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# Recommendation for Key-Derivation Methods in Key-Establishment Schemes

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C O M P U T E R   S E C U R I T Y

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22 **Revision 1**

23 **Recommendation for Key-Derivation**  
24 **Methods in Key-Establishment Schemes**

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105

### Abstract

106 This Recommendation specifies techniques for the derivation of keying material from a  
107 shared secret established during a key-establishment scheme defined in NIST Special  
108 Publications 800-56A or 800-56B.

109

110

### Keywords

111 Expansion; extraction; extraction-then-expansion; hash function; key derivation; key  
112 establishment; message authentication code.

113

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119 during the public comment periods, which helped to improve the quality of this publication.

120

### Conformance Testing

121 Conformance testing for implementations of the functions that are specified in this  
122 publication will be conducted within the framework of the Cryptographic Algorithm  
123 Validation Program (CAVP) and the Cryptographic Module Validation Program (CMVP).  
124 The requirements on these implementations are indicated by the word “shall.” Some of  
125 these requirements may be out-of-scope for CAVP or CMVP validation testing, and thus  
126 are the responsibility of entities using, implementing, installing, or configuring  
127 applications that incorporate this Recommendation.

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130

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159

160 **1 Introduction**

161 During the execution of a public-key-based key-establishment scheme specified in either  
 162 of the NIST Special Publications [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#), a key-derivation method  
 163 may be required to obtain secret cryptographic keying material. This Recommendation  
 164 specifies the key-derivation methods that can be used, as needed, in those key-  
 165 establishment schemes.

166

167 **2 Scope and Purpose**

168 This Recommendation specifies two categories of key-derivation methods that can be  
 169 employed, as required, as part of a key-establishment scheme specified in [\[SP 800-56A\]](#) or  
 170 [\[SP 800-56B\]](#).

171 The first category consists of a family of one-step key-derivation functions, which derive  
 172 keying material of a desired length from a shared secret generated during the execution of  
 173 a key-establishment scheme (and possibly other information as well).

174 The second category consists of an extraction-then-expansion key-derivation procedure,  
 175 which involves two steps:

- 176 1) Randomness extraction, to obtain a single cryptographic key-derivation key from a  
 177 shared secret generated during the execution of a key-establishment scheme, and
- 178 2) Key expansion, to derive keying material of the desired length from that key-  
 179 derivation key and other information. Since NIST's [\[SP 800-108\]](#) specifies several  
 180 families of key-derivation functions that are **approved** for deriving additional  
 181 keying material from a given cryptographic key-derivation key, those functions are  
 182 employed in the second (key-expansion) step of these two-step procedures.

183 In addition to the key-derivation methods whose specifications are provided in this  
 184 document, [\[SP 800-135\]](#) describes several variants (of both the one-step and two-step  
 185 methods) that are **approved** for specific applications.

186

187 **3 Definitions, Symbols and Abbreviations**

188 **3.1 Definitions**

<b>Approved</b>	FIPS approved or NIST Recommended. An algorithm or technique that is either 1) specified in a FIPS or NIST Recommendation, 2) adopted in a FIPS or NIST Recommendation or 3) specified in a list of NIST-approved security functions.
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Big-endian	<p>The property of a byte string having its bytes positioned in order of decreasing significance. In particular, the leftmost (first) byte is the most significant (containing the most significant eight bits of the corresponding bit string) and the rightmost (last) byte is the least significant (containing the least significant eight bits of the corresponding bit string).</p> <p>For the purposes of this Recommendation, it is assumed that the bits within each byte of a big-endian byte string are also positioned in order of decreasing significance (beginning with the most significant bit in the leftmost position and ending with the least significant bit in the rightmost position).</p>
Bit length	<p>The number of bits in a bit string. E.g., the bit length of the string 0110010101000011 is sixteen bits. The bit length of the empty (i.e., null) string is zero.</p>
Bit string	<p>An ordered sequence of bits (represented as 0's and 1's). Unless otherwise stated in this document, bit strings are depicted as beginning with their most significant bit (shown in the leftmost position) and ending with their least significant bit (shown in the rightmost position). E.g., the most significant (leftmost) bit of 0101 is 0, and its least significant (rightmost) bit is 1. If interpreted as the 4-bit binary representation of an unsigned integer, 0101 corresponds to five.</p>
Byte	<p>A bit string consisting of eight bits.</p>
Byte length	<p>The number of consecutive (non-overlapping) bytes in a byte string. For example, 0110010101000011 = 01100101    01000011 is two bytes long. The byte length of the empty string is zero.</p>
Byte string	<p>An ordered sequence of bytes, beginning with the most significant (leftmost) byte and ending with the least significant (rightmost) byte. Any bit string whose bit length is a multiple of eight can be viewed as the concatenation of an ordered sequence of bytes, i.e., a byte string. E.g., the bit string 0110010101000011 can be viewed as a byte string, since it is the concatenation of two bytes: 01100101 followed by 01000011.</p>

Estimated maximum security strength	An estimate of the largest security strength that can be attained by a cryptographic mechanism, given the explicit and implicit assumptions that are made regarding its implementation and supporting infrastructure (e.g., the algorithms employed, the selection of associated primitives and/or auxiliary functions, the choices for various parameters, the methods of generation and/or protection for any required keys, etc.). The estimated maximum security strengths of various <b>approved</b> cryptographic mechanisms are provided in <a href="#">[SP 800-57]</a> .
Concatenation	As used in this Recommendation, the concatenation, $X \parallel Y$ , of bit string $X$ followed by bit string $Y$ is the ordered sequence of bits formed by appending $Y$ to $X$ in such a way that the leftmost (i.e., initial) bit of $Y$ follows the rightmost (i.e., final) bit of $X$ .
Hash function	A function that maps a bit string of arbitrary length to a fixed-length bit string. <b>Approved</b> hash functions are designed to satisfy the following properties: <ol style="list-style-type: none"> <li>1. (One-way) It is computationally infeasible to find any input that maps to any pre-specified output, and</li> <li>2. (Collision resistant) It is computationally infeasible to find any two distinct inputs that map to the same output.</li> </ol> <b>Approved</b> hash functions are specified in <a href="#">[FIPS 180]</a> and <a href="#">[FIPS 202]</a> .
Key-derivation function	As used in this Recommendation, either a one-step key-derivation method, or a PRF-based key-derivation function as specified in <a href="#">[SP 800-108]</a> .
Key-derivation method	As used in this Recommendation, a process that derives keying material from a shared secret. This Recommendation specifies both one-step and two-step key-derivation methods.
Key-derivation procedure	As used in this Recommendation, a two-step key-derivation method consisting of randomness extraction followed by key expansion.
Key-derivation key	As used in this Recommendation, a key that is used during the key-expansion step of a key-derivation procedure to derive the output keying material. This key-derivation key is obtained from a shared secret during the randomness-extraction step.
Key establishment	A procedure that results in keying material that is shared among different parties.

Key expansion	The second step in the key-derivation procedure specified in this Recommendation, in which a key-derivation key is used to derive keying material having the desired length.
Keying material	As used in this Recommendation, a bit string output by a key-derivation method, that can be parsed into non-overlapping segments of appropriate bit lengths to provide the cryptographic keys and/or any other secret parameters required by the relying application.
Message Authentication Code (MAC) algorithm	<p>A family of cryptographic functions that is parameterized by a symmetric key. Each of the functions can act on input data (called a “message”) of variable length to produce an output value of a specified length. The output value is called the MAC of the input message. <math>MAC(k, x, \dots)</math> is used to denote the MAC of message <math>x</math> computed using the key <math>k</math> (and any additional algorithm-specific parameters). An <b>approved</b> MAC algorithm is expected to satisfy the following property (for each supported security strength):</p> <p style="padding-left: 40px;">Without knowledge of the key <math>k</math>, it must be computationally infeasible to predict the (as-yet-unseen) value of <math>MAC(k, x, \dots)</math> with a probability of success that is a significant improvement over simply guessing either the MAC value or <math>k</math>, even if one has already seen the results of using that same key to compute <math>MAC(k, x_j, \dots)</math> for (a bounded number of) other messages <math>x_j \neq x</math>.</p> <p>A MAC algorithm can be employed to provide authentication of the origin of data and/or to provide data-integrity protection. In this Recommendation, <b>approved</b> MAC algorithms are used to determine families of pseudorandom functions (indexed by the choice of key) that may be employed during key derivation; the use of MAC algorithms for key confirmation is addressed in <a href="#">[SP 800-56A]</a> and <a href="#">[SP 800-56B]</a>.</p>
Nonce	A varying value that has at most a negligible chance of repeating – for example, a random value that is generated anew for each use, a timestamp, a sequence number, or some combination of these.
Pseudorandom function family (PRF)	<p>An indexed family of (efficiently computable) functions, each defined for the same particular pair of input and output spaces. The indexed functions are pseudorandom in the following sense:</p> <p>If a function from the family is selected by choosing an index value uniformly at random, and one’s knowledge of the selected function is limited to the output values corresponding to a feasible number of (adaptively) chosen input values, then the selected function is computationally indistinguishable from a function chosen uniformly at random from the set of all possible functions mapping</p>

