

Subject: OFFICIAL COMMENT: Vortex - simple correlation on some of the output bits

From: Niels Ferguson <niels@microsoft.com>

Date: Sun, 14 Dec 2008 17:38:29 -0800

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I think I found a simple correlation on some of the output bits of Vortex.

The hash result is the output of the V function. I'll use the notation of Figure 4 in the Vortex documentation, and use $X[0]$ to refer to the least significant bit of word X.

new_B0 and new_A0 are two of the output words of the function V.

new_B0[0] is a function of three bits B1[0], B0[0], and A0[0].

new_A0[0] is a function of three bits B0[0], A1[0], and A0[0].

These two functions share inputs and are correlated. $\text{new_B0}[0] = \text{new_A0}[0]$ with probability 5/8. This leads to a trivially detectable output bias, and makes the hash function unsuitable for many applications, including key derivation and Hash_DRBG from SP800-90.

Let's rename the four input bits to A, B, C, and D, and the two output bits to X and Y. We have:

$$X = (A \& D) \wedge B$$

$$Y = (B \& C) \wedge D$$

If $A=0$ then $X = B$ and $Y = \text{<some expression>} \wedge D$ so both output bits are uncorrelated and unbiased.

If $C=0$ the same applies.

But if $A=C=1$ we have

$$X = D \wedge B$$

$$Y = B \wedge D$$

and thus

$$X = Y$$

So 3/4 of the time the two output bits are unrelated, and 1/4 of the time they are the same, which leads to $X=Y$ for 5/8 of all inputs.

I haven't verified this experimentally, but the submitters of Vortex agreed with this analysis.

Cheers!

Niels

From: Michael Kounavis [michael_kounavis@hotmail.com]
Sent: Saturday, May 30, 2009 3:40 AM
To: hash-function@nist.gov
Cc: hash-forum@nist.gov
Subject: OFFICIAL COMMENT: Vortex - New paper and web page

Hello,

In response to the bit correlation remark posted by Niels and the other published attacks we have posted a new paper titled: "Security Enhancement of the Vortex Family of Hash Functions" that can be found in our algorithm's new web site: <http://math.haifa.ac.il/~vortex>

Regards
Shay and Michael