

Security Analysis of the 3rd Round SHA-3 Candidates BLAKE, Grøstl, JH, Keccak and Skein

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The Model

- **H** is SHA-3 candidate
- Security of **H** with **idealized**:
 - **F** compression f-n
 - **P, Q** permutations, **E** bl.cipher
- **This work**: ideal E, P, Q (lowest level primitive)

Upper bound maximal $\text{Adv}^{\text{atk}}_{\text{H}}(q)$ of any A in breaking some property **atk** of H with underlying primitives $\in \{E, P, Q\}$ after q queries.

- **atk** = NIST security requirements for SHA-3
- Security of **H** wrt $\text{atk} \in \{\mathbf{Col}, \mathbf{Sec}, \mathbf{Pre}\}$ and **Indif**

Reminder

$$\text{Adv}_H^{\text{atk}} \leq \text{Pr}_{\text{RO}}^{\text{atk}} + \text{Adv}_H^{\text{Indif}}$$

- $\text{Adv}_H^{\text{atk}=\{\text{Sec}, \text{Pre}, \text{Col}\}} \leq \max\{\text{Pr}_{\text{RO}}^{\text{atk}}, \text{Adv}_H^{\text{Indif}}\}$
- $\text{Pr}_{\text{RO}}^{\text{atk}}$ is success probability against atk generic attack on H, where H is viewed as a RO

Security Analysis of the 2nd Round SHA-3 Candidates [AMP10]

	type	sf	pf	(n, l, m)	$\text{Adv}_f^{\text{pre}}$	$\text{Adv}_f^{\text{pre}}$	$\text{Adv}_f^{\text{col}}$	$\text{Adv}_H^{\text{pre}}$	$\text{Adv}_H^{\text{pre}}$	$\text{Adv}_H^{\text{col}}$	$\text{Adv}_H^{\text{col}}$	$\text{Adv}_H^{\text{pre}}$
BLAKE	HAIFA	✓	✓	(256, 256, 512) or (512, 512, 1024)	PGV5-like E ideal		PGV5-like E ideal		$\Theta(q/2^n)$ f ideal	$\leq \text{Adv}_f^{\text{gcol}}$	$\Theta(q^2/2^n)$ f ideal	$\Theta(Kq^2/2^n)$ f ideal
BMW	chop-(MD+FT)	✓	✗	(256, 512, 512) or (512, 1024, 1024)	PGV3-like E ideal		PGV3-like E ideal			$\leq \text{Adv}_f^{\text{gcol}} + \text{Adv}_{\text{chop} \circ g}^{\text{gcol}}$		chopHMAC-like f ideal
CubeHash	chop-(MD+FT)	✗	✗	(256, 1024, 256) or (512, 1024, 256)	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$O\left(\frac{q}{2^n} + \frac{q^2}{2^{l-n}}\right)$ P ideal	$O\left(\frac{q}{2^n} + \frac{q^2}{2^{l-n}}\right)$ P ideal	(no preservation)	$\Theta(q^2/2^n)$ P ideal	$O((Kq)^2/2^{l-n})$ P ideal
ECHO	chop-HAIFA	✓	✓	(256, 512, 1536) or (512, 1024, 1024)	$\Theta(q/2^l)$ E ideal		$\Theta(q^2/2^l)$ E ideal		chop-HAIFA f ideal	$\leq \text{Adv}_{\text{chop} \circ f}^{\text{gcol}}$	$\Theta(q^2/2^n)$ E ideal (proof by preservation)	chopMD construction
Fugue	chop-(MD+FT)	✓	✗	(256, 960, 32) or (512, 1152, 32)	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal			(no preservation)		sponge-like P ideal
Grøstl	chop-(MD+FT)	✓	✗	(256, 512, 512) or (512, 1024, 1024)	$\Theta(q^2/2^l)$ P, Q ideal		$\Theta(q^4/2^l)$ P, Q ideal			$\leq \text{Adv}_f^{\text{gcol}} + \text{Adv}_{\text{chop} \circ g}^{\text{gcol}}$	$\Theta(q^2/2^n)$ P, Q ideal (proof by preservation)	$O((Kq)^4/2^l)$ P, Q ideal
Hamsi	MD+FT	✓	✗	(256, 256, 32) or (512, 512, 64)	$\Theta(q/2^n)$ P ideal		$\Theta(q^2/2^n)$ P ideal			$\leq \text{Adv}_f^{\text{gcol}} + \text{Adv}_g^{\text{gcol}}$	$\Theta(q^2/2^n)$ P, \tilde{P} ideal (proof by preservation)	NMAC-like f, g ideal
JH	chop-MD	✓	✗	(256, 1024, 512) or (512, 1024, 512)	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$O\left(\frac{q}{2^n} + \frac{q^3}{2^{l-n}}\right)$ P ideal	$O\left(\frac{q}{2^n} + \frac{q^3}{2^{l-n}}\right)$ P ideal	(no preservation)	$O\left(\frac{q^3}{2^n} + \frac{q^3}{2^{l-n}}\right)$ P ideal	$O\left(\frac{q^3}{2^{l-n}} + \frac{Kq^3}{2^{l-n}}\right)$ P ideal
Keccak	chop-MD	✗	✗	(256, 1600, 1088) or (512, 1600, 576)	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$\Theta(1)$ P ideal	$\Theta(q/2^n)$ P ideal	$\Theta(q/2^n)$ P ideal	(no preservation)	$\Theta(q^2/2^n)$ P ideal	$\Theta((Kq)^2/2^{l-n})$ P ideal
Luffa	chop-(MD+FT)	✗	✗	(256, 768, 256) or (512, 1278, 256)	$\Theta(1)$ P_i ideal	$\Theta(1)$ P_i ideal	$\Theta(1)$ P_i ideal			(no preservation)		sponge-like P_i ideal
Shabal	chop-MD	✓	✓	(256, 1408, 512) or (512, 1408, 512)			$O(q^2/2^{l-n})$ E ideal	$\Theta(q/2^n)$ E ideal	$O\left(\frac{q}{2^n} + \frac{q^2}{2^{l-n}}\right)$ E ideal	$\leq \text{Adv}_{\text{chop} \circ f}^{\text{gcol}}$	$\Theta(q^2/2^n)$ E ideal	$O((Kq)^2/2^{l-n})$ E ideal
SHAvite-3	HAIFA	✓	✓	(256, 256, 512) or (512, 512, 1024)	$\Theta(q/2^n)$ E ideal		$\Theta(q^2/2^n)$ E ideal		$\Theta(q/2^n)$ f ideal	$\leq \text{Adv}_f^{\text{gcol}}$	$\Theta(q^2/2^n)$ E ideal (proof by preservation)	$O((Kq)^2/2^n)$ E ideal
SIMD	chop-(MD+FT)	✓	✗	(256, 512, 512) or (512, 1024, 1024)	$\Theta(q/2^l)$ E ideal		$\Theta(q^2/2^l)$ E ideal			$\leq \text{Adv}_f^{\text{gcol}} + \text{Adv}_{\text{chop} \circ g}^{\text{gcol}}$	$\Theta(q^2/2^n)$ E, \tilde{E} ideal (proof by preservation)	chopMD construction
Skein	chop-MD	✓	✓	(256, 512, 512) or (512, 512, 512)	$\Theta(q/2^l)$ E ideal		$\Theta(q^2/2^l)$ E ideal	$O\left(\frac{q}{2^n} + \frac{q^2}{2^n}\right)$ E ideal	$O\left(\frac{q}{2^n} + \frac{q^2}{2^n}\right)$ E ideal	$\leq \text{Adv}_f^{\text{gcol}}$	$\Theta(q^2/2^n)$ E ideal (proof by preservation)	$O((Kq)^2/2^l)$ E ideal