	the input space to the output space.
Randomness extraction	The first step in the two-step key-derivation procedure specified in this Recommendation; during this step, a key-derivation key is produced from a shared secret.
Salt	As used in this Recommendation, a byte string (which may be secret or non-secret) that is used as a MAC key by either 1) a MAC-based auxiliary function H employed in one-step key derivation, or, 2) a MAC employed in the randomness-extraction step during two-step key derivation.
Security strength	A number characterizing the amount of work that is expected to suffice to “defeat” an implemented cryptographic mechanism (e.g., by compromising its functionality and/or circumventing the protection that its use was intended to facilitate). In this Recommendation, security strength is measured in bits. If the security strength of a particular implementation of a cryptographic mechanism is $s$ bits, it is expected that the equivalent of (roughly) $2^s$ basic operations of some sort will be sufficient to defeat it in some way.
Shared secret	The secret byte string that is computed/generated during the execution of an <b>approved</b> key-establishment scheme and used as input to a key-derivation method as part of that transaction.
<b>Shall</b>	A requirement that needs to be fulfilled to claim conformance to this Recommendation. Note that <b>shall</b> may be coupled with <b>not</b> to become <b>shall not</b> .
Support (a security strength)	<p>A security strength of <math>s</math> bits is said to be supported by a particular choice of algorithm, primitive, auxiliary function, parameters (etc.) for use in the implementation of a cryptographic mechanism if that choice will not prevent the resulting implementation from attaining a security strength of at least <math>s</math> bits.</p> <p>In this Recommendation, it is assumed that implementation choices are intended to support a security strength of 112 bits or more (see <a href="#">[SP 800-57]</a> and <a href="#">[SP 800-131A]</a>).</p>
<b>Targeted security strength</b>	The maximum security strength that is intended to be supported by one or more implementation-related choices (such as algorithms, primitives, auxiliary functions, parameter sizes and/or actual parameters) for the purpose of implementing a cryptographic mechanism.

189 **3.2 Symbols and Abbreviations**

0x	A marker used to indicate that the following symbols are to be interpreted as a bit string written in hexadecimal notation (using the symbols 0, 1, ..., 9, and A, B, ..., F to denote 4-bit binary representations of the integers zero through nine and ten through fifteen, respectively). A byte can be represented by a hexadecimal string of length two; the leftmost hexadecimal symbol corresponds to the most significant four bits of the byte, and the rightmost hexadecimal symbol corresponds to the least significant four bits of the byte. For example, 0x9D represents the bit string 10011101 (assuming that the bits are positioned in order of decreasing significance).
AES	Advanced Encryption Standard (the block cipher specified in <a href="#">[FIPS 197]</a> ).
AES- $N$ ( $N = 128, 192, \text{ or } 256$ )	The variant of the AES block cipher that requires an $N$ -bit encryption/decryption key; the three variants specified in <a href="#">[FIPS 197]</a> are AES-128, AES-192, and AES-256.
AES-CMAC	The Cipher-based Message Authentication Code (CMAC) mode of operation for the AES block cipher, as specified in <a href="#">[SP 800-38B]</a> .
AES- $N$ -CMAC( $k, x$ ) ( $N = 128, 192, \text{ or } 256$ )	An implementation of AES-CMAC based on the AES- $N$ variant of the AES block cipher (for $N = 128, 192, \text{ or } 256$ ); its output is a 128-bit MAC computed over the “message” $x$ using the key $k$ .
<i>counter</i>	An unsigned integer, represented as a big-endian four-byte string, that is employed by the one-step key-derivation method specified in <a href="#">Section 4.1</a> .
<i>Context</i>	A bit string of context-specific data; a subcomponent of the <i>FixedInfo</i> that is included as part of the input to the two-step key-derivation method specified in <a href="#">Section 5.1</a> .
<i>default_salt</i>	A default value assigned to <i>salt</i> (if necessary) to implement an auxiliary function $H$ selected according to Option 2 or 3 in the one-step key-derivation method specified in <a href="#">Section 4.1</a> .
<i>DerivedKeyingMaterial</i>	Keying material that is derived from a shared secret $Z$ (and other data) through the use of a key-derivation method.

ECC	Elliptic curve cryptography.
$enc_8(x)$	A one-byte encoding of an integer $x$ , where $0 \leq x \leq 255$ , with bit 0 being the low-order (least significant) bit and bit 7 being the high-order (most significant) bit.
FFC	Finite field cryptography.
<i>FixedInfo</i>	A bit string of context-specific data whose value does not change during the execution of a key-derivation method specified in this Recommendation.
H	The auxiliary function used to produce blocks of keying material during the execution of the one-step key-derivation method specified in <a href="#">Section 4.1</a> .
<i>hash</i>	A hash function. Approved choices for <i>hash</i> are specified in <a href="#">[FIPS 180]</a> and <a href="#">[FIPS 202]</a> .
HMAC	Keyed-hash Message Authentication Code, as specified in <a href="#">[FIPS 198]</a> .
$HMAC\text{-}hash(k, x)$	An implementation of HMAC using the hash function <i>hash</i> ; its output is a MAC computed over “message” $x$ using the key $k$ .
$H\_outputlen$	A positive integer that indicates the length (in bits) of the output of either 1) the auxiliary function H used in the one-step key-derivation method specified in <a href="#">Section 4.1</a> , or, 2) an auxiliary HMAC algorithm used in the two-step key-derivation method specified in <a href="#">Section 5.1</a> .
IFC	Integer factorization cryptography.
<i>IV</i>	Initialization vector; as used in this Recommendation, it is a bit string used as an initial value during the execution of an <b>approved</b> PRF-based KDF operating in Feedback Mode, as specified in <a href="#">[SP 800-108]</a> .
KDF	Key-derivation function.
$K_{DK}$	The key-derivation key resulting from the randomness-extraction step and then used in the key-expansion step during the execution of the key-derivation procedure specified in <a href="#">Section 5.1</a> .
<i>KDM</i>	Key-derivation method.

KMAC	Keccak Message Authentication Code, as specified in <a href="#">[SP 800-185]</a> .
$KMAC\#(k, x, l, S)$	A variant of KMAC (either KMAC128 or KMAC256, as specified in <a href="#">[SP 800-185]</a> ); its output is an $l$ -bit MAC computed over the “message” $x$ using the key $k$ and “customization string” $S$ .
$L$	A positive integer specifying the desired length (in bits) of the derived keying material.
$[L]_2$	An agreed-upon encoding of the integer $L$ as a bit string.
MAC	Message Authentication Code.
$MAC(k, x, \dots)$	An instance of a MAC algorithm computed over the “message” $x$ using the key $k$ (and any additional algorithm-specific parameters).
$max\_H\_inputlen$	The maximum length (in bits) for strings used as input to the auxiliary function $H$ employed by the one-step key-derivation method specified in <a href="#">Section 4.1</a> .
<i>OtherInput</i>	A collective term for any and all additional data (other than the shared secret itself) used as input to a key-derivation method specified in this Recommendation.
PRF	Pseudorandom Function.
$s$	Security strength (in bits).
SHA	Secure Hash Algorithm, as specified in <a href="#">[FIPS 180]</a> (i.e., SHA-1, SHA-224, SHA-512/224, SHA-256, SHA-512/256, SHA-384, or SHA-512) or <a href="#">[FIPS 202]</a> (i.e., SHA3-224, SHA3-256, SHA3-384, or SHA3-512).
$Z$	Shared secret (determined according to the specifications in either <a href="#">[SP 800-56A]</a> or <a href="#">[SP 800-56B]</a> ).

