out on many opportunities to improve the attack. Below are just some of the areas that we believe improvements can be made in:
better differentials Our choices for $D$ and $D^{\prime}$ have been purely random in the set of values with weight $w$, and we have computed the resulting output biases experimentally. Even within the small set of experiments that we ran we found that some differences lead to much higher biases than other differences. A more detailed analysis of the differential propagation will no doubt result in ways of finding better differentials.
subtraction vs. xor We looked at $H(X \mid L) \oplus H\left(X \mid L^{\prime}\right)$, but given that the last operation in the compression function is an addition, it might be interesting to look at $H(X \mid L) \boxminus H\left(X \mid L^{\prime}\right)$ where $\boxminus$ is the word-
wise subtraction. This preserves the group structure of the last mixing operations and might lead to better biases.

Multi-bit correlations For simplicity we have limited ourselves to single bit biases. We expect that analyzing multiple output bits together (e.g. using a $\chi^{2}$ test) will produce biases that are more easily detectable.

More attention to detail In several places we ignore details that can help the attacker, or use a simple but pessimistic estimate of the effectiveness of the attack. A more detailed analysis should improve our attacks.

## 4 Comments on Edon- $\mathcal{R}$

Looking at figure 1 it is surprising to see how much processing is done on the message block without involving the chaining value. Half of the 14 nonlinear bijections have inputs that do not depend on the chaining value.

If we rewrite Edon- $\mathcal{R}$ a bit, we can think of the pair $(g(C), D)$ as the message block. The 7 red and white functions become an expensive message expansion function that computes a third block value $E$. The remaining 7 nonlinear functions perform the actual compression. In this representation the padding rule becomes complicated, but that affects only the last block.

Intuitively this feels like an inefficient use of computational resources. Half the time is spent in the message expansion to compute a single extra block that then affects the output of the compression function almost directly.

Another question is whether it is useful to apply the $f$ and $g$ functions to $H_{a}$ and $H_{b}$ respectively. These would be useful if an attacker could get nonrandom patterns in the chaining value, but an attacker that can do that can create non-random patterns in the hash function output too.

An alternate design for a compression function based on 14 nonlinear permutations would be to build a block cipher using a 14 -round Feistel network with a very simple key schedule, and run this in one of the standard hashing modes. This would achieve a similar speed as Edon- $\mathcal{R}$ in software, but it would seem to be much harder to attack.

### 4.1 Edon- $\mathcal{R}$ 's proof of security against differential cryptanalysis

In [1] section 3.5 the Edon- $\mathcal{R}$ submitters provide a proof that Edon- $\mathcal{R}$ is secure against differential cryptanalysis. They show that a single bit difference in $M_{a}$ or $M_{b}$ will not lead to a detectable difference patterns in the output.

We believe this analysis is incomplete. It shows that a single-bit input difference does not lead to a detectable output difference, but it does not take differentials into account that start out with many bits, then narrow down to one or just a few bits halfway through the computation, and then fan out again. From experience we know that the highest probability differentials are often of this form, and the proof provides no upper bound on their probability.

Our attack is exactly of that form. We have a big difference in the message block which narrows down to a low Hamming-weight difference halfway through the computation.

## 5 Acknowledgements

We would like to thank Danilo Gligoroski and the other members of the Edon- $\mathcal{R}$ team for their encouragement and support. They were also kind enough to provide us with the description of the inverse $f$ and $g$ functions.

## 6 Conclusion

Edon- $\mathcal{R}$ has insufficient mixing between the message block and the chaining state. This leads to message differentials with detectable biases in the output, which can be used to recover the chaining state input to the last compression function if the attacker controls only the last message block. This breaks a variety of protocols and algorithms in which hash functions are used.

## References

[1] Danilo Gligoroski, Rune Steinsmo Ødesgård, Marija Mihova, Svein Johan Knapskog, Ljupco Kocarev, Aleš Drápal, "Cryptographic Hash Function Edon-R" http://people.item.ntnu.no/~danilog/Hash/ Edon-R/Supporting_Documentation/EdonRDocumentation.pdf, Submission to NIST, 2008
[2] Skein team. "Engineering comparison of SHA-3 candidates", http:// www.skein-hash.info/sha3-engineering, retrieved April 19, 2009.

From: hash-forum@nist.gov on behalf of Danilo Gligoroski [danilo.gligoroski@gmail.com]
Sent: Saturday, August 01, 2009 3:15 AM
To: Multiple recipients of list
Subject: RE: OFFICIAL COMMENT: EDON-R
Hi ,
I can confirm findings reported in the paper of Novotney-Ferguson.
Namely, I have independently checked and repeated Ferguson-Novotney experiments and I can confirm that they are correct (Peter - thanks for your C source code).

Although there is a simple fix that Niels suggested in a private e-mail message to me, having in mind that EDON-R is not selected in 14 candidates of the second round SHA-3there is no point of considering its further fixing and development (until - as one mentioned on some forum - we have SHA-4 or NESSIE 2.0 competition for ultra-fast crypto primitives () hehe).

Best regards,
Danilo Gligoroski

From: hash-forum@nist.gov [mailto:hash-forum@nist.gov] On Behalf Of Niels Ferguson
Sent: Saturday, August 01, 2009 2:21 AM
To: Multiple recipients of list
Subject: OFFICIAL COMMENT: EDON-R
Peter Novotney and myself found detectable correlations in Edon-R.


#### Abstract

: The Edon-R compression function has a large set of useful differentials that produce easily detectable output bit biases. We show how to construct such differentials, and use them to create a distinguisher for Edon-R-512 that requires around $\$ 2^{\wedge}\{54\}$ \$ compression function evaluations (or $\$ 2^{\wedge}\{28\} \$$ evaluations after a pre-computation of $\$ 2^{\wedge}\{66\} \$$ evaluations). The differentials can also be used to attack a variety of MAC and KDF constructions when they use Edon-R-512.


I have attached the paper; it should also appear soon on eprint.iacr.org as 2009/455
Cheers!
Niels


[^0]:    ${ }^{1}$ As we were finalizing this paper, NIST announced the round 2 candidates for the SHA-3 competition. Edon- $\mathcal{R}$ was not selected for round 2.