NIST Requirements

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
BLAKE (256, 256, 512) (512, 512, 1024)								
Grøstl (256, 512, 512) (512, 1024, 1024)								
JH (256, 1024, 512) (512, 1024, 512)								
Keccak (256, 1600, 1088) (512, 1600, 576)								
Skein (256, 512, 512) (512, 512, 512)								
NIST requirements				256 512	256-L 512-L	128 256	-	

Earlier Results for BLAKE, Grøstl, JH, Keccak and Skein

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
BLAKE (256, 256, 512) (512, 512, 1024)				256 512	256 512	128 256	128 256	F
Grøstl (256, 512, 512) (512, 1024, 1024)	512 1024	512 1024	256 512	256 512	128 256	128 256	128 256	P, Q
JH (256, 1024, 512) (512, 1024, 512)	Insec Insec	Insec Insec	Insec Insec	170 170	170 170	128 256	170 170	P
Keccak (256, 1600, 1088) (512, 1600, 576)	Insec Insec	Insec Insec	Insec Insec	256 512	256 512	128 256	256 512	P
Skein (256, 512, 512) (512, 512, 512)	512 512	512 512	256 256	256 512	256 256	128 256	256 256	E
NIST requirements				256 512	256-L 512-L	128 256	-	

Our Objective

Provide “fair” security comparison for all H

- Focus on security analysis of H
- Security of all H based on ideal lower level primitives (E, P, Q, etc.)
- Tighten security results for H (where possible)
- Ideally: color uniformity in our previous table

BLAKE Old Results

(n, l, m) n output, l state, m msg.bl.	Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
BLAKE (256, 256, 512) (512, 512, 1024)				256 512	256 512	128 256	128 256	F
NIST requirements				256 512	256-L 512-L	128 256	-	

- If **F** ideal
 - Indif $2^{n/2}$
 - Pre, Sec, Col (HAIFA design)
- If **F** Col and Pre → BLAKE is Pre and Col (preservation)

BLAKE New Results

(n, l, m) n output, l state, m msg.bl.	Pre H	Sec H	Col H	Indif H	Ideal
BLAKE (256, 256, 512) (512, 512, 1024)	256 512	256 512	128 256	128 256	E
NIST requirements	256 512	256-L 512-L	128 256	-	

- **F** differentiable in $2^{n/4} \ll 2^{n/2}$ queries
- New: if **E** ideal:
 - Indif $2^{n/2}$
 - F is Pre and Col \rightarrow BLAKE is Pre and Col (preservation)
 - BLAKE Sec direct proof

E. Andreeva, A. Luykx and B. Mennink, "**Provable Security of BLAKE with Non-Ideal Compression Function**", *ePrint Archive, Report 2011/620*.