190

191 **4 One-Step Key Derivation**

192 This section specifies a family of **approved** key-derivation functions (KDFs) that are  
 193 executed in a single step; a two-step procedure is specified in [Section 5](#). The input to each  
 194 specified KDF includes the shared secret generated during the execution of a key-  
 195 establishment scheme specified in [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#), an indication of the  
 196 desired bit length of the keying material to be output, and, perhaps, other information (as

197 determined by the particular implementation of the key-establishment scheme and/or key-  
198 derivation function).

199 Implementations of these one-step KDFs depend upon the choice of an auxiliary function  
200 H, which can be either 1) an **approved** hash function, denoted as *hash*, as defined in [FIPS  
201 180] or [FIPS 202]; 2) HMAC with an **approved** hash function *hash*, denoted as HMAC-  
202 *hash*, and defined in [FIPS 198]; or 3) a KMAC variant, as defined in [SP 800-185]. Tables  
203 1, 2, and 3 in Section 4.2 describe the possibilities for H, and also include any restrictions  
204 on the associated implementation-dependent parameters. H **shall** be chosen in accordance  
205 with the selection requirements specified in Section 7.

206 When an **approved** MAC algorithm (HMAC or KMAC) is used to define the auxiliary  
207 function H, it is permitted to use a known *salt* value as the MAC key. In such cases, it is  
208 assumed that the MAC algorithm will satisfy the following property (for each of its  
209 supported security strengths):

210 Given knowledge of the key  $k$ , and (perhaps) partial knowledge of a message  $x$  that  
211 includes an unknown substring  $z$ , it must be computationally infeasible to predict the  
212 (as-yet-unseen) value of  $\text{MAC}(k, x, \dots)$  with a probability of success that is a significant  
213 improvement over simply guessing either the MAC value or the value of  $z$ , even if one  
214 has already seen the values of  $\text{MAC}(k_j, x_j, \dots)$  for a feasible number of other  $(k_j, x_j)$   
215 pairs, where each key  $k_j$  is known and each (partially known) message  $x_j$  includes the  
216 same unknown substring  $z$ , provided that none of the  $(k_j, x_j)$  pairs is identical to  $(k, x)$ .

217 This property is consistent with the use of the MAC algorithm as the specification of a  
218 family of pseudorandom functions defined on the appropriate message space and indexed  
219 by the choice of MAC key. Under Option 2 and Option 3 of the KDF specification below,  
220 the auxiliary function H is a particular selection from such a family.

#### 221 4.1 Specification of Key-Derivation Functions

222 A family of one-step key-derivation functions is specified as follows:

223 **Function call:**  $\text{KDM}(Z, \text{OtherInput})$ .

#### 224 Options for the Auxiliary Function H:

225 Option 1:  $H(x) = \text{hash}(x)$ , where *hash* is an **approved** hash function meeting the  
226 selection requirements specified in Section 7, and the input,  $x$ , is a bit string.

227 Option 2:  $H(x) = \text{HMAC-hash}(salt, x)$ , where HMAC-*hash* is an implementation of the  
228 HMAC algorithm (as defined in [FIPS 198]) employing an **approved** hash  
229 function, *hash*, that meets the selection requirements specified in Section 7.  
230 An implementation-dependent byte string, *salt*, whose (non-null) value may  
231 be optionally provided in *OtherInput*, serves as the HMAC key, and  $x$  (the  
232 input to H) is a bit string that serves as the HMAC “message” – as specified  
233 in [FIPS 198].

234 Option 3:  $H(x) = \text{KMAC}\#(salt, x, H\_outputlen, S)$ , where KMAC# is a particular  
235 implementation of either KMAC128 or KMAC256 (as defined in [SP 800-

236 [185](#)) that meets the selection requirements specified in [Section 7](#). An  
 237 implementation-dependent byte string, *salt*, whose (non-null) value may be  
 238 optionally provided in *OtherInput*, serves as the KMAC# key, and *x* (the input  
 239 to H) is a bit string that serves as the KMAC# “message” – as specified in [\[SP](#)  
 240 [800-185\]](#). The parameter *H\_outputlen* determines the bit length chosen for  
 241 the output of the KMAC variant employed. The “customization string” *S* **shall**  
 242 be the byte string 01001011 || 01000100 || 01000110, which represents the  
 243 sequence of characters “K”, “D”, and “F” in 8-bit ASCII. (This three-byte  
 244 string is denoted by “KDF” in this document.)

#### 245 **Implementation-Dependent Parameters:**

- 246 1. *H\_outputlen* – a positive integer that indicates the length (in bits) of the output of the  
 247 auxiliary function, H, that is used to derive blocks of secret keying material. If Option  
 248 1 or Option 2 is chosen, then *H\_outputlen* corresponds to the bit-length of the output  
 249 block of the particular hash function used in the implementation of H; therefore,  
 250 *H\_outputlen* is in the set {160, 224, 256, 384, 512}, with the precise value determined  
 251 by the choice for *hash* (see [Section 4.2](#) for details). If Option 3 is chosen, then  
 252 *H\_outputlen* **shall** either be set equal to the length (in bits) of the secret keying  
 253 material to be derived (see input *L* below) or selected from the set {160, 224, 256,  
 254 384, 512}.
- 255 2. *max\_H\_inputlen* – a positive integer that indicates the maximum permitted length (in  
 256 bits) of the bit string, *x*, that is used as input to the auxiliary function, H. If Option 1  
 257 or Option 2 is chosen for the implementation of H, then an upper bound on  
 258 *max\_H\_inputlen* may be determined by the choice of *hash* (see [Section 4.2](#) for  
 259 details); *max\_H\_inputlen* values smaller than a specification-imposed upper bound  
 260 may be dictated by the particular use case. If *hash* is specified in [\[FIPS 202\]](#), or if  
 261 Option 3 is chosen for the implementation of H, then there is no specification-  
 262 imposed upper bound on *max\_H\_inputlen*; the value assigned to *max\_H\_inputlen*  
 263 may be determined by the needs of the relying applications/parties.
- 264 3. *default\_salt* – a (secret or non-secret) byte string that is needed only if either Option 2  
 265 (HMAC-*hash*) or Option 3 (KMAC#) is chosen for the implementation of the  
 266 auxiliary function H. This byte string is used as the value of *salt* if a (non-null) value  
 267 is not included in *OtherInput* (see below).

268 If  $H(x) = \text{HMAC-}hash(salt, x)$ , then, in the absence of an agreed-upon alternative, the  
 269 *default\_salt* **shall** be an all-zero byte string whose bit length equals that specified as  
 270 the bit length of an input block for the hash function, *hash*. (Input-block lengths for  
 271 the **approved** hash functions that can be employed to implement HMAC-*hash* are  
 272 listed in [Table 1](#) of [Section 4.2](#).)

273 If  $H(x) = \text{KMAC128}(salt, x, H\_outputlen, \text{“KDF”})$ , then, in the absence of an agreed-  
 274 upon alternative, the *default\_salt* **shall** be an all-zero string of 164 bytes (i.e., an all-  
 275 zero string of 1312 bits).

276 If  $H(x) = \text{KMAC256}(salt, x, H\_outputlen, \text{“KDF”})$ , then, in the absence of an agreed-  
 277 upon alternative, the *default\_salt* **shall** be an all-zero string of 132 bytes (i.e., an all-  
 278 zero string of 1056 bits).

279 **Input:**280 1.  $Z$  – a byte string that represents the shared secret.281 2. *OtherInput*, which includes:282 a.  $\{salt\}$  – a (secret or non-secret) byte string that can be (optionally) provided if  
283 either Option 2 (HMAC-*hash*) or Option 3 (KMAC#) is chosen for the  
284 implementation of the auxiliary function H, since those options require a *salt*  
285 value that is used as a MAC key.286 The *salt* included in *OtherInput* could be, for example, a value computed from  
287 nonces exchanged as part of a key-establishment protocol that employs one or  
288 more of the key-agreement schemes specified in [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#),  
289 a value already shared by the protocol participants, or a value that is pre-  
290 determined by the protocol. The possibilities for the length of *salt* are determined  
291 as follows:292 (1) The HMAC-*hash* algorithm as defined in [\[FIPS 198\]](#) can accommodate MAC  
293 keys of any bit length permitted for input to the hash function, *hash*.  
294 Therefore, when Option 2 is chosen, the length of the byte string *salt* can be  
295 as large as allowed for any string used as input to *hash*. However, if the bit  
296 length of *salt* is greater than the bit length specified for a single input block  
297 for *hash*, then the value of *salt* is replaced by  $hash(salt)$  as part of the HMAC  
298 computation. See [Table 2](#) for details.299 (2) The KMAC128 and KMAC256 algorithms specified in [\[SP 800-185\]](#) can  
300 accommodate MAC keys of any length up to  $2^{2040} - 1$  bits. Therefore, when  
301 Option 3 is chosen, *salt* can be a byte string of any agreed-upon length that  
302 does not exceed  $2^{2037} - 1$  bytes (i.e.,  $2^{2040} - 8$  bits). The input *salt* value will  
303 be (re)formatted (using a byte-padding function) during the execution of the  
304 KMAC algorithm to obtain a string whose length is a multiple of either 168  
305 bytes (for KMAC128) or 136 bytes (for KMAC256). See [Table 3](#) for details.306 If a *salt* value required by H is omitted from *OtherInput* (or if a required *salt* value  
307 included in *OtherInput* is the null string), then the value of *default\_salt* **shall** be  
308 used as the value of *salt* when H is executed.309 b.  $L$  – a positive integer that indicates the length (in bits) of the secret keying  
310 material to be derived;  $L$  **shall not** exceed  $H\_outputlen \times (2^{32} - 1)$ .311 ( $L = keydatalen$  in the notation of previous versions of [\[SP 800-56A\]](#), while  $L =$   
312  $KBits$  in the notation of [\[SP 800-56B\]](#).)313 c. *FixedInfo* – a bit string of context-specific data that is appropriate for the relying  
314 key-establishment scheme. As its name suggests, the value of *FixedInfo* does not  
315 change during the execution of the process described below.316 *FixedInfo* may, for example, include appropriately formatted representations of  
317 the values of *salt* and/or  $L$ . The inclusion of additional copies of the values of *salt*  
318 and  $L$  in *FixedInfo* would ensure that each block of derived keying material is  
319 affected by all of the information conveyed in *OtherInput*. See [\[SP 800-56A\]](#) and

320 [\[SP 800-56B\]](#) for more detailed recommendations concerning the format and  
321 content of *FixedInfo* (also known as *OtherInfo* in earlier versions those  
322 documents).

323 **Process:**

- 324 1. If  $L > 0$ , then set  $reps = \lceil L / H\_outputlen \rceil$ ; otherwise, output an error indicator  
325 and exit this process without performing the remaining actions (i.e., omit steps 2  
326 through 8).
- 327 2. If  $reps > (2^{32} - 1)$ , then output an error indicator and exit this process without  
328 performing the remaining actions (i.e., omit steps 3 through 8).
- 329 3. Initialize a big-endian 4-byte unsigned integer *counter* as 0x00000000,  
330 corresponding to a 32-bit binary representation of the number zero.
- 331 4. If  $counter \parallel Z \parallel FixedInfo$  is more than  $max\_H\_inputlen$  bits long, then output an  
332 error indicator and exit this process without performing any of the remaining  
333 actions (i.e., omit steps 5 through 8).
- 334 5. Initialize  $Result(0)$  as an empty bit string (i.e., the null string).
- 335 6. For  $i = 1$  to  $reps$ , do the following:
  - 336 6.1 Increment *counter* by 1.
  - 337 6.2 Compute  $K(i) = H(counter \parallel Z \parallel FixedInfo)$ .
  - 338 6.3 Set  $Result(i) = Result(i - 1) \parallel K(i)$ .
- 339 7. Set *DerivedKeyingMaterial* equal to the leftmost  $L$  bits of  $Result(reps)$ .
- 340 8. Output *DerivedKeyingMaterial*.

341 **Output:**

342 The bit string *DerivedKeyingMaterial* of length  $L$  bits (or an error indicator).

343 **Notes:**

344 In step 6.2 above, if  $H(x) = hash(x)$  or  $H(x) = HMAC-hash(salt, x)$ , the entire output  
345 block of the hash function *hash* **shall** be used when computing the output of  $H$ . Some  
346 **approved** hash functions (e.g., SHA-512/224, SHA-512/256, and SHA-384, as  
347 specified in [\[FIPS 180\]](#)) include an internal truncation operation. In such a case, the  
348 “entire output” of *hash* is the output block as defined in its specification. (For example,  
349 in the case of SHA-384, the entire output is defined to be a 384-bit block resulting from  
350 the internal truncation of a certain 512-bit value).

351 If  $H(x) = KMAC\#(salt, x, H\_outputlen, S)$ , then choosing  $H\_outputlen = L$  will likely  
352 be the most efficient way to produce the desired  $L$  bits of keying material.

353 The derived keying material *DerivedKeyingMaterial* **shall** be computed in its entirety  
354 before outputting any portion of it.

355 **4.2 The Auxiliary Function  $H(x)$  and Related Parameters**

356 Tables 1, 2, and 3 enumerate the possibilities for the auxiliary function  $H$  and provide  
 357 additional information concerning the values of related parameters such as  $H\_outputlen$   
 358 and  $max\_H\_inputlen$ . The tables also indicate the range of security strengths that can be  
 359 supported by each choice for  $H$  (when used as specified in [Section 4.1](#)).

360 **Table 1:  $H(x) = hash(x)$  (Option 1)**

Hash Function ( <i>hash</i> )	Byte / Bit Length of Input Blocks	$H\_outputlen$ (in bits) when $H = hash$	$max\_H\_inputlen$ (in bits) when $H = hash$	Security Strength $s$ supported by $H$ (in bits)
SHA-1	64 / 512	160	$\leq 2^{64} - 1$	$112 \leq s \leq 160$
SHA-224	64 / 512	224		$112 \leq s \leq 224$
SHA-256	64 / 512	256		$112 \leq s \leq 256$
SHA-512/224	128 / 1024	224	$\leq 2^{128} - 1$	$112 \leq s \leq 224$
SHA-512/256	128 / 1024	256		$112 \leq s \leq 256$
SHA-384	128 / 1024	384		$112 \leq s \leq 384$
SHA-512	128 / 1024	512		$112 \leq s \leq 512$
SHA3-224	144 / 1152	224	Arbitrarily long inputs can be accommodated.	$112 \leq s \leq 224$
SHA3-256	136 / 1088	256		$112 \leq s \leq 256$
SHA3-384	104 / 832	384		$112 \leq s \leq 384$
SHA3-512	72 / 576	512		$112 \leq s \leq 512$

361

362 **Table 2:  $H(x) = HMAC-hash(salt, x)$  (Option 2)**

Hash Function ( <i>hash</i> )	Effective Byte / Bit Length* of salt for HMAC-hash	$H\_outputlen$ (in bits) when $H = HMAC-hash$	$max\_H\_inputlen$ (in bits) when $H = HMAC-hash$	Security Strength $s$ supported by $H$ (in bits)
SHA-1	64 / 512	160	$\leq 2^{64} - 513$	$112 \leq s \leq 160$
SHA-224	64 / 512	224		$112 \leq s \leq 224$
SHA-256	64 / 512	256		$112 \leq s \leq 256$
SHA-512/224	128 / 1024	224	$\leq 2^{128} - 1025$	$112 \leq s \leq 224$
SHA-512/256	128 / 1024	256		$112 \leq s \leq 256$
SHA-384	128 / 1024	384		$112 \leq s \leq 384$
SHA-512	128 / 1024	512		$112 \leq s \leq 512$

SHA3-224	144 / 1152	224	Arbitrarily long inputs can be accommodated.	$112 \leq s \leq 224$
SHA3-256	136 / 1088	256		$112 \leq s \leq 256$
SHA3-384	104 / 832	384		$112 \leq s \leq 384$
SHA3-512	72 / 576	512		$112 \leq s \leq 512$

363 \* A shorter *salt* (used by H as an HMAC key) will be padded, by appending an all-zero  
 364 bit string, to obtain a string of the indicated length (the length of a single input block for  
 365 *hash*); a longer *salt* will be hashed to produce a shorter string (of bit length  $H\_outputlen$ ),  
 366 which will then be padded (by appending an all-zero bit string) to obtain a string of the  
 367 indicated length. (See [FIPS 198] for additional information.)