D. Chang, M. Nandi and M. Yung: "**Indifferentiability of the hash algorithm BLAKE**", *ePrint Archive, Report 2011/623*.

Grøstl Old Results

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
Grøstl (256, 512, 512) (512, 1024, 1024)	512 1024	512 1024	256 512	256 512	128 256	128 256	128 256	P, Q
NIST requirements				256 512	256-L 512-L	128 256	-	

- If P, Q ideal
 - Indif $2^{l/4} = 2^{n/2}$
 - Sec security implied by Indif (not optimal)
 - **F** is Col and Pre \rightarrow Grøstl is Pre and Col (preservation)

Grøstl New Result

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre H	Sec H	Col H	Indif H	Ideal
Grøstl (256, 512, 512) (512, 1024, 1024)	256 512	256 512	128 256	128 256	P, Q
NIST requirements	256 512	256-L 512-L	128 256	-	

- New: if **P, Q** ideal
 - Sec direct proof: obtain **optimal** security
 Proof: shows similarities with Sec proof of BLAKE

JH Old Result

(n, l, m) n output, l state, m msg.bl.		Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
JH	(256, 1024, 512)	-	-	-	170	170	128	170	P
	(512, 1024, 512)	-	-	-	170	170	256	170	
NIST requirements					256 512	256-L 512-L	128 256	-	

- Based on **P** (**F** is Col, Sec and Pre insecure)
- If **P** ideal
 - Pre, Sec implied by Indif 2^{170} (not optimal)
 - Col direct proof by Lee and Hong 2011

JH New Result

(n, l, m) <i>n output, l state, m msg.bl.</i>		Pre H	Sec H	Col H	Indif H	Ideal
JH	(256, 1024, 512)	256	256	128	170	P
	(512, 1024, 512)	256	256	256	170	
NIST requirements		256 512	256-L 512-L	128 256	-	

- New: if **P** ideal
 - Direct Pre proof (optimal for $n = 256$), (not optimal for $n = 512$)
 - Direct Sec proof (optimal for $n = 256$), (not optimal for $n = 512$)
- Proof
 - technical
 - graph-based: upper bound Pr to find a path from IV to final target hash value

Keccak

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
Keccak (256, 1600, 1088) (512, 1600, 576)	- -	- -	- -	256 512	256 512	128 256	256 512	P
NIST requirements				256 512	256-L 512-L	128 256	-	

- Based on **P** (**F** is Col, Sec and Pre insecure)
- Known results: If **P** ideal
 - Pre, Sec and Col implied by Indif $2^{(l-m)/2}$

Skein Old Results

(n, l, m) <i>n output, l state, m msg.bl.</i>		Pre F	Sec F	Col F	Pre H	Sec H	Col H	Indif H	Ideal
Skein	(256, 512, 512)	512	512	256	256	256	128	256	E
	(512, 512, 512)	512	512	256	512	256	256	256	
NIST requirements					256 512	256-L 512-L	128 256	-	

- Based on **E** (MMO type)
- Earlier: if **E** ideal
 - Indif $2^{l/2}$
 - F is Pre, Col \rightarrow Skein is Pre, Col secure (preservation)
 - Sec implied by Indif $2^{l/2}$ (not optimal Sec for 512-bit version)

Skein New Results

(n, l, m) <i>n output, l state, m msg.bl.</i>	Pre H	Sec H	Col H	Indif H	Ideal
Skein (256, 512, 512) (512, 512, 512)	256 512	256 512	128 256	256 256	E
NIST requirements	256 512	256-L 512-L	128 256	-	

- New: if **E** is ideal
 - Direct Sec proof (optimal for both $n = 256, 512$)
- Proof: shows similarities with Sec proof of BLAKE

Security Results for 256-bit Versions

	l	m	Pre	Sec	Col	Indif
BLAKE-256	256	512	256	256	128	128
Grøstl-256	512	512	256	256-L	128	128
JH-256	1024	512	256	256	128	170
Keccak-256	1600	1088	256	256	128	256
Skein-256	512	512	256	256	128	256
NIST requirements			256	256-L	128	-

Security Results for 512-bit Versions

	l	m	Pre	Sec	Col	Indif
BLAKE-512	512	1024	512	512	256	256
Grøstl-512	1024	1024	512	512-L	256	256
JH-512	1024	512	256	256	256	170
Keccak-512	1600	576	512	512	256	512
Skein-512	512	512	512	512	256	256
NIST requirements			512	512-L	256	-

Open Questions

- Standard model security proofs
(other than Col preservation)
- Improved **Indif** bounds
- JH-512 optimality for Sec and Pre security in the ideal model

Thank you!