368 **Table 3:  $H(x) = KMAC\#(salt, x, H\_outputlen, \text{“KDF”})$  (Option 3)**

KMAC Variant (KMAC#)	Length of a byte-padded <i>salt</i> value	Suggested Maximum Byte Length of <i>salt</i> for KMAC#	$H\_outputlen$ (in bits) when $H = KMAC\#$	$max\_H\_inputlen$ (in bits) when $H = KMAC\#$	Security Strength $s$ supported by $H = KMAC\#$ (in bits)
KMAC128	Multiple of 168 bytes	$168 - 4 = 164$ **	Choice of 160, 224, 256, 384, 512, or $L$ .	Arbitrarily long inputs can be accommodated.	$112 \leq s \leq 128$
KMAC256	Multiple of 136 bytes	$136 - 4 = 132$ ***			$112 \leq s \leq 256$

369  
 370 \*\* Using 164 bytes (or less) leaves room for 4 bytes of prepended header information and  
 371 minimizes the length of `bytepad( encode_string(salt), 168 )`, which is the (re)formatted  
 372 value of *salt* used in the computation of  $KMAC128(salt, x, H\_outputlen, \text{“KDF”})$ :

373 
$$KMAC128(salt, x, H\_outputlen, \text{“KDF”}) = Keccak[256](String, H\_outputlen),$$

374 where *String* is the concatenation of

375 `bytepad( encode_string(“KDF”) || encode_string(“KMAC”), 168 )` and  
 376 `bytepad( encode_string(salt), 168 ) || x || right_encode( $H\_outputlen$ ) || 00`.

377 When *salt* is a 164-byte string, `bytepad( encode_string(salt), 168 )` is this 168-byte string:

378  $left\_encode(168) || encode\_string(salt) = enc_8(1) || enc_8(168) || enc_8(1) || enc_8(164) || salt$ .

379 If *salt* is shorter than 164 bytes, then the string `left_encode(168) || encode_string(salt)` is  
 380 padded as necessary (by appending an all-zero bit string) to obtain a 168-byte string. If *salt*  
 381 is any longer than 164 bytes, then `bytepad( encode_string(salt), 168 )` consists of two or  
 382 more 168-byte blocks.

383 \*\*\* Using 132 bytes (or less) leaves room for 4 bytes of prepended header information and

384 minimizes the length of  $\text{bytepad}(\text{encode\_string}(\textit{salt}), 136)$ , the (re)formatted value of  $\textit{salt}$   
 385 used in the computation of  $\text{KMAC256}(\textit{salt}, x, H\_outputlen, \text{"KDF"})$ :

386 
$$\text{KMAC256}(\textit{salt}, x, H\_outputlen, \text{"KDF"}) = \text{Keccak}[512](\textit{String}, H\_outputlen),$$

387 where  $\textit{String}$  is the concatenation of

388 
$$\text{bytepad}(\text{encode\_string}(\text{"KDF"}) \parallel \text{encode\_string}(\text{"KMAC"}), 136)$$
 and  
 389 
$$\text{bytepad}(\text{encode\_string}(\textit{salt}), 136) \parallel x \parallel \text{right\_encode}(H\_outputlen) \parallel 00.$$

390 When  $\textit{salt}$  is a 132-byte string,  $\text{bytepad}(\text{encode\_string}(\textit{salt}), 136)$  is this 136-byte string:

391 
$$\text{left\_encode}(136) \parallel \text{encode\_string}(\textit{salt}) = \text{enc}_8(1) \parallel \text{enc}_8(136) \parallel \text{enc}_8(1) \parallel \text{enc}_8(132) \parallel \textit{salt}.$$

392 If  $\textit{salt}$  is shorter than 132 bytes, then the string  $\text{left\_encode}(136) \parallel \text{encode\_string}(\textit{salt})$  is  
 393 padded as necessary (by appending an all-zero bit string) to obtain a 136-byte string. If  $\textit{salt}$   
 394 is any longer than 132 bytes, then  $\text{bytepad}(\text{encode\_string}(\textit{salt}), 136)$  consists of two or  
 395 more 136-byte blocks.

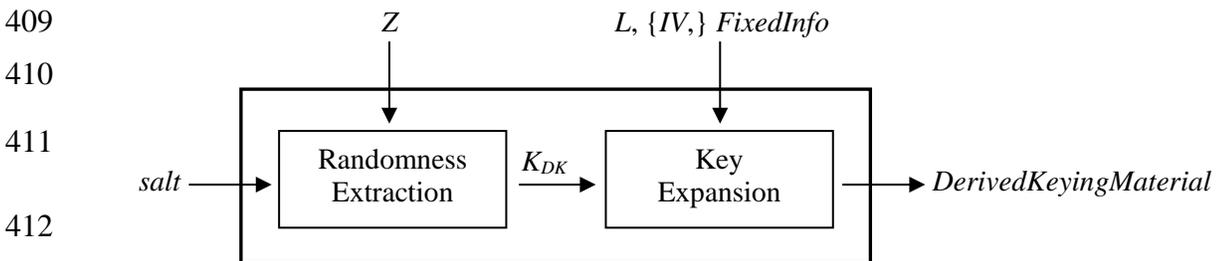
396 See [\[SP 800-185\]](#) for the definitions of  $\text{left\_encode}$ ,  $\text{right\_encode}$ ,  $\text{encode\_string}$ , and  
 397  $\text{bytepad}$ .

398

399 **5 Two-Step Key Derivation**

400 This section specifies an **approved** (two-step) extraction-then-expansion key-derivation  
 401 procedure. Like the one-step key-derivation functions described in [Section 4](#), the input to  
 402 this two-step procedure includes  $Z$ , the shared secret generated during the execution of a  
 403 key-establishment scheme that is specified in either [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#);  $L$ , a  
 404 positive integer indicating the desired length (in bits) of the output keying material; and  
 405 other information (as determined by the particular implementation of the key-establishment  
 406 scheme and/or key-derivation method). In contrast to the one-step methods, a  $\textit{salt}$  value is  
 407 required to be included as part of the input.

408 The extraction-then-expansion key-derivation procedure is pictured in [Figure 1](#).



413

**Figure 1: The Extraction-then-Expansion Key-Derivation Procedure**

414 The first (randomness-extraction) step uses either HMAC, as defined in [FIPS 198], or  
415 AES-CMAC, as defined in [SP 800-38B]. In either case, there are two inputs: *salt*, which  
416 serves as a MAC key, and the shared secret, *Z*, which serves as the “message.” The resulting  
417 MAC output is used as a key-derivation key,  $K_{DK}$ . The use of this  $K_{DK}$  is restricted to a  
418 single execution of the key-expansion step of this procedure.

419 The second (key-expansion) step uses the key-derivation key,  $K_{DK}$ , along with the integer  
420  $L$  and other appropriate data, as the input to a PRF-based key-derivation function specified  
421 in [SP 800-108]. The output returned by that key-derivation function is either secret keying  
422 material (in the form of *DerivedKeyingMaterial*, a bit string of length  $L$ ) or an error  
423 indicator.

## 424 5.1 Specification of Key-Derivation Procedure

425 The extraction-then-expansion key-derivation procedure is specified as follows:

426 **Function call:**  $KDM(Z, OtherInput)$ .

### 427 Options for the Auxiliary MAC Algorithm:

428 The MAC algorithm employed for randomness extraction **shall** be either an  
429 implementation of HMAC as defined in [FIPS 198], based on an **approved** hash  
430 function *hash* (i.e., HMAC-*hash*), or an implementation of AES-CMAC as defined in  
431 [SP 800-38B] (i.e., AES- $N$ -CMAC for  $N = 128, 192, \text{ or } 256$ ); in either case, the  
432 (untruncated) output of the MAC algorithm is used as the key-derivation key for  
433 subsequent key expansion. Tables 4 and 5 in Section 5.2 describe the possibilities for  
434 the auxiliary MAC algorithm, which **shall** be chosen in accordance with the selection  
435 requirements specified in Section 7.

### 436 Implementation-Dependent Auxiliary PRF-based KDF:

437 One of the general-purpose PRF-based key-derivation functions defined in [SP 800-  
438 108] **shall** be used for key expansion. These key-derivation functions employ an  
439 **approved** MAC algorithm as the PRF. In this Recommendation, the PRF used in key  
440 expansion is determined by the MAC algorithm that is used for randomness extraction.  
441 Specifically:

- 442 a. If HMAC-*hash* is used in the randomness-extraction step, then the same HMAC-  
443 *hash* (with the same hash function *hash*) **shall** be used as the PRF in the key-  
444 expansion step; and
- 445 b. If either AES-128-CMAC, AES-192-CMAC, or AES-256-CMAC is used in the  
446 randomness-extraction step, then only AES-128-CMAC (i.e., the CMAC mode of  
447 AES-128) **shall** be used as the PRF in the key-expansion step.

448 The rationale for these rules is discussed in Section 8.3.

449

450 **Input:**

- 451 1.  $Z$  – a byte string that represents the shared secret. It is used as the “message” during the  
452 execution of the MAC algorithm employed in the randomness-extraction step.
- 453 2. *OtherInput*, which includes:
- 454 a. *salt* – a (secret or non-secret) byte string used as the MAC key during the execution  
455 of the randomness-extraction step (i.e., step 1 in the process shown below). This  
456 *salt* could be, for example, a value computed from nonces exchanged as part of a  
457 key-establishment protocol that employs one or more of the key-agreement  
458 schemes specified in [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#), a value already shared by the  
459 protocol participants, or a value that is pre-determined by the protocol. The  
460 possibilities for the length of *salt* are determined by the auxiliary MAC algorithm  
461 that is used for randomness extraction:
- 462 (1) The HMAC-*hash* algorithm as defined in [\[FIPS 198\]](#) can accommodate keys of  
463 any length up to the maximum bit length permitted for input to the hash  
464 function, *hash*; therefore, the length of the byte string *salt* can be as large as  
465 allowed for any string used as input to *hash*. However, if the bit length of *salt*  
466 is greater than the bit length specified for a single input block for *hash*, then the  
467 value of *salt* is replaced by  $hash(salt)$  as part of the HMAC computation. (Input-  
468 block lengths for the **approved** hash functions that can be employed to  
469 implement HMAC-*hash* are included in column 4 of [Table 1](#) in Section 4.2;  
470 also see [Table 4](#) of Section 5.2.) In the absence of an agreed-upon alternative,  
471 the input *salt* value **shall** be an all-zero byte string whose length is equal to that  
472 of a single input block for *hash*.
- 473 (2) AES- $N$ -CMAC requires keys that are  $N$  bits long (for  $N = 128, 192,$  or  $256$ ),  
474 depending upon the AES variant that is used in the implementation. The bit  
475 length of *salt* **shall** be the bit length required of a key for that AES variant (128  
476 bits for AES-128, 192 bits for AES-192, or 256 bits for AES-256). In the  
477 absence of an agreed-upon alternative, the input *salt* value **shall** be an all-zero  
478 string of the required bit length.
- 479 b.  $L$  – a positive integer that indicates the length (in bits) of the secret keying material  
480 to be derived using the auxiliary PRF-based KDF during the execution of the key-  
481 expansion step (i.e., step 2 in the process shown below). The maximum value  
482 allowed for  $L$  is determined by the mode (i.e., Counter Mode, Feedback Mode, or  
483 Double-Pipeline Iteration Mode) and implementation details of the chosen KDF, as  
484 specified in [\[SP 800-108\]](#). An error event will occur during the execution of the  
485 KDF if  $L$  is too large.<sup>1</sup>

---

<sup>1</sup> The restrictions on the size of  $L$  that are given in [\[SP 800-108\]](#) are stated in terms of  $n = \lceil L/h \rceil$ , where  $h$  denotes the bit length of an output block of the PRF used to implement the auxiliary KDF. In the case of Counter Mode, the restriction is  $n \leq 2^r - 1$ , where  $r \leq 32$  is the (implementation-dependent) bit length allocated for the KDF's counter variable. For

486 (Note that  $L = \textit{keydatalen}$  in the notation of previous versions of [\[SP 800-56A\]](#),  
487 while  $L = \textit{KBits}$  in the notation of [\[SP 800-56B\]](#).)

488 c.  $\{IV\}$  – a bit string included (if required) for use as an initial value during execution  
489 of the auxiliary PRF-based KDF; an  $IV$  **shall** be included in *OtherInput* if and only  
490 if the chosen PRF-based KDF is operating in Feedback Mode. It can be either secret  
491 or non-secret. It may be an empty string. If the PRF-based KDF is operating in  
492 either Counter Mode or Double-Pipeline Iteration Mode, an  $IV$  **shall not** be  
493 included in *OtherInput*. (See [\[SP 800-108\]](#) for details.)

494 d. *FixedInfo*, including:

495 (1) *Label* – a bit string that identifies the purpose for the derived keying material.  
496 For example, it can be the ASCII code for a character string. The value and  
497 encoding method used for the *Label* are defined in a larger context, for example,  
498 in the protocol that uses this key-derivation procedure. As an alternative to  
499 including this string as a separate component of *FixedInfo*, *Label* could be  
500 incorporated in *Context* (see below).

501 (2) *Context* – a bit string of context-specific data appropriate for the relying key-  
502 establishment scheme/protocol and the chosen PRF-based KDF.

503 For recommendations concerning the format and context-specific content of  
504 *Context*, see the specifications of *FixedInfo* and/or *OtherInfo* in [\[SP 800-56A\]](#)  
505 and/or [\[SP 800-56B\]](#), respectively.

506 (3)  $[L]_2$  – an agreed-upon encoding of  $L$  as a bit string that is appropriate for use by  
507 the chosen PRF-based KDF (see [\[SP 800-108\]](#) for details). As an alternative to  
508 including this string as a separate component of *FixedInfo*,  $[L]_2$  could be  
509 incorporated in *Context* (see above).

510 **Process:**

511 **[Randomness Extraction]**

512 1. Call  $\text{MAC}(salt, Z, \dots)$  to obtain  $K_{DK}$  or an error indicator; if an error occurs, output  
513 an error indicator, and exit from this process without performing step 2.

514 **[Key Expansion]**

515 2. Call  $\text{KDF}(K_{DK}, L, \{IV\}, \textit{FixedInfo})$  to obtain *DerivedKeyingMaterial* or an error  
516 indicator (see [\[SP 800-108\]](#) for details). If an error occurs, output an error indicator;  
517 otherwise output *DerivedKeyingMaterial*.

---

the other KDF modes, the restriction is simply  $n \leq 2^{32} - 1$ .

518 **Output:**519 The bit string *DerivedKeyingMaterial* of length  $L$  bits (or an error indicator).520 **Notes:**

521 When HMAC-*hash* is used as the auxiliary MAC algorithm, the length of  $K_{DK}$  is the  
 522 length of an (untruncated) output block from the hash function *hash*. When AES-  
 523 CMAC is used, then (regardless of the AES variant employed)  $K_{DK}$  is a 128-bit binary  
 524 string.  $K_{DK}$  is used (locally) as a key-derivation key by the auxiliary KDF during the  
 525 key-expansion step, and then **shall be** destroyed (along with all other sensitive locally  
 526 stored data) after its use. Its value **shall not** be an output of the key-derivation  
 527 procedure.

528 [\[RFC 5869\]](#) specifies a version of the above extraction-then-expansion key-derivation  
 529 procedure using HMAC for both the extraction and expansion steps. For an extensive  
 530 discussion concerning the rationale for the extract-and-expand mechanisms specified in  
 531 this Recommendation, see [\[LNCS 6223\]](#).

532 **5.2 The Auxiliary MAC Algorithm and Related Parameters**

533 Tables [4](#) and [5](#) enumerate the possibilities for the auxiliary MAC algorithm used for  
 534 randomness extraction and provide additional information concerning the lengths of the  
 535 MAC key (i.e., the *salt* value) and the extracted key-derivation key (i.e.,  $K_{DK}$ ). The tables  
 536 also indicate the range of security strengths that can be supported by each choice for MAC  
 537 (when used as specified in [Section 5.1](#)).

538 **Table 4: MAC(*salt*, *Z*, ...) = HMAC-*hash*(*salt*, *Z*) (For Randomness Extraction)**

Hash Function ( <i>hash</i> )	Effective Byte / Bit Length* of <i>salt</i> for HMAC- <i>hash</i>	Bit Length of Extracted $K_{DK}$	Security Strength $s$ supported (in bits)
SHA-1	64 / 512	160	$112 \leq s \leq 160$
SHA-224	64 / 512	224	$112 \leq s \leq 224$
SHA-256	64 / 512	256	$112 \leq s \leq 256$
SHA-512/224	128 / 1024	224	$112 \leq s \leq 224$
SHA-512/256	128 / 1024	256	$112 \leq s \leq 256$
SHA-384	128 / 1024	384	$112 \leq s \leq 384$
SHA-512	128 / 1024	512	$112 \leq s \leq 512$
SHA3-224	144 / 1152	224	$112 \leq s \leq 224$
SHA3-256	136 / 1088	256	$112 \leq s \leq 256$
SHA3-384	104 / 832	384	$112 \leq s \leq 384$
SHA3-512	72 / 576	512	$112 \leq s \leq 512$

539  
540 \* A shorter *salt* (which is used as an HMAC key) will be padded, by appending an all-zero  
541 bit string, to obtain a string of the indicated length (the length of a single input block for  
542 *hash*); a longer *salt* will be hashed to produce a shorter string, which will then be padded  
543 (by appending an all-zero bit string) to obtain a string of the indicated length. (See [FIPS  
544 [198](#)] for additional information.)

545 **Note:** The *hash* used by the HMAC algorithm employed during randomness extraction  
546 **shall** be used again in the subsequent key-expansion step to implement the HMAC  
547 algorithm that is employed as a PRF by the auxiliary PRF-based KDF.

548 **Table 5: MAC( *salt*, Z, ... ) = AES-N-CMAC( *salt*, Z ) (For Randomness Extraction)**

AES Variant used by AES-CMAC	Bit Length of <i>salt</i> for AES-CMAC	Bit Length of Extracted $K_{DK}$	Security Strength $s$ supported (in bits)
AES-128	128	128	$112 \leq s \leq 128$
AES-192	192		
AES-256	256		

549  
550 **Note:** Regardless of which AES variant is used by the AES-CMAC algorithm during  
551 randomness-extraction, the 128-bit AES block size determines the bit length of the  
552 resulting  $K_{DK}$ . To accommodate the use of this 128-bit  $K_{DK}$  as a key-derivation key, the  
553 CMAC mode of AES-128 **shall** be the PRF employed by the auxiliary PRF-based KDF in  
554 the subsequent key-expansion step.

555 **6 Application-Specific Key-Derivation Methods**

556 Additional **approved** application-specific key-derivation methods are enumerated in  
557 [\[SP 800-135\]](#). Unless an explicit exception is made in [\[SP 800-135\]](#), any hash or MAC  
558 algorithm employed by the key-derivation methods enumerated in [\[SP 800-135\]](#) **shall** be  
559 **approved** and **shall** also meet the selection requirements specified in this Recommendation  
560 (i.e., SP 800-56C).

561 **7 Selecting Hash Functions and MAC Algorithms**

562 The key-derivation methods specified in this Recommendation, as well as those  
563 enumerated in [\[SP 800-135\]](#), use hash functions and/or message authentication code  
564 (MAC) algorithms as auxiliary functions. In particular:

- 565 • The one-step key-derivation functions that are specified in [Section 4.1](#) of this  
566 Recommendation employ an appropriate choice of hash function (*hash*), an HMAC  
567 algorithm based on an appropriate choice of hash function (HMAC-*hash*), or one

568 of two KMAC variants (KMAC128 or KMAC256) to implement the auxiliary  
569 function H.

- 570 • The extraction-then-expansion key-derivation procedure specified in [Section 5.1](#)  
571 employs either an HMAC algorithm based on an appropriate choice of hash  
572 function (HMAC-*hash*) for both randomness extraction and key expansion, or an  
573 appropriate variant of the AES-CMAC algorithm (i.e., AES-*N*-CMAC for  $N = 128$ ,  
574 192, or 256) for randomness extraction together with AES-128-CMAC for key  
575 expansion.

576 Unless explicitly stated to the contrary, (e.g., in [\[SP 800-135\]](#)), the following requirements  
577 apply to the hash functions and MAC algorithms employed for key derivation:

- 578 • Whenever a hash function is employed (including as the primitive used by HMAC),  
579 an **approved** hash function **shall** be used. [\[FIPS 180\]](#) and [\[FIPS 202\]](#) specify  
580 **approved** hash functions.
- 581 • Whenever an HMAC algorithm is employed, the HMAC implementation **shall**  
582 conform to the specifications found in [\[FIPS 198\]](#).
- 583 • Whenever a KMAC variant (KMAC128 or KMAC256) is employed, the KMAC  
584 implementation **shall** conform to the specifications found in [\[SP 800-185\]](#).
- 585 • Whenever an AES-CMAC algorithm is employed, the implementation of AES **shall**  
586 conform to [\[FIPS 197\]](#) and the AES-CMAC implementation **shall** conform to [\[SP](#)  
587 [800-38B\]](#).

588 As specified in [\[SP 800-56A\]](#) and [\[SP 800-56B\]](#), an **approved** key-establishment scheme  
589 can be implemented with parameters of various types and sizes that will impact the  
590 estimated maximum security strength that can be supported by the resulting scheme. When  
591 a key-establishment scheme employs a choice of parameters that are associated with a  
592 targeted security strength of  $s$  bits, the selection of a hash function, HMAC, KMAC, or  
593 AES-CMAC employed during the implementation of its key-derivation method **shall**  
594 conform to the following restrictions:

- 595 • An **approved** hash function **shall** be employed (whether alone or as the primitive  
596 used by HMAC) in the implementation of a one-step or two-step key-derivation  
597 method only if its output block length (in bits) is greater than or equal to  $s$ .
- 598 • For the purposes of implementing one-step key derivation only: KMAC128 **shall** be  
599 employed only in instances where  $s$  is 128 bits or less; KMAC256 **shall** be employed  
600 only in instances where  $s$  is 256 bits or less. (See, however, the note below.)
- 601 • For the purposes of implementing two-step key derivation only: AES-CMAC **shall**  
602 be employed only in instances where  $s$  is 128 bits or less. (See the note following  
603 [Table 5](#).)

604 Tables 1 through 5 (in Sections [4.1](#) and [5.1](#)) can be consulted to determine which hash

605 functions and/or MAC algorithms are **approved** for use when a key-derivation method  
606 specified in this Recommendation is used by an **approved** key-establishment scheme to  
607 support a targeted security strength of  $s$  bits.

608 **Note:** At the time of publication of this Recommendation, a key-establishment scheme  
609 implemented in accordance with either [\[SP 800-56A\]](#) or [\[SP 800-56B\]](#) can have a targeted  
610 security strength of at most 256 bits.

611

## 612 **8 Further Discussion**

613 In this section, the following issues are discussed:

### 614 **8.1 Using a Truncated Hash Function**

615 SHA-224, SHA-512/224, SHA-512/256 and SHA-384 are among the **approved** hash  
616 functions specified in [\[FIPS 180\]](#). SHA-224 is a truncated version of SHA-256, while  
617 SHA-512/224, SHA-512/256, and SHA-384 are truncated versions of SHA-512. (Each of  
618 these truncated versions uses a specific initial value, which is different from the initial  
619 value used by untruncated version.) In applications that require a relatively long bit string  
620 of derived keying material, implementing the key-derivation methods specified in this  
621 Recommendation with a truncated version of a hash function may be less efficient than  
622 using the corresponding untruncated version (i.e., SHA-256 or SHA-512).

### 623 **8.2 The Choice of a Salt Value**

624 In this Recommendation, the MAC algorithms employed either in a one-step key-  
625 derivation method or in the randomness-extraction step of a two-step key derivation  
626 method use a salt value as a MAC key (see Sections [4](#) and [5](#)). This Recommendation does  
627 not require the use of a randomly selected salt value. In particular, if there is no means to  
628 select a salt value and share it with all of the participants during a key-establishment  
629 transaction, then this Recommendation specifies that a predetermined default (e.g., all-  
630 zero) byte string be used as the salt value. The benefits of using “random” salt values, when  
631 possible, are discussed (briefly) in Section 3.1 (“To salt or not to salt.”) of [\[RFC 5869\]](#),  
632 and in greater detail in [\[LNCS 6223\]](#).

### 633 **8.3 MAC Algorithms used for Extraction and Expansion**

634 Provided that the targeted security strength can be supported (see Tables 4 and 5 in [Section](#)  
635 [5.2](#)), this Recommendation permits either HMAC-*hash* (i.e., HMAC implemented with an  
636 appropriately chosen **approved** hash function, *hash*) or AES-CMAC (i.e., the CMAC  
637 mode of AES-128, AES-192, or AES-256) to be selected as the MAC algorithm used in  
638 the randomness-extraction step of the key-derivation procedure specified in [Section 5.1](#).

639 The PRF-based KDF used in the key-expansion step of the procedure also requires an  
640 appropriate MAC (to serve as the PRF). While it may be technically feasible (in some  
641 cases) to employ completely different MAC algorithms in the two steps of the specified

642 key-derivation procedure, this Recommendation does not permit such flexibility. Instead,  
643 the following restrictions have been placed on MAC selection (see Sections [5](#) and [7](#)):

- 644 • When an HMAC-*hash* is chosen for use in the randomness-extraction step, the same  
645 MAC algorithm (i.e., HMAC-*hash* with the same **approved** hash function, *hash*)  
646 **shall** be employed to implement the PRF-based KDF used in the key-expansion  
647 step.
- 648 • When AES-128-CMAC, AES-192-CMAC, or AES-256-CMAC is chosen for use  
649 in the randomness-extraction step, the MAC algorithm employed by the PRF-based  
650 KDF used in the key-expansion step **shall** be AES-128-CMAC, the CMAC mode  
651 of AES-128. (AES-128 is the only AES variant that can employ the 128-bit  $K_{DK}$   
652 produced by AES- $N$ -CMAC during the randomness-extraction step.)
- 653 • The MAC algorithm selected for the implementation of a two-step key-derivation  
654 method **shall** be capable of supporting the targeted security strength, as determined  
655 by consulting Tables 4 and 5 in [Section 5.2](#). (This limits the use of AES-CMAC to  
656 cases where the targeted security strength is no more than 128 bits.)

657 The imposed restrictions are intended to reduce the overall complexity of the resulting  
658 implementations, promote interoperability, and simplify the negotiation of the parameters  
659 and auxiliary functions affecting the security strength supported by the key-derivation  
660 procedure.

661 **Note:** At this time, KMAC has not been specified for use in the implementation of a two-  
662 step key derivation procedure. This restriction may be reconsidered once a general-purpose  
663 KMAC-based KDF has been **approved** for use in the key-expansion step.

#### 664 **8.4 Destruction of Sensitive Locally Stored Data**

665 Good security practice dictates that implementations of key-derivation methods include  
666 steps that destroy potentially sensitive locally stored data that is created (and/or copied for  
667 use) during the execution of a particular process; there is no need to retain such data after  
668 the process has been completed. Examples of potentially sensitive locally stored data  
669 include local copies of shared secrets that are employed during the execution of a particular  
670 process, intermediate results produced during computations, and locally stored duplicates  
671 of values that are ultimately output by the process. The destruction of such locally stored  
672 data ideally occurs prior to or during any exit from the process. This is intended to limit  
673 opportunities for unauthorized access to sensitive information that might compromise a  
674 key-establishment transaction.

675 It is not possible to anticipate the form of all possible implementations of the key-derivation  
676 methods specified in this Recommendation, making it impossible to enumerate all  
677 potentially sensitive data that might be locally stored by a process employed in a particular  
678 implementation. Nevertheless, the destruction of any potentially sensitive locally stored  
679 data is an obligation of all implementations.

680

681 **Appendix A—References**

- 682 [SP 800-38B] NIST SP 800-38B, Recommendation for Block Cipher Modes of  
683 Operation – The CMAC Mode for Authentication, May 2005.
- 684 [SP 800-56A] Draft NIST SP 800-56A Rev. 3, Recommendation for Pair-Wise Key  
685 Establishment Schemes Using Discrete Logarithm Cryptography,  
686 August 2017.
- 687 [SP 800-56B] NIST SP 800-56B Rev. 1, Recommendation for Pair-Wise Key  
688 Establishment Schemes Using Integer Factorization Cryptography,  
689 September 2014.
- 690 [SP 800-57] NIST SP 800-57 Rev. 4, Recommendation for Key Management  
691 Part1: General, January 2016.
- 692 [SP 800-108] NIST SP 800-108, Recommendation for Key Derivation using  
693 Pseudorandom Functions, October 2009.
- 694 [SP 800-131A] NIST SP 800-131A Rev. 1, Transitions: Recommendation for  
695 Transitioning the Use of Cryptographic Algorithms and Key Lengths,  
696 November 2015.
- 697 [SP 800-135] NIST SP 800-135 Rev. 1, Recommendation for Existing Application-  
698 Specific Key Derivation Functions, December 2011.
- 699 [SP 800-185] NIST SP 800-185, SHA-3 Derived Functions: *cSHAKE*, *KMAC*,  
700 *TupleHash* and *ParallelHash*, December 2016.
- 701 [FIPS 180] FIPS 180-4, Secure Hash Standard, August 2015.
- 702 [FIPS 197] FIPS 197, Advanced Encryption Standard, November 2001.
- 703 [FIPS 198] FIPS 198-1, The Keyed-Hash Message Authentication Code (HMAC),  
704 July 2008.
- 705 [FIPS 202] FIPS 202, SHA-3 Standard: Permutation-Based Hash and Extendable-  
706 Output Functions, August 2015.
- 707 [RFC 5869] IETF RFC 5869 HMAC-based Extract-and-Expand Key Derivation  
708 Function (HKDF), May 2010.
- 709 [LNCS 6223] H. Krawczyk. “Cryptographic Extraction and Key Derivation: The  
710 HKDF Scheme”, *Advances in Cryptology - Crypto’2010, Lecture Notes  
711 in Computer Science Vol. 6223*, pp. 631-648. Springer. 2010.
- 712

**713 Appendix B—Revisions (Informative)**

714 The original SP 800-56C (published in November 2011) focused entirely on the  
715 specification of a two-step extraction-then-expansion key-derivation procedure to be used  
716 in conjunction with a key-establishment scheme from either [SP 800-56A](#) or [SP 800-56B](#);  
717 it provided an alternative to the one-step key-derivation functions that were already  
718 included in those companion publications.

719 The 2017 revision of SP 800-56C reorganizes the original content (it still includes the  
720 specification of an extraction-then-expansion key-derivation procedure) and also includes  
721 the specification of a family of one-step key-derivation functions, expanding on material  
722 that was previously found only in SP 800-56A and SP 800-56B. This change was made in  
723 support of the removal of detailed descriptions of key-derivation methods from SP 800-  
724 56A and a future revision of SP 800-56B. The consolidation of specifications in SP 800-  
725 56C revision 1 will promote consistency between the key-derivation options available for  
726 use with an **approved** key-establishment scheme chosen from either of those companion  
727 NIST publications. (There will, however, continue to be a number of application-specific key-  
728 derivation methods specified in [SP 800-135](#).)

729 Specifically named FFC, ECC, and IFC key-establishment “parameter sets” (FA – FC for  
730 finite-field cryptography; EA – EE for elliptic-curve cryptography; and IA – IB for  
731 integer-factorization cryptography) are no longer used as guides for choosing the auxiliary  
732 functions employed by a key-derivation method. Instead, SP 800-56C revision 1 indicates  
733 the security strengths that can be supported by the various possibilities for the auxiliary  
734 functions. Implementers are expected to let the targeted security strength of the key-  
735 establishment scheme guide their choices. Of course, each of the named parameter sets was  
736 associated with a targeted security strength, so this is more a change of perspective than of  
737 substance. The change is, however, consistent with the revision of [SP 800-56A](#), which will  
738 de-emphasize (in the FFC case) or eliminate (in the ECC case) the use of named  
739 parameter (size) sets.

740 There is one substantial change to the specification of key-derivation methods that is worth  
741 noting: a KMAC-based option for implementing the auxiliary function H has been added  
742 to the specification of one-step key-derivation functions (see [Section 4.1](#)). At this time,  
743 however, KMAC has not been specified for use as an auxiliary MAC algorithm in the two-  
744 step extraction-then-expansion key-derivation procedure (see [Section 8.3](#)).

745 Given the extent to which SP 800-56C has been revised, it is impractical to list all of the  
746 changes that have been made to the original text. It is recommended that SP 800-56C  
747 revision 1 be read in its entirety in order to gain familiarity with the details of the current  
748 specifications for both one-step and two-step key-derivation methods used in **approved**  
749 key-establishment schemes.